REPORT DO	<b>OCUMENTATION PA</b>	<b>GE</b> A	FRL-SR-BL-	-TR-01-
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1. AGENCY USE ONLY (Leave blank)	2. REPORT DATE August 28, 2001	3. REPORT TYPE AND Final Technical Report:	01/01/98 to 09	/30/98
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6. AUTHOR(S) Professor Richard B. Miles				
7. PERFORMING ORGANIZATION NA Princeton University Dept. Mechanical & Aerospace Engrg Olden St. Princeton, NJ 08544			8. PERFORMING REPORT NUI	G ORGANIZATION MBER
9. SPONSORING / MONITORING AG AFOSR/NA 801 North Randolph St. Room 732 Arlington, VA 22203-1977	GENCY NAME(S) AND ADDRESS(ES		10. SPONSORII AGENCY R	NG / MONITORING EPORT NUMBER
11. SUPPLEMENTARY NOTES  12a. DISTRIBUTION / AVAILABILITY	'STATEMENT			12b. DISTRIBUTION CODE
Approved for public release; distribut	ion is unlimited.			
This grant supported an Air Force-spe Princeton University, February 26-27 plasmas. This interest is, in part, mot ionized air plasmas is at a higher veloused for supersonic/hypersonic drag to and hypersonic propulsion systems. properties of these plasmas, are of sign	onsored workshop, "Understanding a 7, 1998. In recent years, there has been tivated by experiments conducted in I socity than would be predicted by presented to the predicted by presented	Russia and in the United a cently understood models.	States which indicate in the states which indicate in the state is, indeed low control devices	cate shock propagation in weakly, the case, such plasmas could be es, electromagnetic attenuation,
14. SUBJECT TERMS Air plasmas, Weakly ionized air plas	smas, AFOSR workshop	2	0011	15. NUMBER OF PAGES 2 plus 1 Appendix 16. PRICE CODE
17. SECURITY CLASSIFICATION OF REPORT Unclassified	18. SECURITY CLASSIFICATION OF THIS PAGE Unclassified	19. SECURITY CLASS OF ABSTRACT Unclassifi		20. LIMITATION OF ABSTRACT UL

### FINAL TECHNICAL REPORT (Dated 8/28/01)

AFOSR GRANT #F4920-97-1-0497, P00002 (150-6756)

### "SHOCK PROPAGATION AND SUPERSONIC DRAG IN LOW TEMPERATURE PLASMAS"

### SUPPORT FOR:

AFOSR-SPONSORED WORKSHOP ENTITLED:
"Understanding and Control of Ionized High-Speed Flows"
Princeton University
Princeton, NJ 08544
February 26-27, 1998

### **ABSTRACT**

This grant supported the costs of an Air Force-sponsored workshop, "Understanding and Control of Ionized High-Speed Flows," which was conducted at Princeton University, February 26-27, 1998. In recent years, there has been a great deal of interest in the formation mechanisms and properties of air plasmas. This interest is, in part, motivated by experiments conducted in Russia and in the United States which indicate shock propagation in weakly ionized air plasmas is at a higher velocity than would be predicted by presently understood models. If this is, indeed, the case, such plasmas could be used for supersonic/hypersonic drag reduction. In addition, atmospheric plasmas could influence flow control devices, electromagnetic attenuation, and hypersonic propulsion systems. As a consequence, the formation of such plasmas in atmospheric pressure environments, and the study of the properties of these plasmas, are of significant national interest.

### **DISCUSSION**

The purpose of the workshop was to highlight the basic science issues involved with controlling high-speed flows using weakly-ionized plasmas. The specific objectives of the two-day meeting were to review recent experimental/theoretical research in this area, and to exchange ideas/ understanding on the basic flow physics of the problem, and to discuss future research directions. Princeton University was a natural location for this workshop since work is underway here to examine both drag characteristics and electron discharge physics associated with weakly ionized plasmas.

Sixty individuals, each of whom is considered a leading authority on this issue, attended the two-day workshop (a full listing of the participants is located in Appendix A). The first day of the workshop consisted of four sessions on an agenda of twelve speakers and covered the following topics:

Session I: "Introduction to the Problem" (presentations by B. Ganguly of AFRL and A. Auslender of NASA LaRc).

Session II: "Aerodynamics of Ionized Flow" (presentations by R. Miles of Princeton University, J. Shang of AFRL, N. Malmuth and V. Soloviev of Rockwell Science, and V. Subramanian of The Ohio State University).

Session III: "Theory and Computation of Ionized Flows" (presentations by G. Karniadakis of Brown University, K. Powell of the University of Michigan, and S. Nazarenko of the University of Arizona).

Session IV: "Plasma Generation and Maintenance" (Presentations by S. Kuo of Polytechnic University, J. Kline of Research Support Instruments, and W. Rich of The Ohio State University).

The second day of the workshop, the participants were divided into four separate working groups for further discussion, followed by debriefings and laboratory tours at Princeton.

Appendix A is a complete record of the two-day workshop and includes the final agenda for the meeting, the complete list of participants and their contact information, as well as copies of each of the presentations for all of the four topic areas listed above.

Princeton University

School of Engineering and Applied Science Department of Mechanical and Aerospace Engineering

P.O. Box CN5263

Princeton, New Jersey 08544-5263



### FINAL AGENDA

### AFOSR-SPONSORED WORKSHOP:

### "UNDERSTANDING AND CONTROL OF IONIZED HIGH-SPEED FLOWS"

### February 26-27, 1998

**MEETING LOCATION:** 

Convocation Room (C217) Engineering Quadrangle

Olden Street, Princeton, NJ 08544

### THURSDAY, FEBRUARY 26, 1998:

SIGN-IN/COFFEE 7:30 AM OPENING REMARKS: G.L. Brown--Chairman, MAE Dept., Princeton 8:00 AM R. Miles--Princeton S. Walker--AFOSR INTRODUCTION TO THE PROBLEM 8:30 AM **SESSION I:** B. Ganguly--AFRL, A. Auslender--NASA LaRC DISCUSSION 9:30 AM 10:00 AM BREAK AERODYNAMICS OF IONIZED FLOW **SESSION II:** 10:30 AM R. Miles--Princeton, J. Shang--AFRL, N. Malmuth/V. Soloviev--Rockwell Science V. Subramanian--OSU 11:30 AM DISCUSSION 12:00 PM LUNCH SESSION III: THEORY AND COMPUTATION OF IONIZED FLOWS 1:30 PM G. Karniadakis--Brown U., K. Powell--UM, S. Nazarenko--UA 2:30 PM DISCUSSION BREAK 3:00 PM SESSION IV: PLASMA GENERATION AND MAINTENANCE 3:30 PM S. Kuo--Polytechnic Univ., J. Kline--RSI, W. Rich--OSU DISCUSSION 4:30 PM

### FRIDAY, FEBRUARY 27, 1998:

5:00 PM

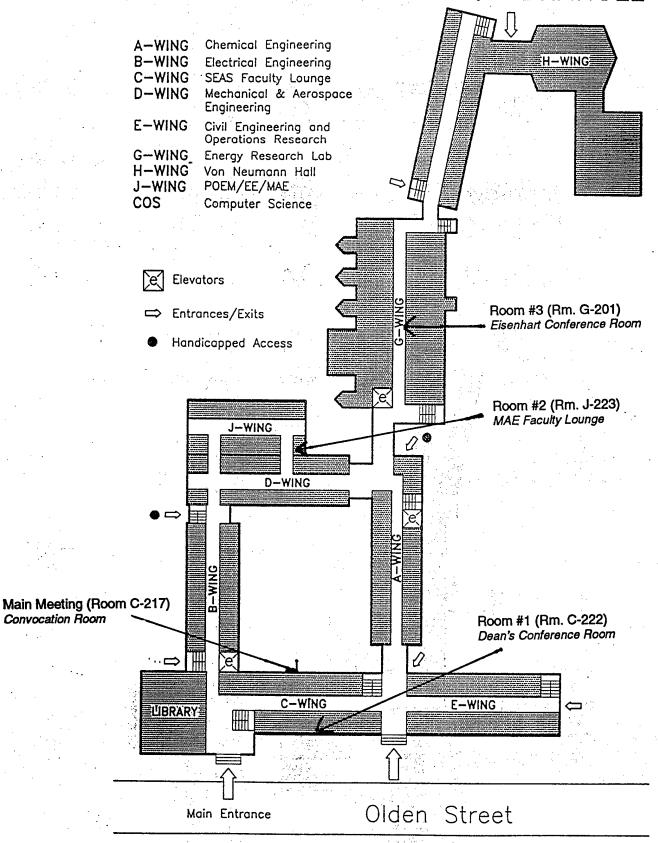
6:00 PM

7:30 AM	SIGN-IN/COFFEE
8:00 AM	OPENING REMARKS
8:15 AM	WORKING GROUPS
10:30 AM	BREAK
11:00 AM	GROUP DEBRIEFINGS
12:00 PM	LUNCH/LABORATORY TOUR

FIRST DAY WRAP-UP

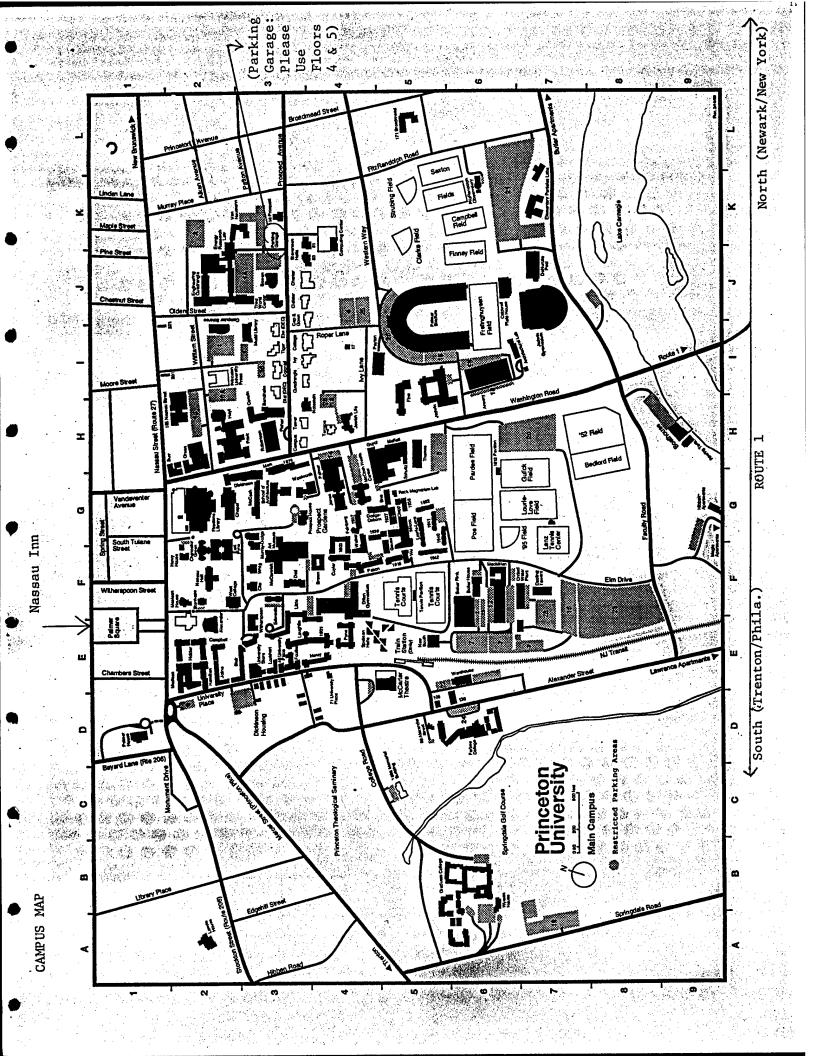
RECEPTION, Prospect House

ENGINEERING QUADRANGLE



COMPUTER SCIENCE BUILDING

Restrooms are located in the corners of the building where 2 wings meet.



### **PARTICIPANT LIST**

### AFOSR-SPONSORED WORKSHOP: "UNDERSTANDING & CONTROL OF IONIZED HIGH-SPEED FLOWS"

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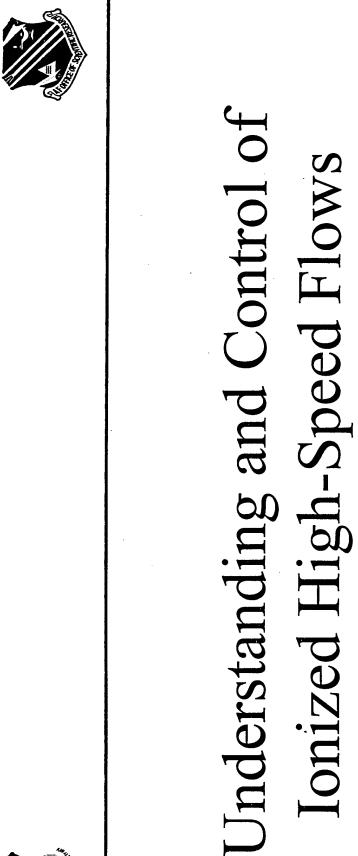
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AFOSR-Sponsored Workshop Princeton University

26-27 Feb 98

# NEW WORLD VISTAS (NWV)

- 41 Technologies Identified By AFMC And The Air Force Scientific Advisory Board
- 32 NWV Technologies To Receive Basic Research Support
- **\$14.8M Budget For FY 1997**

### HYPERSONICS

### **Objectives**

- Investigate Advanced Propellants And Aeropropulsion And Combined Cycle Hydrocarbon-Fueled Mach 8+ Cooling Concepts To Enable **Propulsion**
- Examine Electromagnetic Manipulation Of Ionized Flowfields To Improve Hypersonic Vehicle **Performance**



### POWER PROJECTION AND MOBILITY **NEW WORLD VISTAS**

### **TOPIC 08 - HYPERSONICS**

VEHICLE/PROPULSION SYSTEM PERFORMANCE RESEARCH ISSUE: IMPACT OF WEAKLY IONIZED FLOWS ON

RUSSIAN AYAKS FLIGHT VEHICLE CONCEPT

BOW SHOCK

MEASUREMENTS INDICATE THAT 'UNSTEADY ANALYSIS IS REQUIRED TO DESCRIBE ENERGY TRANSFER BETWEEN SHOCKS AND NONEQUILIBRIUM MEDIA (GANGULY, AFRL/PR)

EXPERIMENTAL RESULTS SHOW THAT REACTION WITH IONIZED AIR CAUSES HYDROCARBON FUEL COMPONENTS TO DECOMPOSE AND FORM REACTIVE FREE RADICALS (MORRIS, AFRLVS)



### Background



- changes in shock strength, speed, and Many experiments have shown large stand-off distance in weakly-ionized flows
- mechanisms for the observed shock Complete analysis of proposed dynamics is lacking
- US interest/research is increasing -USAFA June 97 workshop



## Purpose of Workshop



- with controlling high-speed flows using Highlight basic science issues involved weakly-ionized plasma
- Review recent basic research in the area
- Technical exchange on flow physics
- Discuss future directions

### FINAL AGENDA

### AFOSR-SPONSORED WORKSHOP:

### "UNDERSTANDING AND CONTROL OF IONIZED HIGH-SPEED FLOWS"

### February 26-27, 1998

MEETING LOCATION:

Convocation Room (C217) Engineering Quadrangle

Olden Street, Princeton, NJ 08544

### THURSDAY, FEBRUARY 26, 1998:

7:30 AM 8:00 AM	SIGN-IN/COFFEE  OPENING REMARKS: G.L. BrownChairman, MAE Dept., Princeton R. MilesPrinceton
8:30 AM	S. WalkerAFOSR SESSION I: <u>INTRODUCTION TO THE PROBLEM</u> B. GangulyAFRL, A. AuslenderNASA LaRC
9:30 AM	DISCUSSION
10:00 AM	BREAK
10:30 AM	SESSION II: <u>AERODYNAMICS OF IONIZED FLOW</u>
	R. MilesPrinceton, J. ShangAFRL,
	N. Malmuth/V. SolovievRockwell Science
	V. SubramanianOSU
11:30 AM	DISCUSSION
12:00 PM	LUNCH
1:30 PM	SESSION III: THEORY AND COMPUTATION OF IONIZED FLOWS
	G. KarniadakisBrown U., K. PowellUM, S. NazarenkoUA
2:30 PM	DISCUSSION
3:00 PM	BREAK
3:30 PM	SESSION IV: <u>PLASMA GENERATION AND MAINTENANCE</u> S. KuoPolytechnic Univ., J. BrandenburgRSI, W. RichOSU
_	•
4:30 PM	DISCUSSION
5:00 PM	FIRST DAY WRAP-UP
6:00 PM	RECEPTION, Prospect House

### FRIDAY, FEBRUARY 27, 1998:

7:30 AM	SIGN-IN/COFFEE
8:00 AM	OPENING REMARKS
8:15 AM	WORKING GROUPS
10:30 AM	BREAK
11:00 AM	GROUP DEBRIEFINGS
12:00 PM	LUNCH/LABORATORY TOUR



## Rules of Engagement



- Let's keep this science-oriented but relevant; we'll let someone else actually build AJAX
- Let's really attempt to better understand this stuff before we leave
- Let's critique the work, but not criticize the people
- Please don't say, "It's just a thermal effect"; prove it.
- Don't be afraid to ask questions; we have people from many diverse technical backgrounds here
- Government people never say stupid things (by default)
- Please treat the second day as your collective chance to shape the future AF basic research investment in this area
- Let's have <u>fun</u> 2 days without email, voice mail, dept. chairs, supervisors, etc.

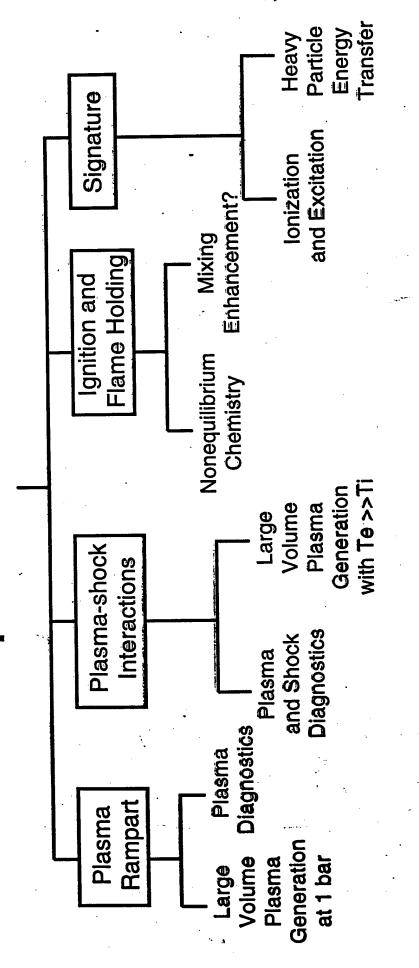
AFOSR Workshop

Princeton Univ

Feb 26, 1998

Dr. Bish Ganauly

## Nonequilibrium Air Plasma



### POTENTIAL PAYOFFS OF NONEQUILIBRIUM PLASMAS **TO HYPERSONICS**

- shock wave dissipation by Thermal problem minimized nonequilibrium plasmas
- Combustion efficiency improvement mixing enhancement by plasma interactions
- Drag reductions through boundary layer control
- Improve ignition and flame holding for subsonic to hypersonic combustor by nonequilibrium plasma chemistry

### EXPERIMENTAL OBSERVATIONS OF PLASMA-SHOCK INTERACTIONS

- Shock wave dispersion, damping and velocity increase (super thermal) are observed in glow discharges of both atomic and molecular gases
  - a. fractional ionization 107 to 103 b. gas temperature 300 to 1400 K
- Similar features are not observed in thermal plasmas
- Weak magnetic field impacts sound velocity
- Sound velocity change depends on Te
- UV illumination of the plasma is <u>claimed</u> to increase speed of sound in plasma

# CURRENT STATUS OF THE RESEARCH RESULTS

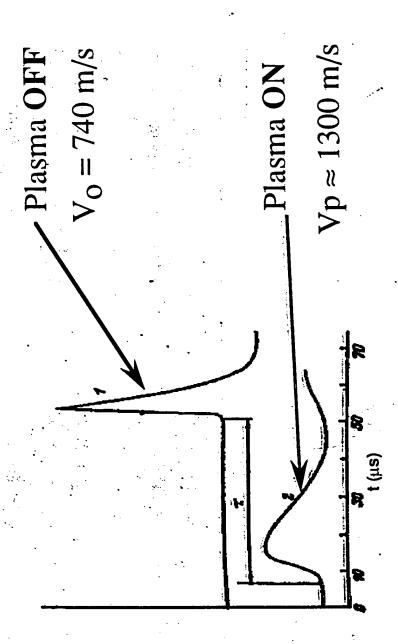
- DAMPING OF SHOCK WAVES IN WEAKLY IONIZED PLASMAS, ALSO SEVERAL GROUPS HAVE REPORTED INCREASED DISPERSION AND HIGHER SHOCK PROPAGATION VELOCITIES
- RESEARCHERS ASCRIBED THE EFFECTS TO THE A PLASMAS, OTHERS TO THE TEMPERATURE GRADIENT FORMED IN PLASMAS NÖNEQUILIBRIUM PLASMAS, OF THE SOME
- ACCURATE THEORETICAL MODEL EXISTS FOR SMALL AMPLITUDE AUDIO FREQUENCY ACOUSTIC WAVE PROPAGATION IN PLASMAS
- WAVE SHOCK FOR PROPAGATION IN NONEQUILIBRIUM PLASMAS **EXIST** DOES NOT ACCURATE MODEL



### Shock Wave Propagation in a Weakly Ionized Low-pressure Discharge

### Plasma Parameters

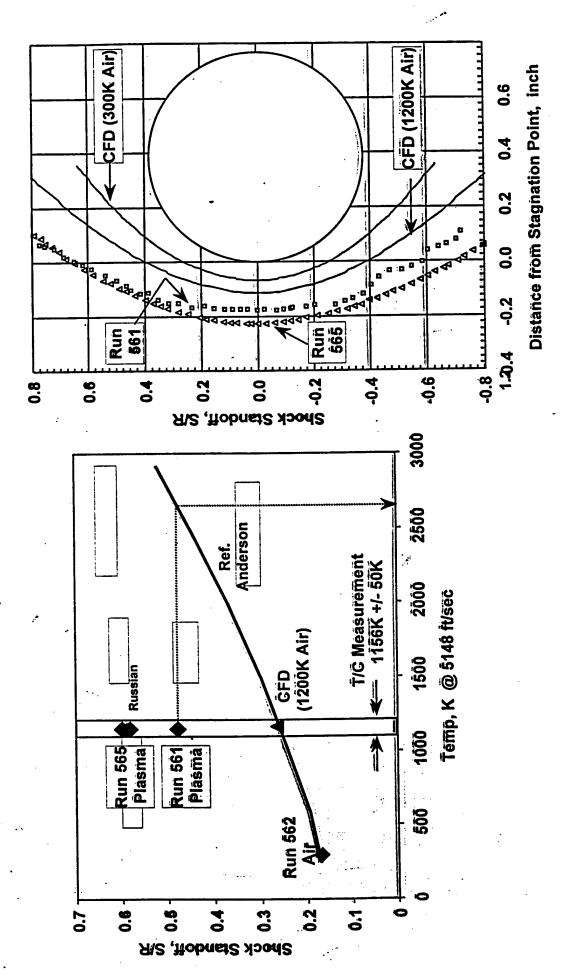
$$p = 30 \text{ torr}$$
  
 $J = 3 \text{ mA/cm}^2$   
 $T_g = 800 \text{ K}$ 



A. I. Klimov et al., Sov. Tech. Phys. Lett. 8, 192 (1982)

# Shock Standoff Comparison to Predictions

(0.75 in. diam, 30 torr)



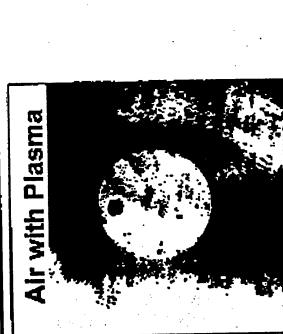
### RESEARCH TOPICS OF INTEREST

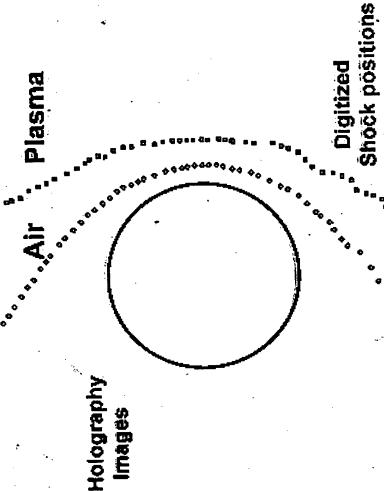
- MACH NO. DEPENDENT SHOCK WAVE ATTENUATION AND DISPERSION VS. GAS PRESSURE AND CURRENT DENSITY
- SIMULTANEOUS MULTIPOINT MEASUREMENTS
  - GAS HEATING EFFECTS
- LINEAR/NONLINEAR ENERGY COUPLING
  - ENERGY TRANSFER MÉCHANISM
- ENERGY EXCHANGE MECHANISMS
- CHARGE EXCHANGE EFFECTS
- AMBIPOLAR ELECTRIC ELECTRON ENERGY ENHANCEMENT BY FIELD
  - KINETIC TO ELECTROSTATIC ENERGY TRANSFER

# Initial Replication of Russian Results at AEDC

(0.75-in diam sphere, 30 torr)





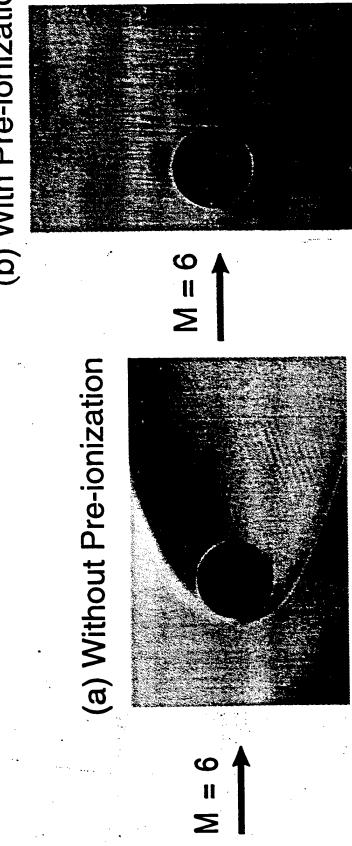


# Weakly lonized Gas Research Russian Ballistic Tests (G. Mishin & A. Kilmov, 1978)

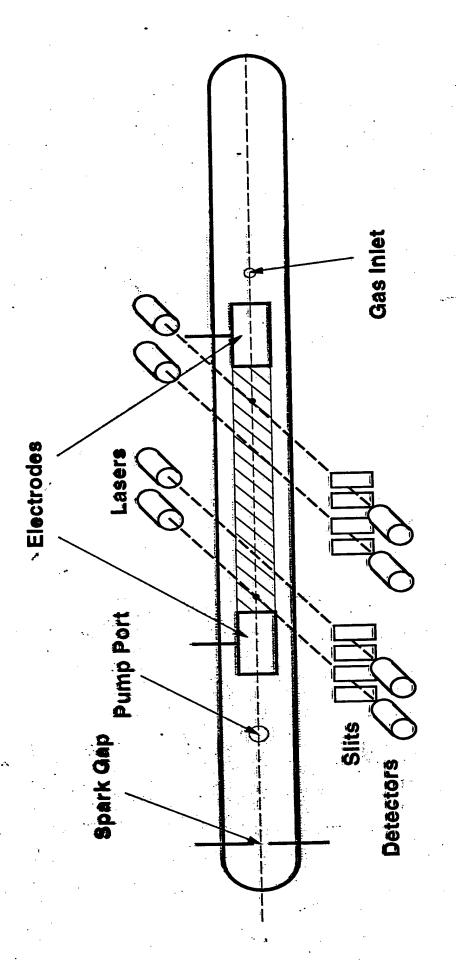
Effect of pre-ionization on the flow around a sphere at Mach 6

in air

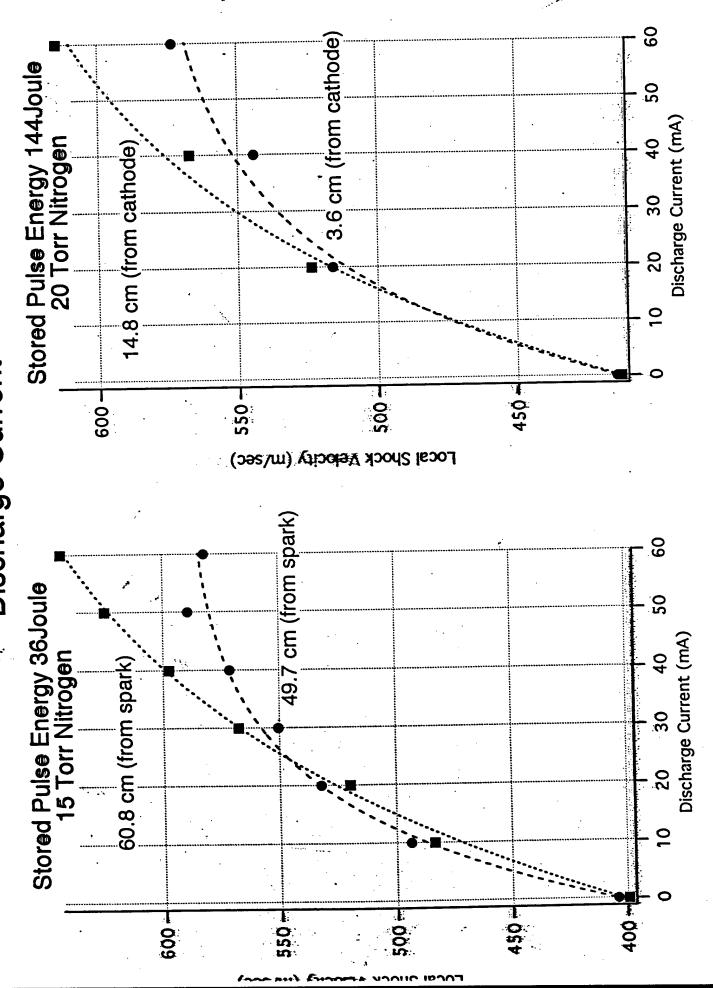
(b) With Pre-ionization



### Schematic of Experiment



# Local Velocity in Discharge as Function of Discharge Current



### SHOCK WAVE INTERACTIONS WITH WEAKLY IONIZED GASES

- Confirmed shock wave relaxation in nonequilibrium plasmas
- Occurs even at 10<sup>7</sup> fractional ionization
- Measurements demonstrated highly non-linear interactions of acoustic shock wave with non-equilibrium weakly ionized plasmas
- interaction quantify 2 performed mechanisms and energy balance Measurements need to be
- Data will be required to permit energy efficiency analysis of plasma based drag reduction and shock wave amplitude control

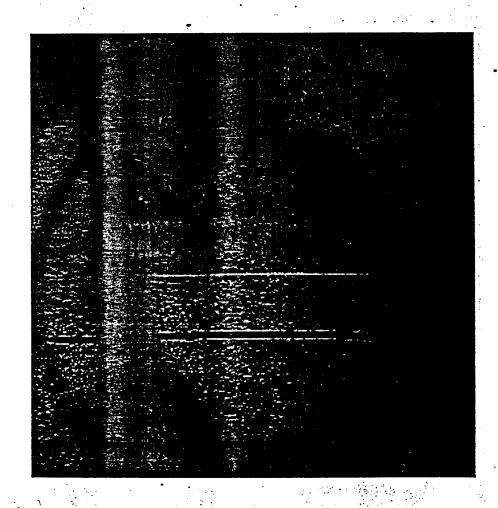
# **OUR PLANNED RESEARCH FOR FY98-99**

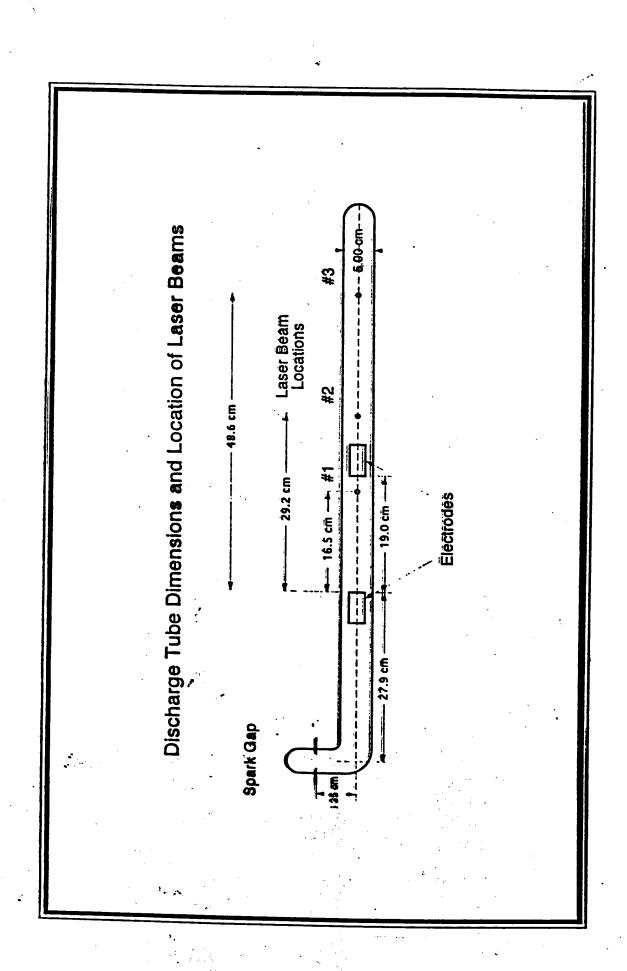
- Simultaneous multi-point local shock wave velocity measurements.
- Spectroscopic measurement of gas temperatures.
- Shock wave structure recovery in decaying plasma and neutral gas.
- 2-D Schlieren imaging of shock profiles.
- Spectroscopic measurement of shock wave density profile.
- Shock dispersion measurements in pulsed and radio frequency discharges.
- Shock propagation in double layer plasmas.
- Shock induced electric field modulation measurements.

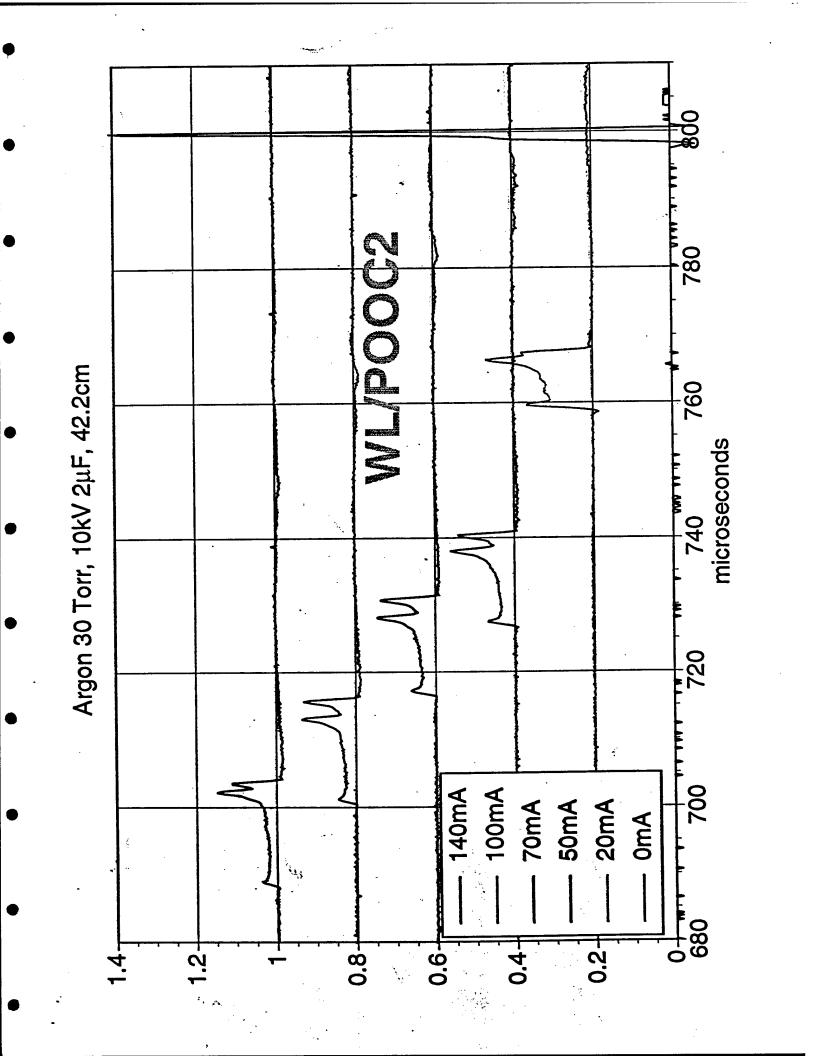
### SUMMARY

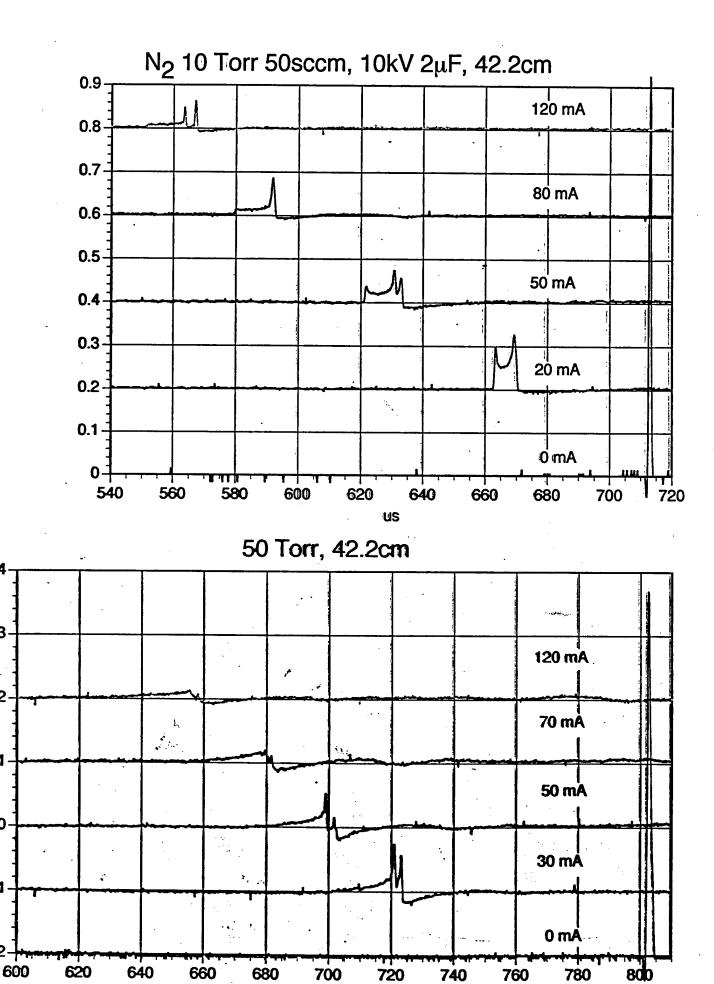
- Data show the dissipation of supersonic shock waves is nonlinearly dependent on amplitude in weakly ionized nonequilibrium plasmas
- Spatially resolved measurements indicate that shock propagation velocity change and dispersion cannot be explained by gas heating
- gas Shock wave dispersion and damping are dependent on the number density and fractional ionization
- The energy coupling mechanisms are not understood at present
- Plasma energy density and single particle collision frequency are inadequate to explain the observed phenomena
- Long range cooperative interactions may be important

A Comparison of the Shock Thickness With a 0.8 mm Diameter Wire, 30 Torr Argon, Pulser Voltage 9kV









US

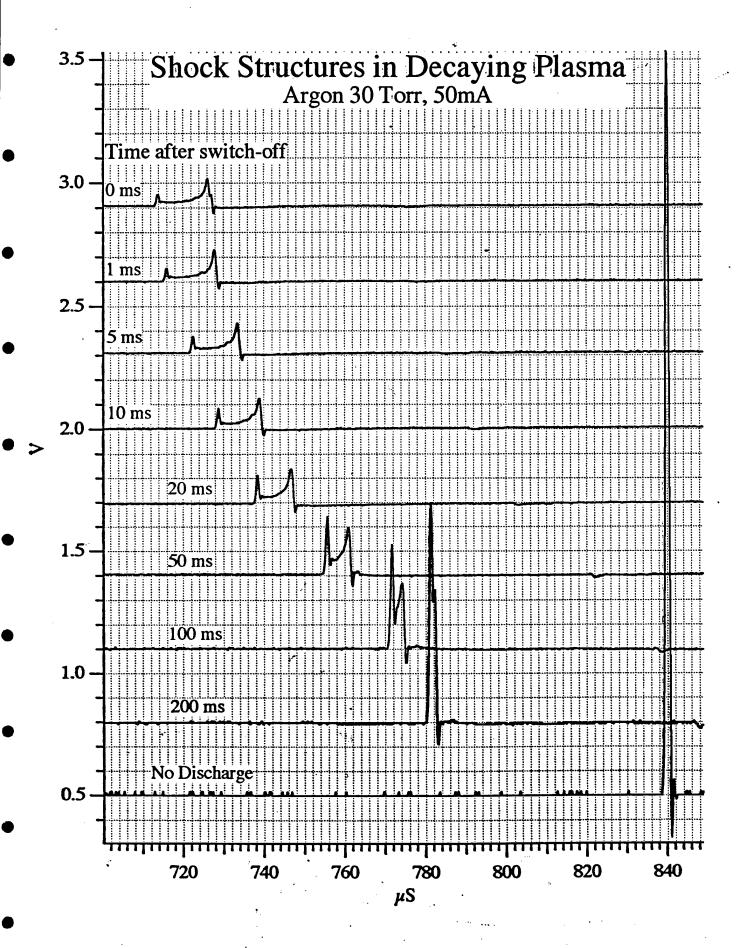
0.4

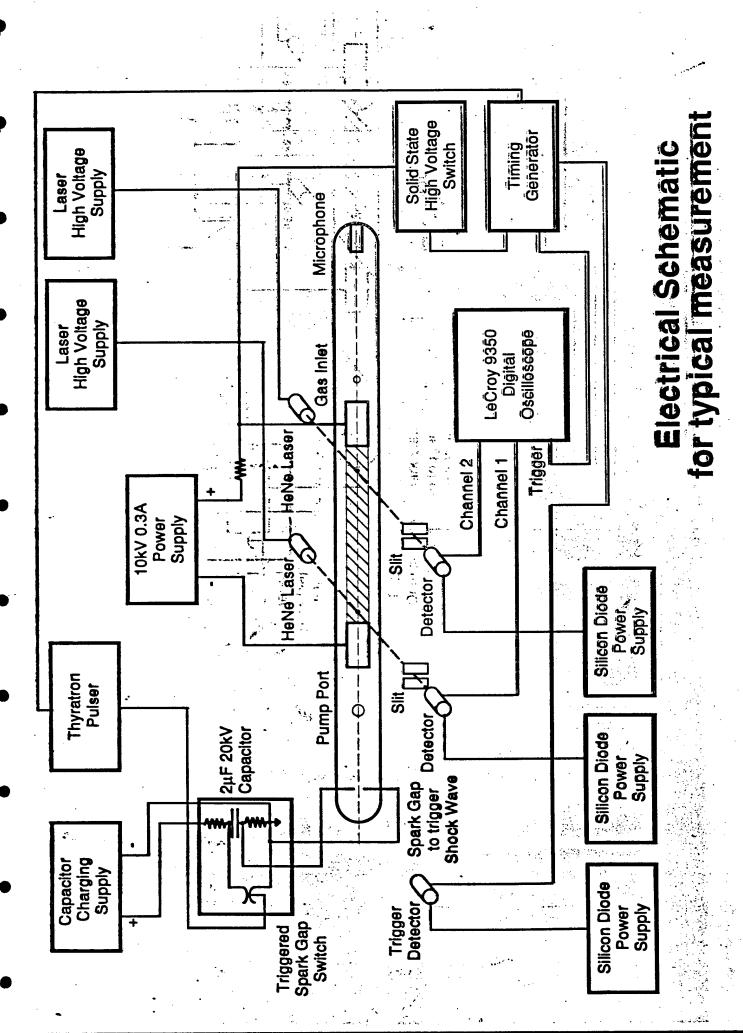
0.3

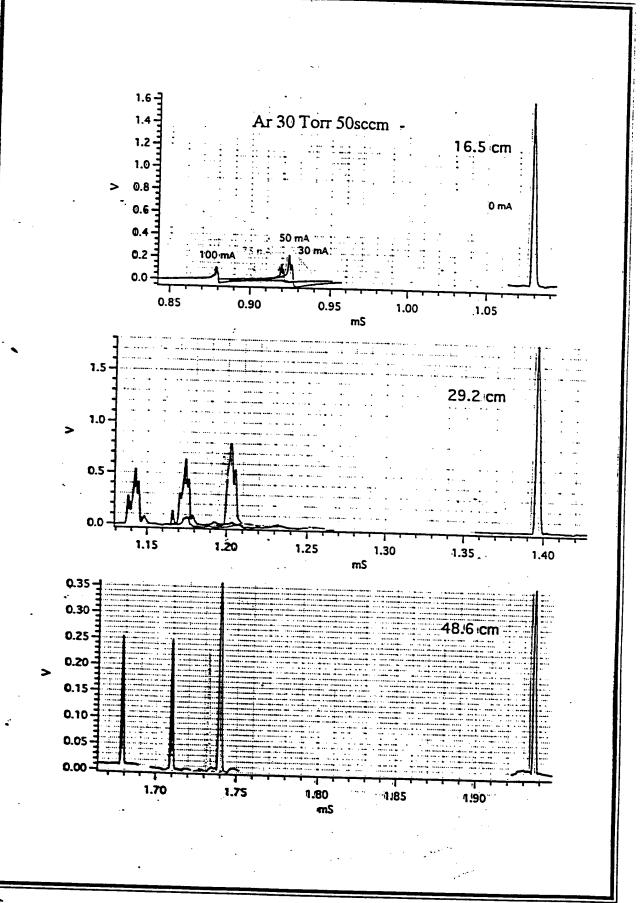
0.1

0

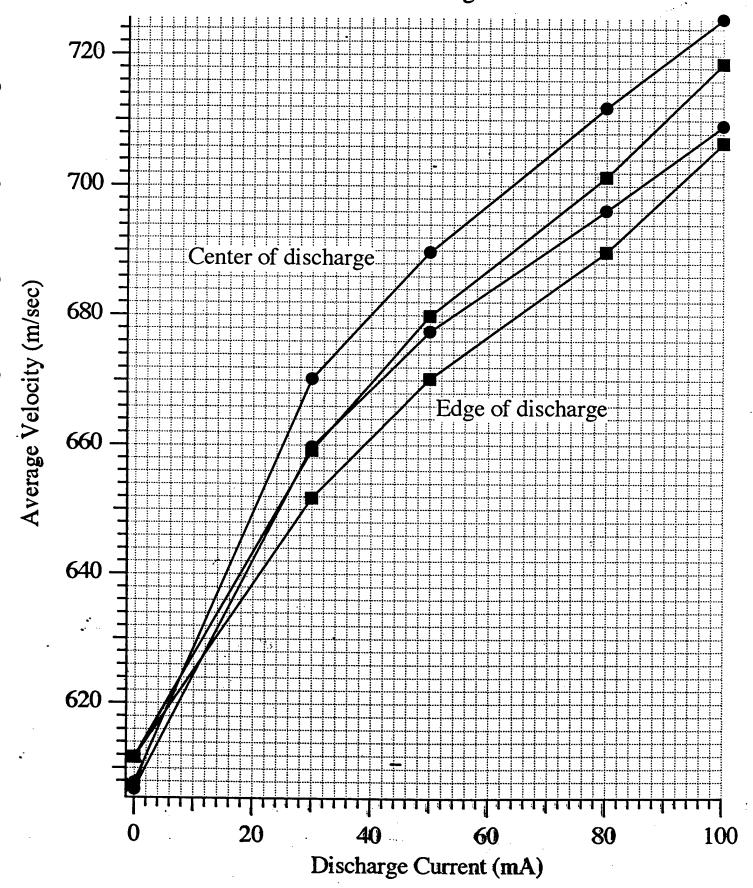
-0.1





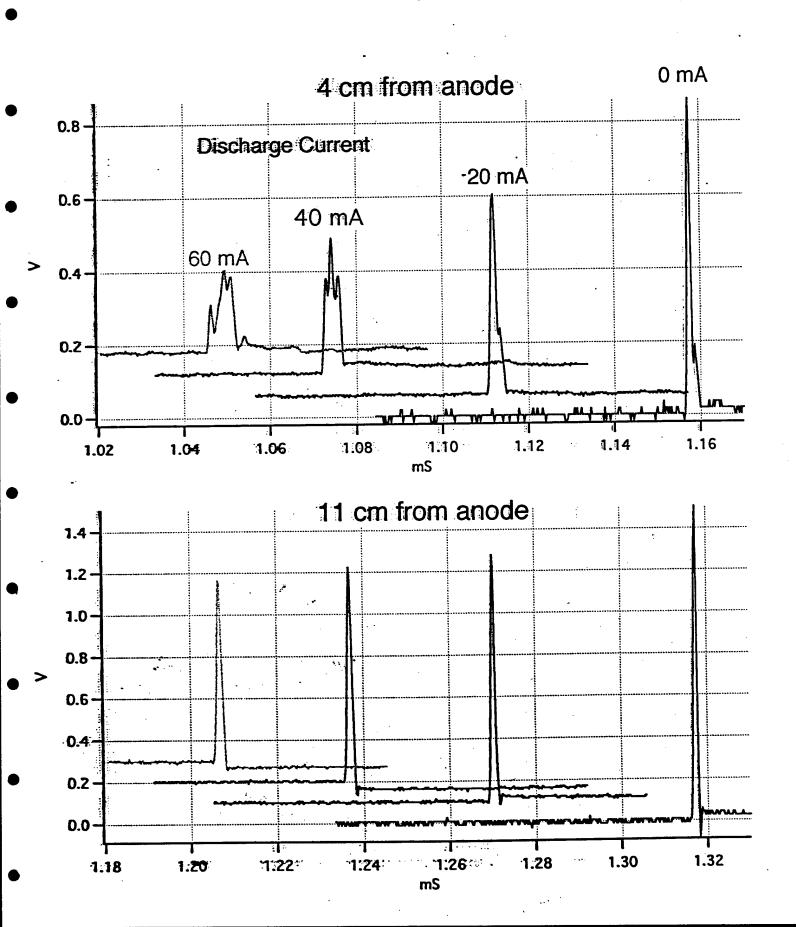


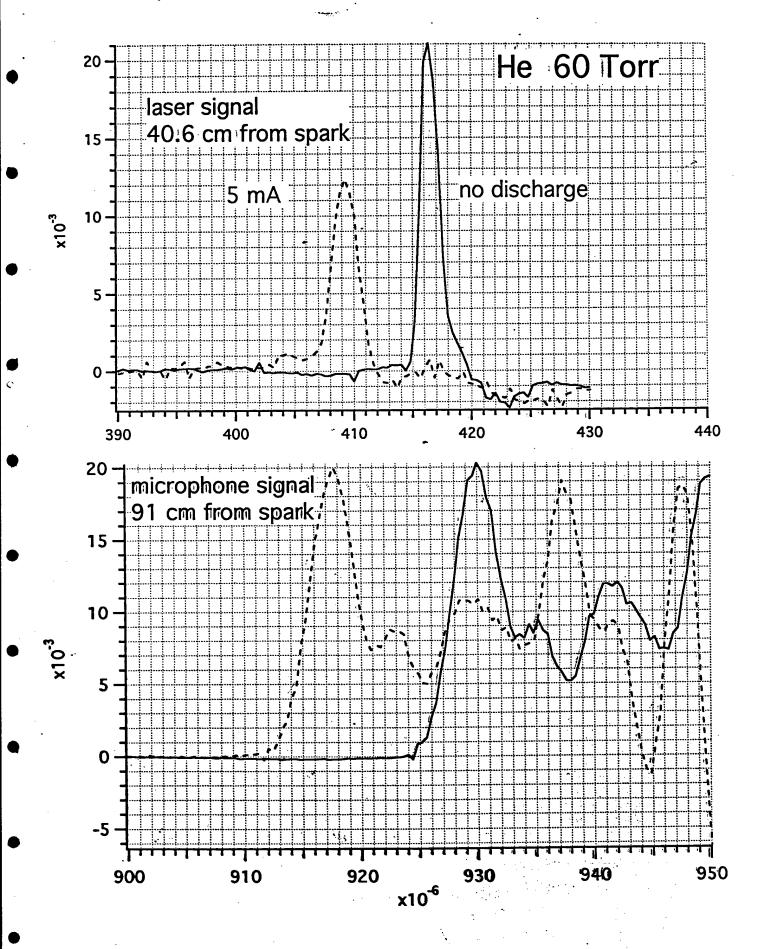
#### Average Velocity of Front and Back Boundaries of Shockwave at Center and Off-Axis as Function of Discharge Current



#### Deflection Signals Downstream of Discharge

Pulse Energy 81 Joule





## NASA Langley Research Center

UNDERSTANDING AND CONTROL OF IONIZED HIGH-SPEED FLOWS

AFOSR WORKSHOP PRINCETON UNIVERSITY FEBRUARY 26–27, 1998 Plasma Drag Reduction — An Overview of the Issues
Aaron Auslender
NASA Langley Research Center

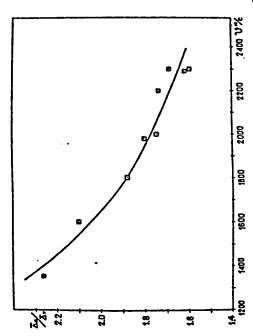
## NASA Langley Research Center -

### OUTLINE

- Problem Statement and Related Issues
- Present Research Focus NASA/LaRC and ICASE
- Analysis of Air Force Experiments ODU
- Ballistic Range Mechanisms ODU
- Onboard-Microwave Experiments NASA/LaRC
- Shock Tube Experiments FA&M

## flow around a sphere moving supersonically in a gas-discharge plasma

G. I. Mishin, Yu. L. Serov, and I. P. Yavor Pis'ma Zh. Tekh. Fiz. 17, 65-71 (June 12, 1991) (Submitted April 11, 1991)



at the same temperature as the plasma  $(\vec{\Delta}_p$  is the relative standoff distance of the bow shock in the plasma,  $\vec{\Delta}_T$  is the relative standoff distance in air FIG. 2. Ratio of experimentally determined relative standoff distance of the bow shock from a sphere moving through a glow-discharge plasma to the corresponding calculated value of the relative standoff distance in air at T = 1350 K, and v is the velocity of the sphere).

414 Sov. Tech. Phys. Lett. 17(6), June 1991

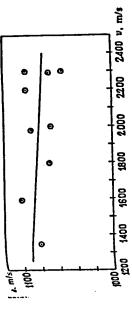
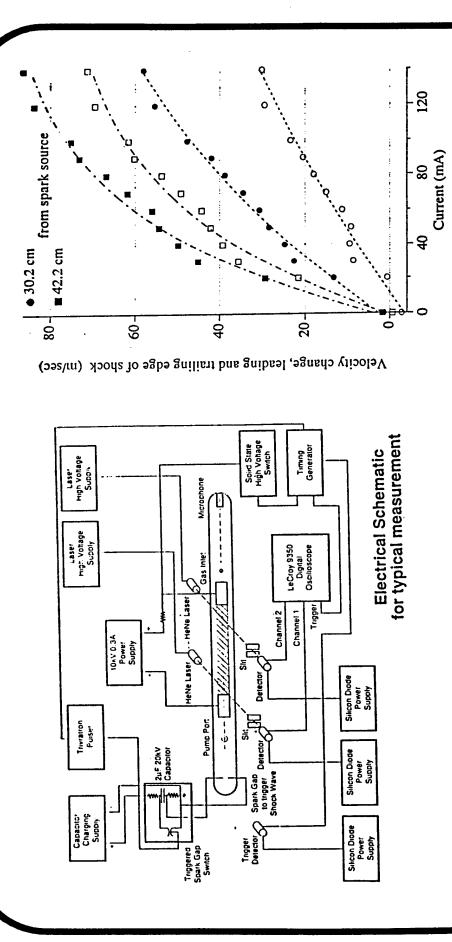


FIG. 3. "Effective" (governing the flow pattern) sound velocity in a plasma in the range of velocities of a spherical model 1350-1300 m/s (a is the effective sound velocity, and v is the velocity of the sphere).

was  $\alpha=10^{-5}-10^{-6}$ , and the electron temperature was  $T_{\rm e}=1-4~{\rm eV}$ . The gaskinetic temperature  $T_{\rm e}$  of the plasma was The main series of experiments was carried out in a steadily burning discharge at a gas pressure of 40-50 torr and a discharge current density of 25-50 mA/cm<sup>2</sup>. The electron density was = 10-11-10-12 cm-3, the ionization coefficient determined by several techniques: by measuring the density Chromel-Alumel thermocouple, by radiation pyrometry, and from the electron vibration-rotation spectra of the molecules.2 The measurements showed that the temperature distribution along the diameter is bell-shaped, with  $T_R \le 1400 \text{ K}$ gas from interferograms, by of the

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## NASA Langley Research Center



## ACOUSTIC SHOCK WAVE PROPAGATION IN NONEQUILIBRIUM NITROGEN AND ARGON PLASMAS

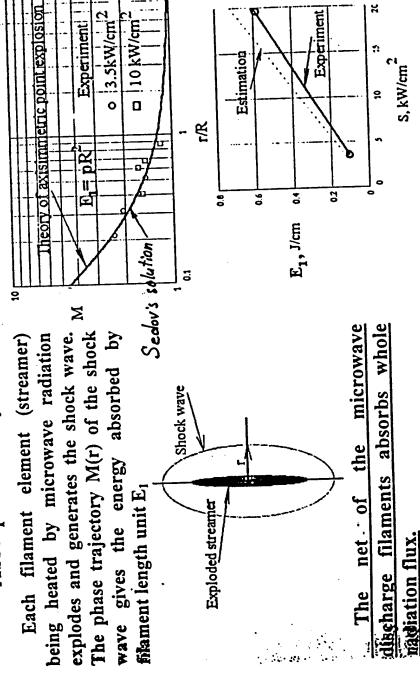
B. N. GANGULY AND P. BLETZINGER WRIGHT LABORATORY, WRIGHT-PATTERSON AFB

AFOSR / High-Speed Workshop

Undercritical Microwave Discharge Supersonic Aerodynamics and and Its Influence on the Physics of the Shock Waves

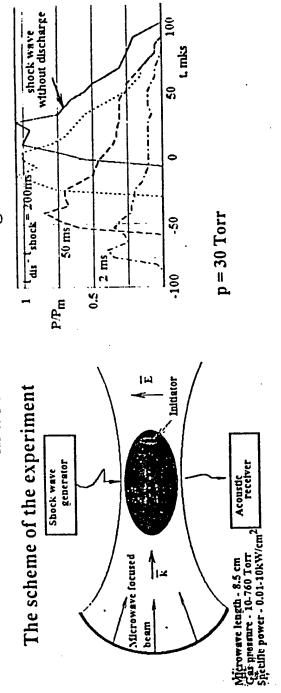
K. Khodataev (MRTI)

Absorption Ability of the Microwave Streamer Discharge



naction flux.

The Experimental Data about a Shock Wave Attenuation in a Microwave Discharge



The typical oscillograms
The measurements show that discharge region:

- attenuates the pulse shock waves,
- increases the pulse shock wave time duration,
- •the memory time of discharge region equals more than 0.1 s.

## The Acoustic Interferometry Study of the Microwave Discharge Region

The sound velocity dependence

on wave number C<sub>s</sub>(k) in the decaying microwave discharge plasma.

The delay time after discharge: 20 ms -solid, 50 ms -dot, 200 ms-dash line.

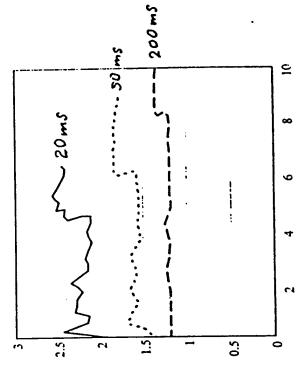
The dependence show that:

is heated in average,has microscale

inhomogeneties,

hot

• has a memory time up to 0.2s.



 $H = \frac{2\pi}{\lambda}$  -acoustic wave length

## NASA Langley Research Center -

$$\frac{\partial \mathbf{v}_n}{\partial t} = -c_n^2 \nabla \rho_v / \rho_{0v} - \omega_{ni} (\mathbf{v}_n - \mathbf{v}_i)$$

$$\frac{\partial \rho_v}{\partial t} = -\rho_{0v} \nabla \cdot \mathbf{v}_n$$

$$\frac{\partial \mathbf{v}_i}{\partial t} = -c_i^2 \nabla \rho_u / \rho_{0u} - \omega_{in} (\mathbf{v}_i - \mathbf{v}_n)$$

$$\frac{\partial \rho_u}{\partial t} = -\rho_{0u} \nabla \cdot \mathbf{v}_i$$

$$\mathbf{v}_n = \nabla \phi_n$$
$$\mathbf{v}_i = \nabla \phi_i$$

(3)

$$\frac{\partial^2 \phi_n}{\partial t^2} - c_n^2 \nabla^2 \phi_n + \omega_{ni} \left( \frac{\partial \phi_n}{\partial t} - \frac{\partial \phi_i}{\partial t} \right) = 0$$
$$\frac{\partial^2 \phi_i}{\partial t^2} - c_i^2 \nabla^2 \phi_i + \omega_{in} \left( \frac{\partial \phi_i}{\partial t} - \frac{\partial \phi_n}{\partial t} \right) = 0$$

 $\widehat{\mathbb{S}}$ 

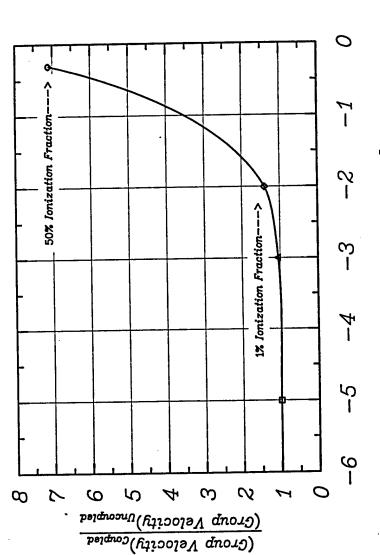
$$\begin{vmatrix} -\omega^2 + c_n^2 k^2 - i\omega\omega_{ni} & i\omega\omega_{ni} \\ i\omega\omega_{in} & -\omega^2 + c_i^2 k^2 - i\omega\omega_{in} \end{vmatrix} = 0 \tag{4}$$

## NASA Langley Research Center

- Analysis assumed:
- (1) Uncoupled Speed-of-Sound Ratio "Fast-Wave" to the "Slow-Wave" equals ten
- (2) Ionization Fraction is constant

- Conclusion:
- (1)"Slow-Wave" only propagates in
- the long-wave-length limit
- (2) Large Ionization Fractions are

required ("Slow-Wave")



Log<sub>10</sub> [Ionization Fraction]

Plasma Drag Reduction Physics

## NASA Langley Research Center

## PRESENT RESEARCH EFFORTS

- Kinetics
- Excited State —> reactions —> "hot" electron production
- Metastable States ---> "long-lived" neutrals
- --- yields mass/momentum/energy fluxes • Far-From Equilibrium Effects --> neutral particle stationary solutions of the Boltzmann kinetic equation having sources/sinks (fluxes) in the shock region (OSU) ---> influences speed-of-sound
- Far-From Equilibrium Effects (OSU, NASA/LaRC and ICASE)
- DSMC Modelling (NASA/LaRC and ICASE) employing a central forcing function of the class: Force =  $\alpha_0 e^{-(X-X_{SHOCK})^2/\alpha_1}$ to assess the magnitude of the required mechanism(s)
- Development of related mechanism(s) and analysis of the relevant "fluid" equation set (OSU)

## Shock-Wave Structure in a Rigid Sphere Gas1

G. A. BIRD<sup>2</sup> Department of Mechanics of Fluids, University of Manchester, Manchester, England

### Translational Equilibrium in a Rigid Sphere Gas

G. A. Bind Department of Aeronautical Engineering, University of Sydney, Sydney, Australia (Received 10 May 1963)

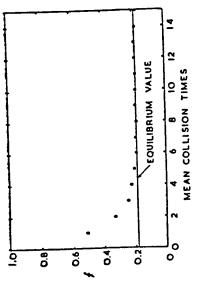


Fig. 2. Fraction of molecules in range 0.9 to 1.1 ".

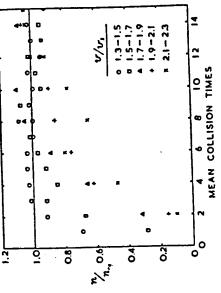


Fig. 3. Approach to equilibrium in higher speed ranges.

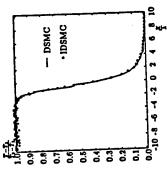
# Exact power-law solutions of the particle kinetic equations

A. V. Kats, V. M. Kontorovich, S. S. Moiseev, and V. E. Novikov

Khar'kov Research Institute for Metrology.

Institute for Radiophysics and Electronics. Circuit Academy of Sciences, and Physico-technical Institute, Ukrainian Academy of Sciences

(Submitted November 21, 1975) Zh. Eksp. Teor. Fiz. 71, 177-192 (July 1976)



6.11 shock-wave

# ODU Research Activity

- Analysis of planar-wave experiments
- shock front propagation
- Analysis of ballistic range experiments
- standoff distance
- Determination of underlying physical mechanisms
- distribution of internal energy
- collisional dynamics during relaxation
- influence of double electric layer on charged and excited particles
- nonequilibrium effects
- Shock dispersion experiments and plasma generation (future work)

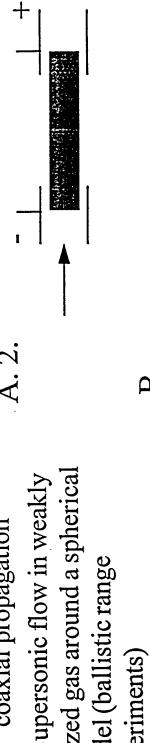
## in Atomic & Molecular Gases at Te>Tn "Anomalous" Effects

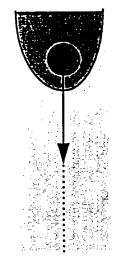
- Not observed at  $T_e = T_n$ .
- Not dependent on direction of applied electric field.
- Reduced/nonexistant at transverse magnetic field of below/above  $\sim 500$  G.
- Increase with ultraviolet irradiation.
- Rise-time from plasma inception ~100 µs.
- Afterglow decay time depends on gas species.

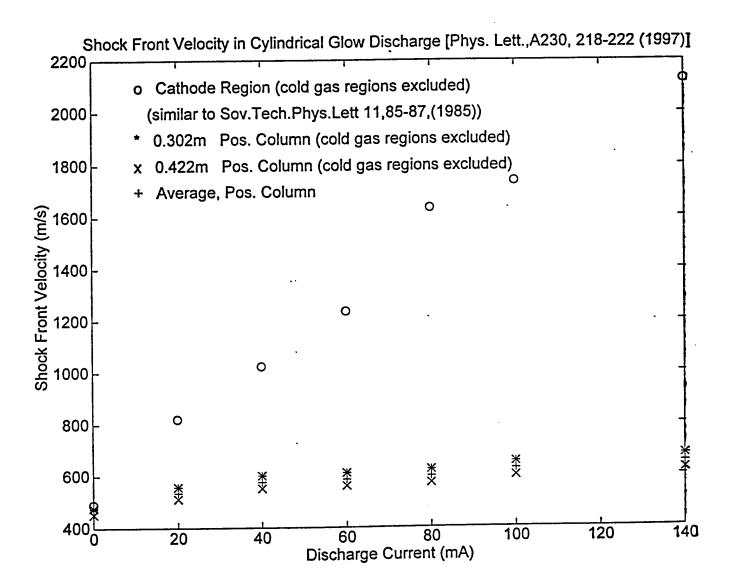
Can be >100 ms.

# Generic Experiments

- through a DC glow discharge A. Shock wave propagation
- transverse propagation 1. parallel-plate
- coaxial propagation 2. cylindrical
- ionized gas around a spherical B. Supersonic flow in weakly model (ballistic range experiments)





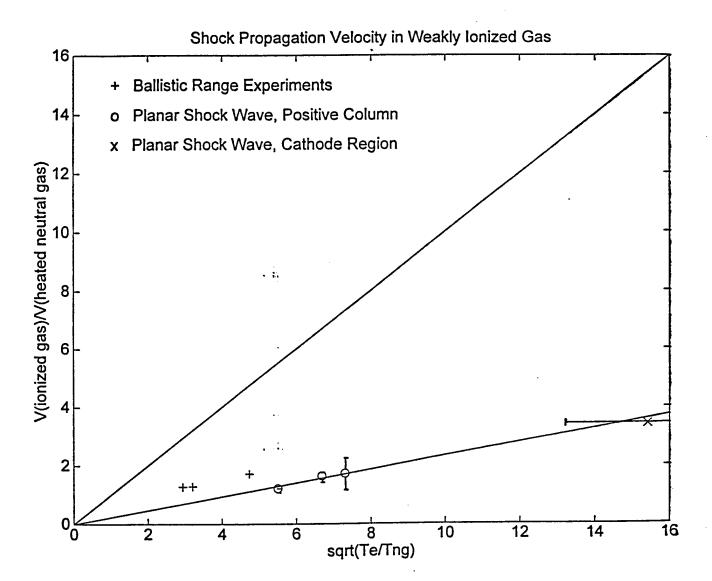


# Metastable States

- Oxygen
- Nitrogen
  - Argon

183,5

- $a^{1}\Delta_{g}$   $A^{3}\Sigma_{u}^{+}$
- (0.97 5) eV(6.17 - 8.83) eV
- 11.55 eV & 11.72 eV
- (12.91 13.48) eV



# Relevant Collision Processes

Electron impact ionization

Dominant ionization mechanism at high pressures.

$$Ar^* + e^- => Ar^+ + e^-(0 \text{ to 4 eV})$$

Energy pooling reactions

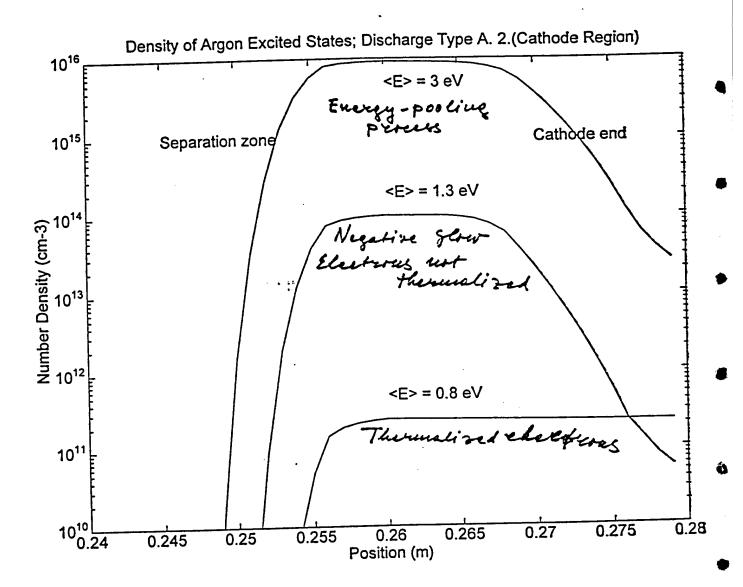
Dominant ionization mechanism at medium pressures.

$$Ar^* + Ar^* => Ar + Ar^+ + e^-(5 \text{ to } 15 \text{ eV})$$
  
=>  $Ar^* + Ar^+ + e^-(0 \text{ to } 4 \text{ eV})$ 

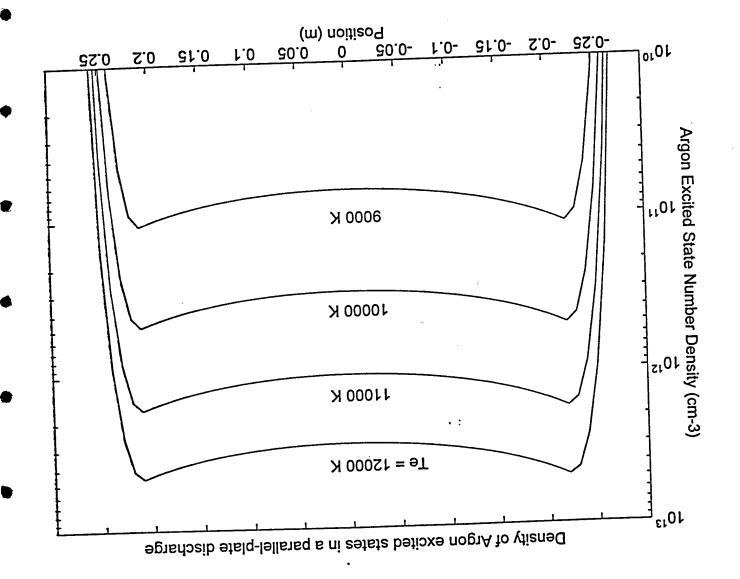
(Density breakdown, "oven effect" of Rydberg states).

Charge Transfer

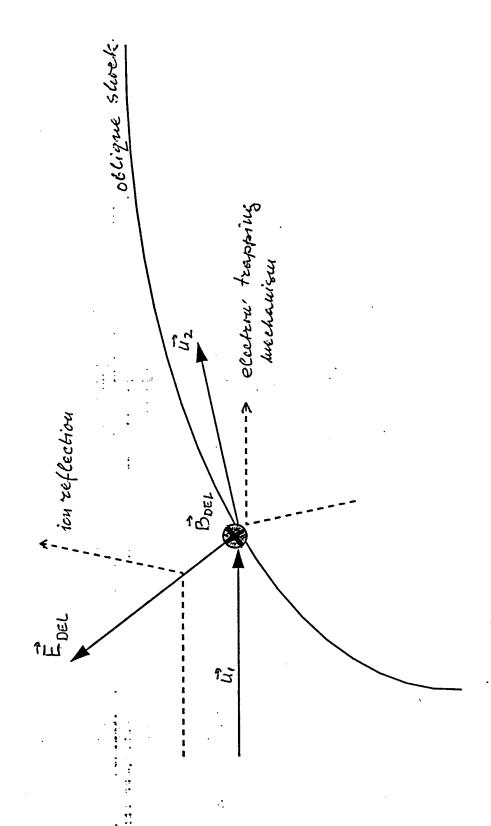
$$Ar^+(fast) + Ar => Ar(fast) + Ar^+$$



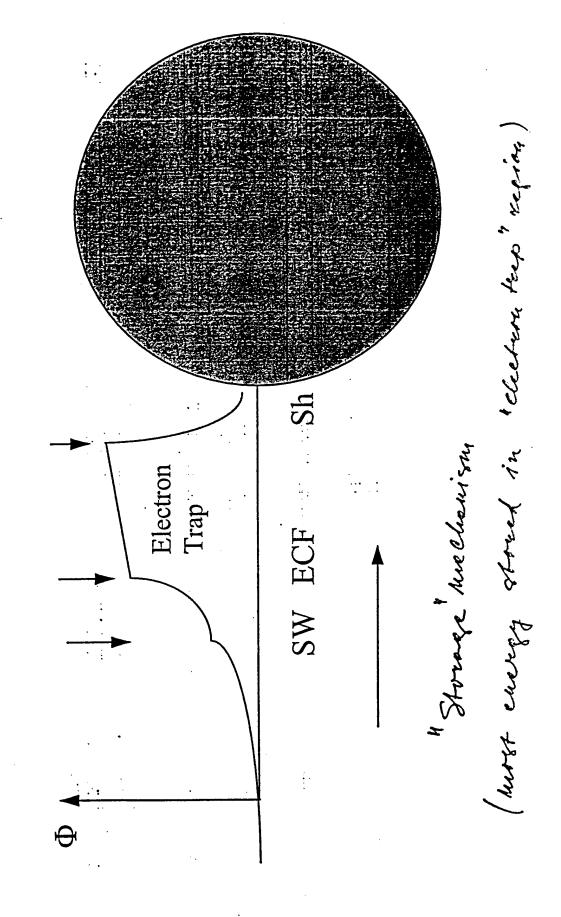
: :**:** 



# EM Field at DEL



## Electric Potential Distribution on the Centerline



## Shock Structure

### Relaxation (ECF)

Shock wave (SW)
"Precursor"

Centerline

### Precursor

"Leader"

### Effects which Follow Initial Perturbation

### - Ion dynamics

- Shock wave generates a Double Electric Layer (DEL).
- DEL generates an ion acoustic wave.
- Local increase of ion density traveling with the wave.
- · Slow ions reflected from DEL.

## - Electron dynamics

- Moving DEL induces transversal B field.
- B field confines slow electrons.
- Fast electrons escape DEL.
- Most electrons trapped in relaxation zone
- Electrons heated by inverse bremstrahlung.

### Precursor

- Fast Ions reflected and accelerated on DEL
- able to excite and ionize atoms and molecules
- Fraction of hot electrons heated by:
- inverse bremstrahlung (observed difference in population of resonant and metastable states)
- energy pooling reactions
- Mechanisms:
- A. Ion-acoustic wave
- B. Ionization wave generated by heavy particles (fast ions and neutrals)?
- C. Onset of turbulence by angular momentum transfer in energy pooling reactions?

# ON-BOARD GENERATION OF A "PRECURSOR" MICROWAVE PLASMA AT MACH 6: EXPERIMENT DESIGN

R. J. EXTON

NASA AERONAUTICS AND SPACE ADMINISTRATION LANGLEY RESEARCH CENTER

# MACH 6 PLASMA/DRAG REDUCTION TEAM

MEMBER

PRIMARY RESPONSIBILITY

R. J. EXTON

EXPERIMENT DEFINITION VISUALIZATION/LASERS

R. J. BALLA G. J. BRAUCKMANN

MODELS/FACILITY

M. DIFULVIO

FACILITY OTERS

W. E. LIPFORD

OPTICAL SUPPORT

MICROWAVE (EXPERIMENT)

J. FUGITT\*

MICROWAVE (THEORY)

M. C. BAILEY

NUCLEAR SOURCES

W. C. KELLIHER

NUCLEAR SOURCES

I. A. CARLBERG

**ELECTRON DENSITY** 

G. C. HERRING B. SHIRINZADEH

NEUTRAL DENSITY

P. D. BABB

SAFETY

CPD

A. H. AUSLENDER D. B. RHODES

SCHLIEREN

S. JONES

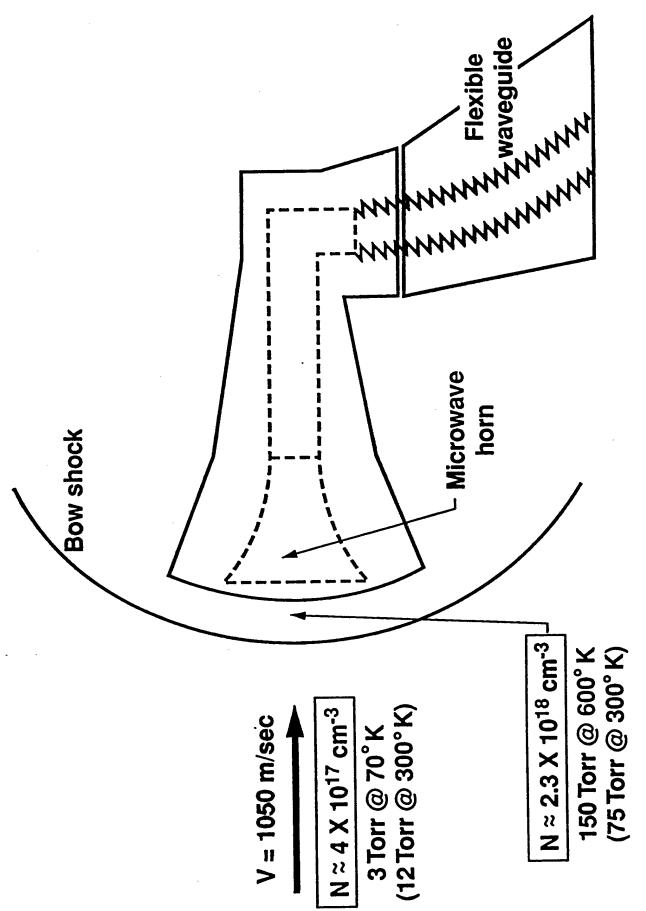
SCHLIEREN

### OBJECTIVES:

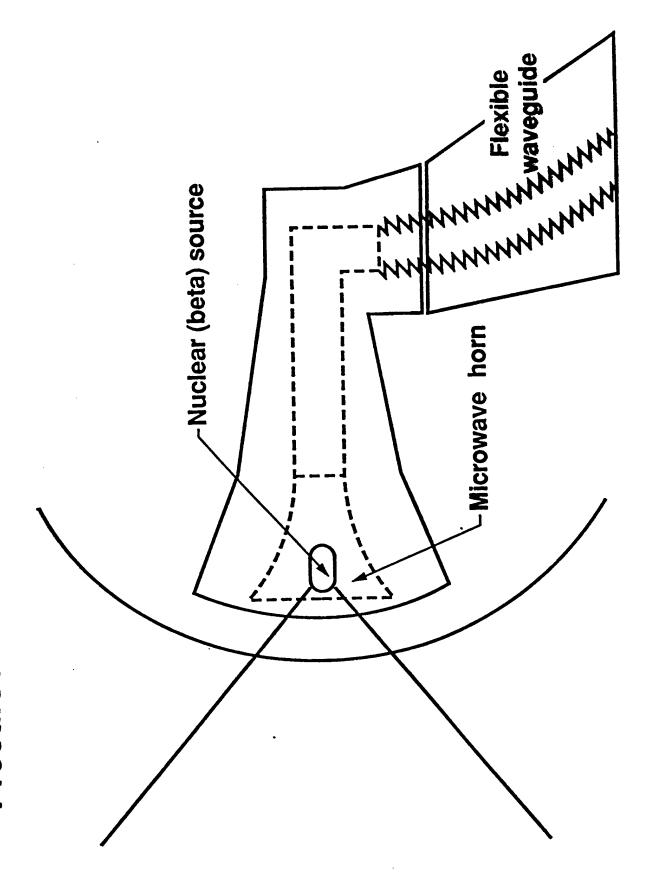
- Experimentally demonstrate a concept for on-board generation of a microwave plasma;
- Develop plasma diagnostic techniques for low density (cold) plasmas;
- Clarify the physics underlying the phenomenon in conjunction with a parallel CFD effort. સં

## APPROACH

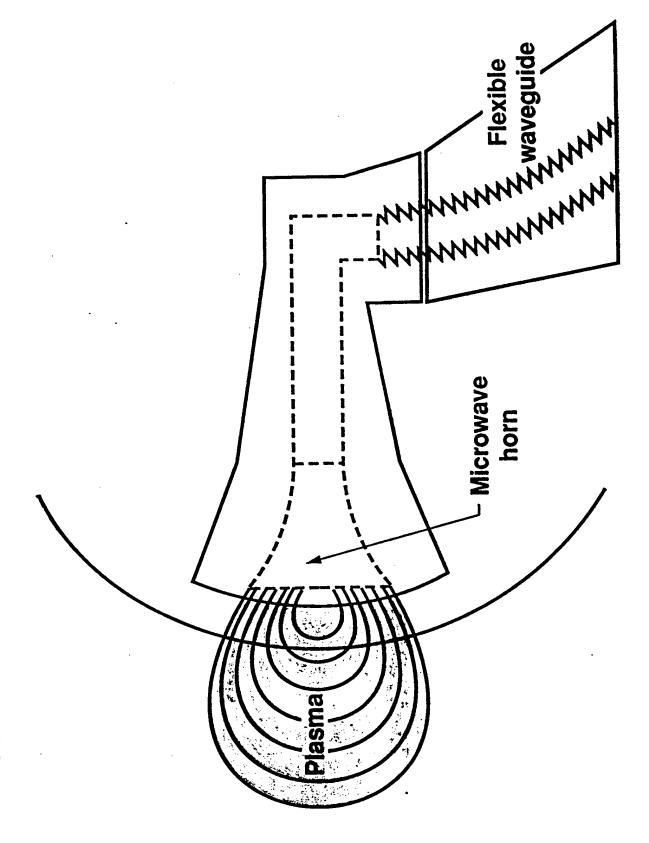
- Design model/microwave horn for Mach 6 facility conditions
- Measure the forces on the model (plasma on/off)
- Characterize the plasma flow field (shock standoff and shape, electron density and temperature, neutral density profile)
- Investigate both cw and pulsed microwave power amplifiers as plasma generators



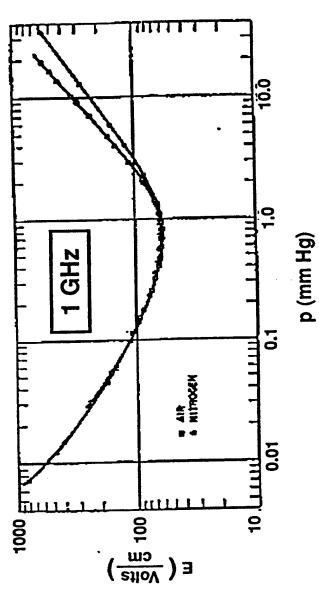
# "Precursor" Microwave Plasma at Mach 6



"Precursor" Microwave Plasma at Mach 6

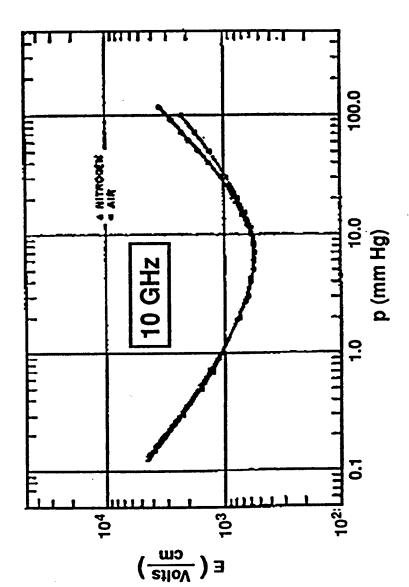


# Microwave Breakdown in Air, O, and N



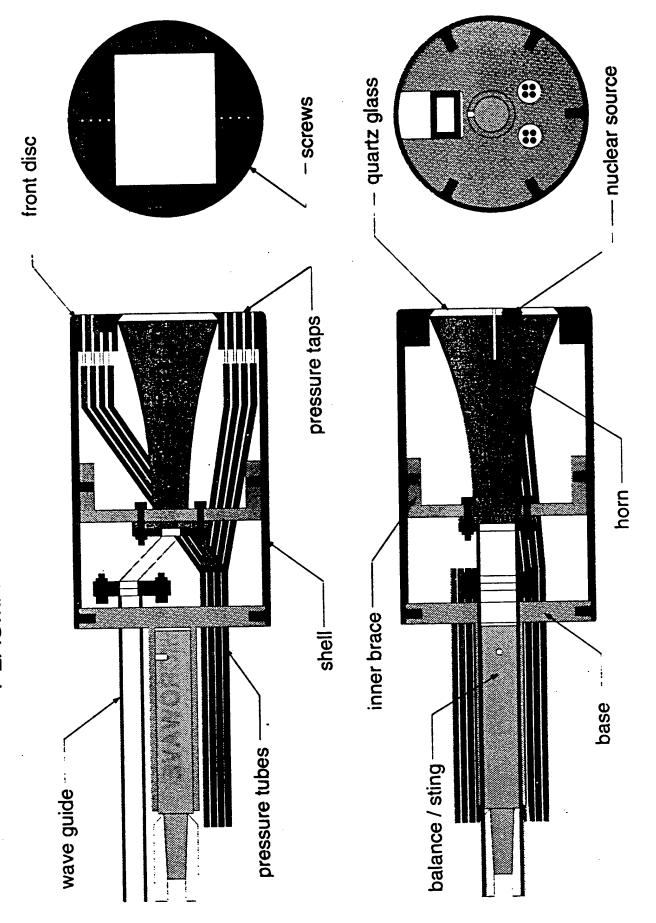
Cw breakdown fields for air and nitrogen at a frequency of 994 Mc/sec. (Characteristic diffusion length A = 2.65 cm)
A. D. MacDonald et. al. Phys. Rev. 130, 1841 (1963)

# Microwave Breakdown in Air, O, and N



Cw breakdown fields for air and nitrogen at a frequency of 9.4 kMc/sec. (Characteristic diffusion length A = 0.22 cm) A. D. MacDonald et. al. Phys. Rev. 130, 1841 (1963)

# PLASMA DRAG REDUCTION MODEL



### DIAGNOSTICS

## INITIAL ENTRY

- PULSED, DIGITAL SCHLIEREN
- GATED, CCD CAMERA
- OPTICAL MULTICHANNEL ANALYZER (200-900 NM)

## FUTURE ENTRIES

- DESCRIMER LASER (NEUTRAL PROFILE)
- LASER/MICROWAVE INTERFEROMETRY

(ELECTRON DENSITY)

### DIAGNOSTICS

## INITIAL ENTRY

- PULSED, DIGITAL SCHLIEREN
- GATED, CCD CAMERA
- OPTICAL MULTICHANNEL ANALYZER (200-900 NM)

## FUTURE ENTRIES

- O EXCIMER LASER (NEUTRAL PROFILE)
- LASER/MICROWAVE INTERFEROMETRY

(ELECTRON DENSITY)

# SCHEDULE/MICROWAVE POWER

SCHEDULE-MACH 6	POWE	POWER AMPLIFIERS (AVAILABILITY)	MILABILITY)
INITIAL ENTRY ~AUG 97	O CM * * *	200 W, 8-18 GHz	(AVAILABLE)
	o • * * •	500 W, 8-18 GHz	(POSSIBLE LOANER)
•	°	2 kw @ 14 GHz	(COMMERCIAL
2ND ENTRYFY98	• * *	10 kw @ 18 GHz	(ننننن)
	* PULSED	) 26 L., DEAK Y.RAND	
	* * *	(8.2-12.4 GHZ) 5% DUTY 1.3 kw AVG.	(POSSIBLE LOANER)
	· * * * ÷	100 kw PEAK, X-BAND (8.2-12.4 GHz)	(POSSIBLE LOANER)
	• * * * *	100 kw PEAK, KU-BAND(POSSIBLE (12.4-18.0 GHz) LOANER) 3 MICROSEC PULSE 100 Hz	O(POSSIBLE LOANER)

### CONCERNS

- SUFFICIENT FIELD STRENGTH FOR BREAKDOWN 0
- (~700 V/CM @ 10-15 TORR)
- PLASMA EXTENT SUFFICIENT TO ATTAIN "PRECURSOR" STATUS
- ELECTRON DENSITY AND TEMPERATURE ADEQUATE TO BRING ABOUT SHOCK MODIFICATION

## SOLUTION

# POWER MORE

## Program Overview

# Shock Wave Dynamics in Weakly Ionized Plasmas

Laboratory for Modern Fluid Physics, Florida A&M University (FAMU), Tallahassee, FL

Prof. J. A. Johnson III, Distinguished Prof. of Science and Engineering Mr. Kester Thompson, Graduate Student, Mechanical Engineering Dr. Richard Appartaim, Research Associate in Physics

# Overall FAMU Purpose

To determine the roles which turbulence and/or nonequilibrium effects in weakly ionized gases play in shock wave transport dynamics through:

bulence and/or nonequilibrium plasmas in the low supersonic and hypercomprehensive optical diagnostics of the interactions of shock waves with tursonic regimes;

(b) rigorous analyses of the associated physics, including quantumechanical as well as classical phenomena;

(c) explorations of potential modalities for the implementation of plasma drag reduction of operational aircraft.

# Recent FAMU Achievements

- Evidence of shock wave strength reduction from a turbulence manipulated nonequilibrium flow in a pressure ruptured shock tube;
- Plasma Facility where a Mach 2 shock wave moves from a plasma free region Preliminary evidence of shock wave acceleration in our new Supersonic Shocked into one with a weak plasma;
- -> Preliminary evidence from our Hypersonic Arc Driven Shock Tube of highly localized energy transfer from small scale turbulent nonequilibrium fluctuations into large scale flow of the sort which can weaken the strength of a resident
- Preliminary experimentally testable explanations of the influence of turbulence and/or nonequilibrium effects on standard macroscopic transport quantities

# Specific Immediate FAMU Plans

- variety of manipulations in the shock wave-plasma interaction, including the -> Modifications of our current Supersonic Shocked Plasma Facility to afford a wider introduction of seed molecules and microwave probes;
- System-specific modelling of the plasma and atomic processes so as to determine the underlying physics along with a full range of test modalities, including those relevant to ballistic ranges, flight, and other configurations different from our
- The implementation of a new Turbulent Stark Velocimetry as a program of developement of relevant portable diagnostics suitable for possible near term introduction on operational airframe platforms.

### AERODYNAMIC APPLICATIONS OF WEAKLY IONIZED PLASMAS

R. Miles, S. Macheret, S.H. Lam, P. Efthimion, L Martinelli Princeton University

Drag Redu	action
Plasma Ra	amparts
Flow Con	trol
-	By Localized Energy Addition
-	By J x B forces
Control ar	nd Intiation of Chemical Processes
Power Ext	traction
-	MHD in an engine inlet (AJAX)
-	MHD in ionized flow
Hyperson	ic Wind Tunnel Drivers
-	By Energy Addition through microwaves
- -	By MHD acceleration
	Plasma Ra Flow Cont  - Control ar  Power Ext

Suppression of shock strength and sonic boom

### SUSTAINING A PLASMA IN HIGH SPEED FLOW

- Important for Drag reduction, Plasma Ramparts, Flow Control, Shock Suppression, MHD, and Combustion Initiation and Control
- Discharge may be blown out
- Thermal (equilibrium) plasma will need to be reinitiated a thermal plasma cannot propagate at supersonic speed
  - Nonequilibrium plasma will require high electric field and high power
- A filamentary plasma may serve the purpose and will require less power (a small portion of the volume is ionized)
- Filaments may be guided by laser or electron beams
- A high power microwave may be the preferred source.

### SUSTAINING MICROWAVE DRIVEN PLASMAS IN ATMOSPHERIC PRESSURE AIR

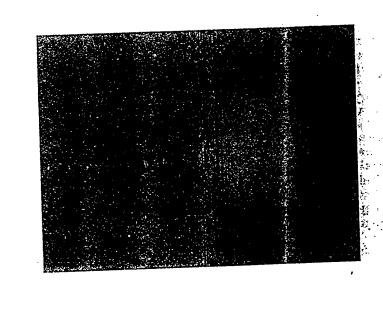
### Thermal Regime

- Requires  $T_{min} > 4000K$
- Needs relatively low microwave power (kilowatts/cm<sup>2</sup>) the power offsets the thermal losses
- Long lifetime (cooling time)

### Nonequilibrium Regime

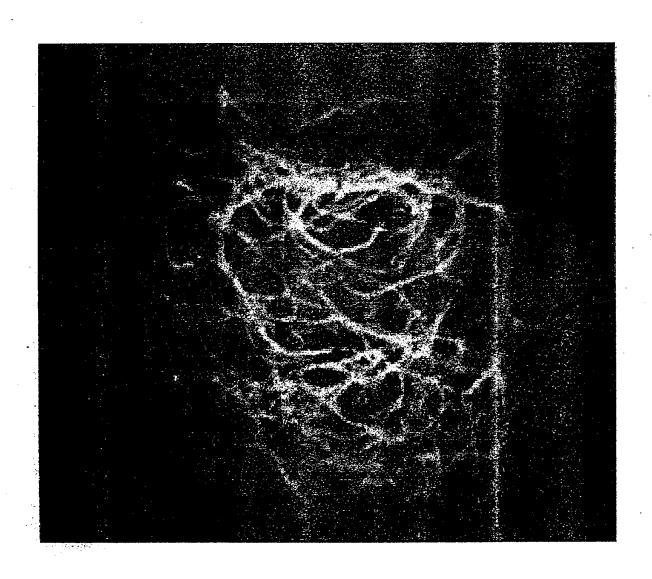
- Requires high power microwaves to overcome the electron recombination and attachment rates
- Diffuse plasma (low pressure)
  - Low temperature neutral species
- Filamentary discharge (high pressure)
  - High temperature localized streamers



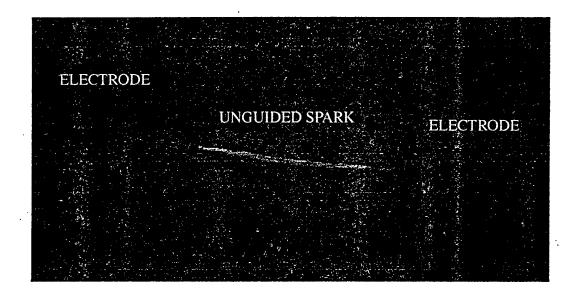


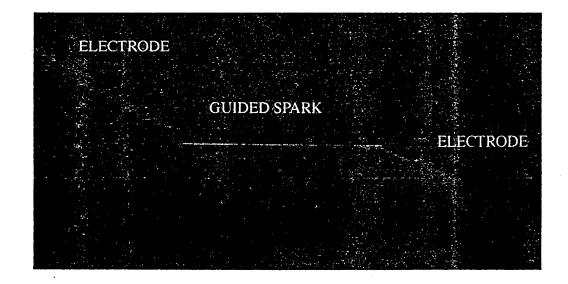
### FILAMENTATION OF ATMOSPHERIC MICROWAVE DRIVEN PLASMA Grachev, Esakov, Mishin and Khodataev

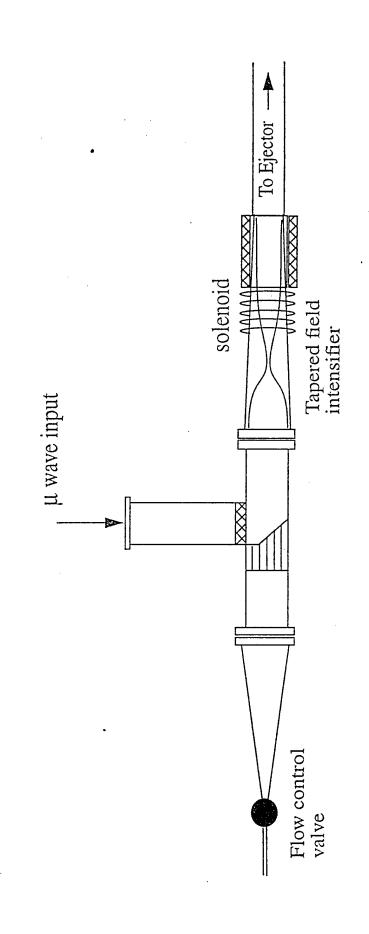
Moscow RadioTechnical Institute



### LASER GUIDED ARC FORMATION







### DRAG REDUCTION Experimental Observations

Shocks Accelerate Upon Entry Into Plasmas From Neutral Gas

Dramatic Changes In Structure:

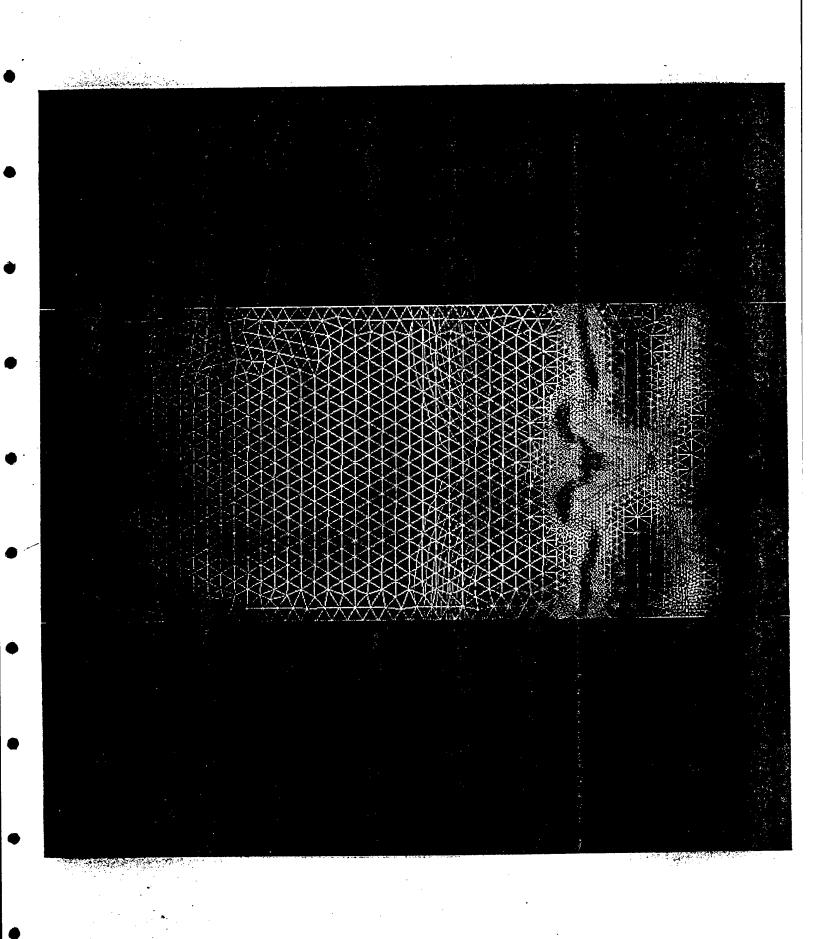
- Shock Front Broadens
- Amplitude Decreases
- Shock Typically Splits Into Two or Three

Effect Persists for Quite a Long Time (up to 1 - 10 msec)

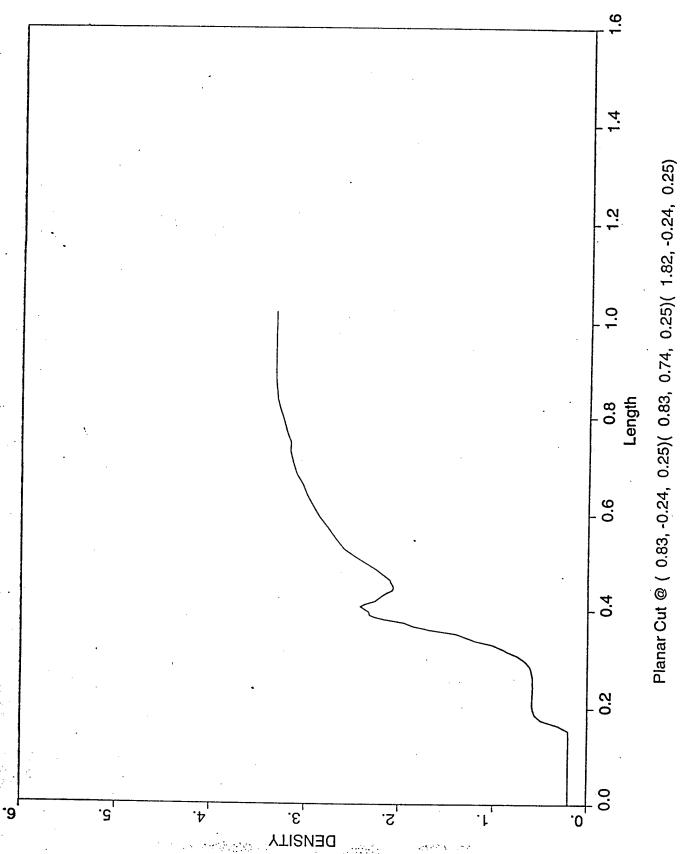
Observations Were Made In Various Discharges (Longitudinal And Transverse), In Various Gases (Air, Argon, Hydrogen, Helium, Etc.) Using Various Diagnostics.

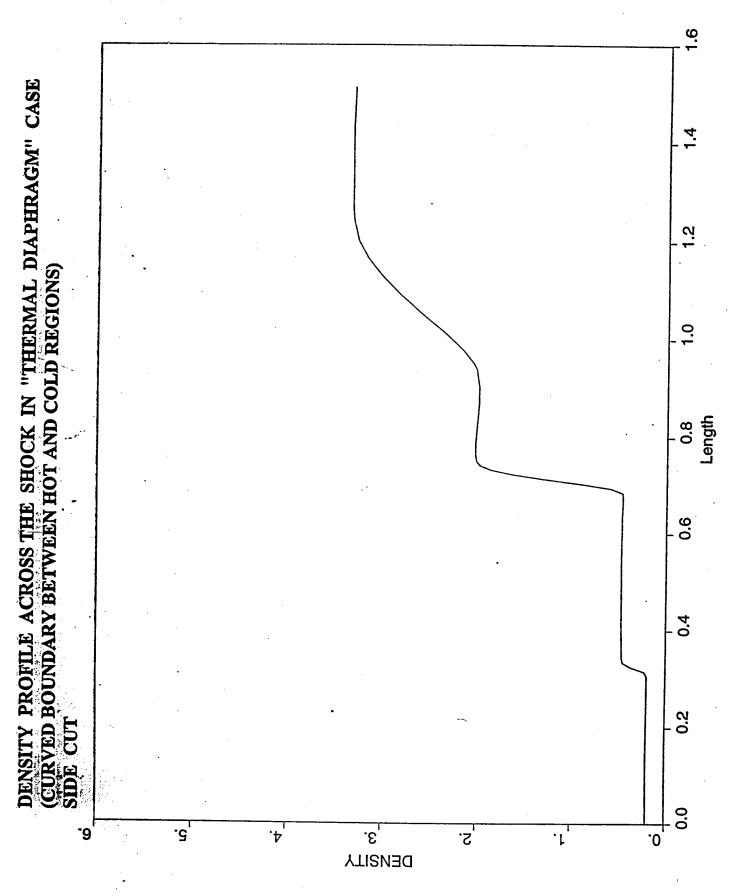
Ballistic Range Experiments Seem to Imply a Change in the Effective Speed of Sound, and Show Decrease in Supersonic Drag.

Thermal diaphragm Density Contours

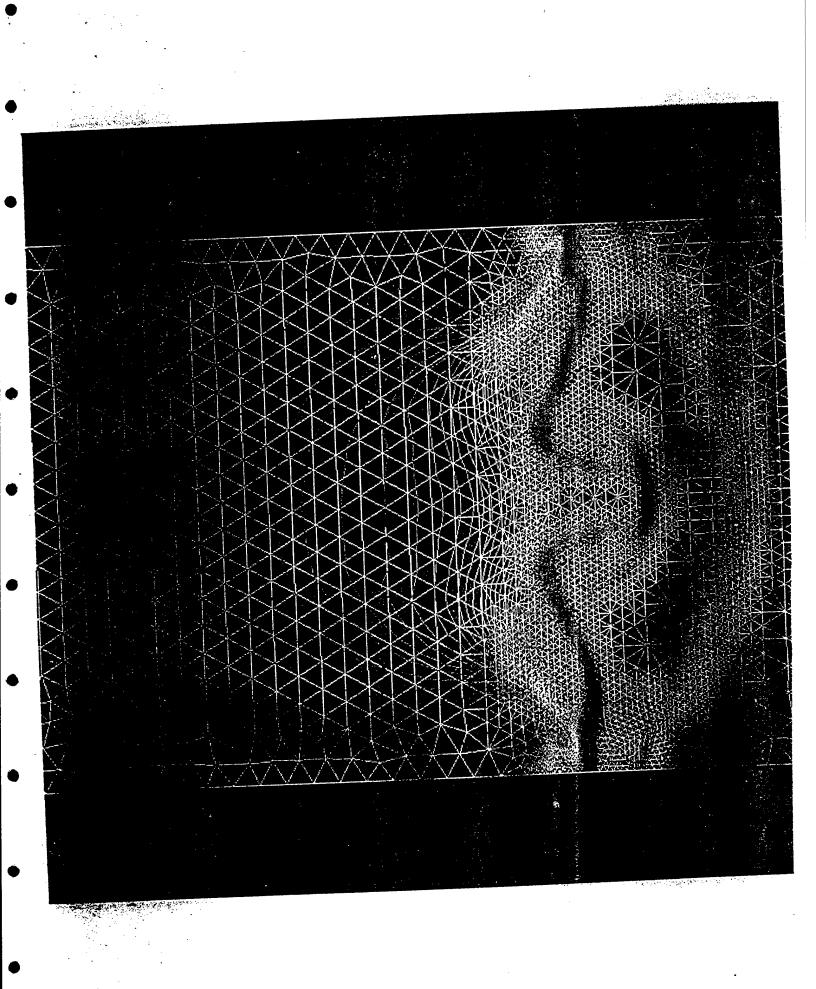


DENSITY PROFILE ACROSS THE SHOCK IN "THERMAL DIAPHRAGM" CASE (CURVED BOUNDARY BETWEEN HOT AND COLD REGIONS)
CUT ALONG THE CENTER LINE





Planar Cut @ (1.01, -0.28, 0.25)(1.01, 1.26, 0.25)(2.55, -0.28, 0.25)



### **EXPERIMENTAL CONCERNS**

### Temperature

In all the experiments, the temperature of the neutral gas has not been directly measured.

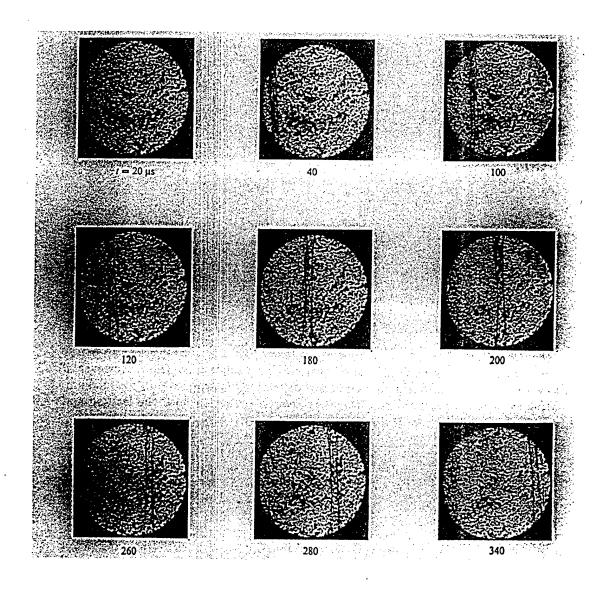
### Temperature Profile

- A transverse temperature profile or a curved thermal boundary will lead to complex shock structure. This may occur as the shock passes through the hot cathode or anode fall regions of the discharge. (Well away from the centerline of the experiment)
- Models indicate the apparent shock splitting and the density rise echo experimental observations

### Nonuniform Temperature Field

Shock splitting has been seen in turbulent mixtures of gases. If the plasma has hot and cold regions, a similar shock break-up may occur.

### M = 1.03 SHOCK PROPAGATION THROUGH HE + R 12 TURBULENT MIXTURE Hesselink and Sturtevant



### **CONCLUSIONS ON DRAG REDUCTION**

- All the experimental phenomena we examined are consistent with thermal gradient effects
- Ballistic range data needs to be studied in more detail
- Accurate temperature and density measurements need to be made
- There may be some effects of thermal gradients, unsteady phenomena, vorticity, and random or flickering heat addition.

### PRINCETON PROGRAM

Development of new diagnostics for temperature and density imaging

### New World Vistas

- Sustaining microwave driven plasmas in a Mach 3 flow
- Plasma effects on the bow shock in a Mach 3 flow.
- Study of basic mechanisms of acoustic wave interactions and shock dynamics in stationary plasmas

### Plasma Ramparts

- Experimental studies of the control of plasma filamentation
- Kinetic model development for pulsed ionized air plasmas
- Modeling nonequilibrium molecular processes
- High power microwave driven discharge dynamics
- Stabilizing and extending microwave driven plasmas with magnetic fields

### Mariah II (Radiatively Driven Wind Tunnel augmented by MHD)

- Sustaining conductivity in atmospheric pressure air with electron beams
- Acceleration and deceleration of supersonic flows in MHD channels
- Energy coupling into high pressure air
- MHD acceleration with filamentary discharges

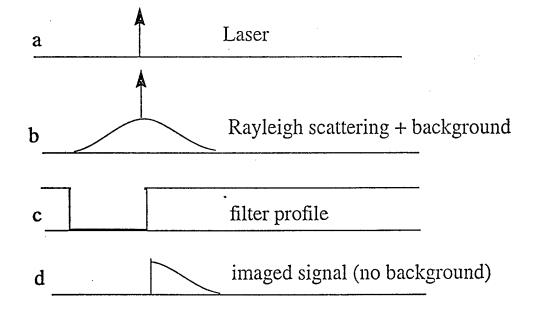
### PLASMA TEMPERATURE MEASUREMENT BY FILTERED RAYLEIGH SCATTERING

### Rayleigh Scattering

- Total Scattering is Proportional to Density
- Linewidth is proportional to  $\sqrt{T}$
- Signal is weak
- Background scattering is at nearly the same frequency

### Filtered Rayleigh Scattering

- Eliminates Background Scattering
- Permits Measurement of Linewidth



### FILTERED RAYLEIGH SCATTERING IMPLEMENTATION

$\sim$			
C,	$\sim$	111	00
L)	u	uі	ce

- Tunable Ultraviolet, Injection Locked Laser
- Ti:sapphire with "Ramp and Lock" Technology (Schwartz Electro-Optics)

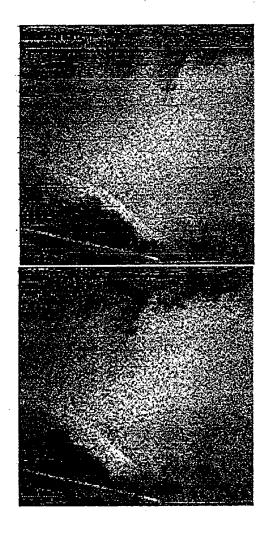
### Filter

- Atomic Mercury Vapor
- 2" Diameter Cell Held at 40°C with a hot water bath (vapor pressure 1 Torr)

### Camera

- UV Sensitive, Intensified CCD (Princeton Instruments)

### SEQUENTIAL RAYLEIGH IMAGES OF MACH 2.5 SHOCKWAVE / BOUNDARY LAYER INTERACTION AT A 14° WEDGE



Framing rate is 500,000 images per second

### Mariah II

No wind tu	nnel can at present be run to accurately
simulate fli	ght conditiona at higher than Mach 8
-	240K, (120,000 ft) requires 2800K, 8 atm in plenum
-	NO contamination
-	Low static T or low static P (enthalpy
	too low or entropy too high)
-	Short time operation

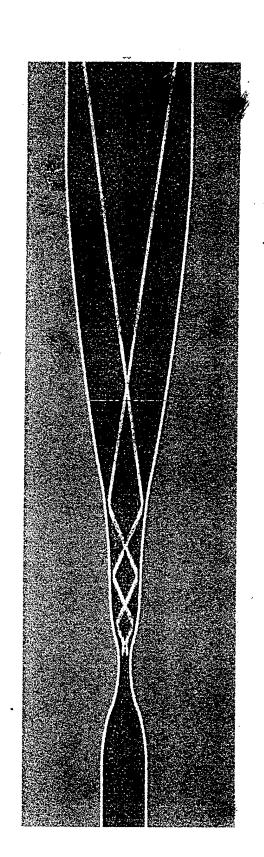
Radiatively Driven concept adds energy downstream of the throat in the supersonic section

- Static temperature stays low
- Low temperature but high pressure in the plenum
- Concept is driven by lasers or electron beams
- Demonstrated with 10KW laser in December at Wright Labs

MHD section is to be added to further accelerate the flow after the Radiative section

- Reduces the front end pressure requirement
- Extends the envelop of the tunnel
- Requires electron beam sustained conductivity
- Must operate at close to room temperature and at pressures on the order of .1 atm.

# Energy Addition by Lasers



RDHWT Review April 23 - 24,1997

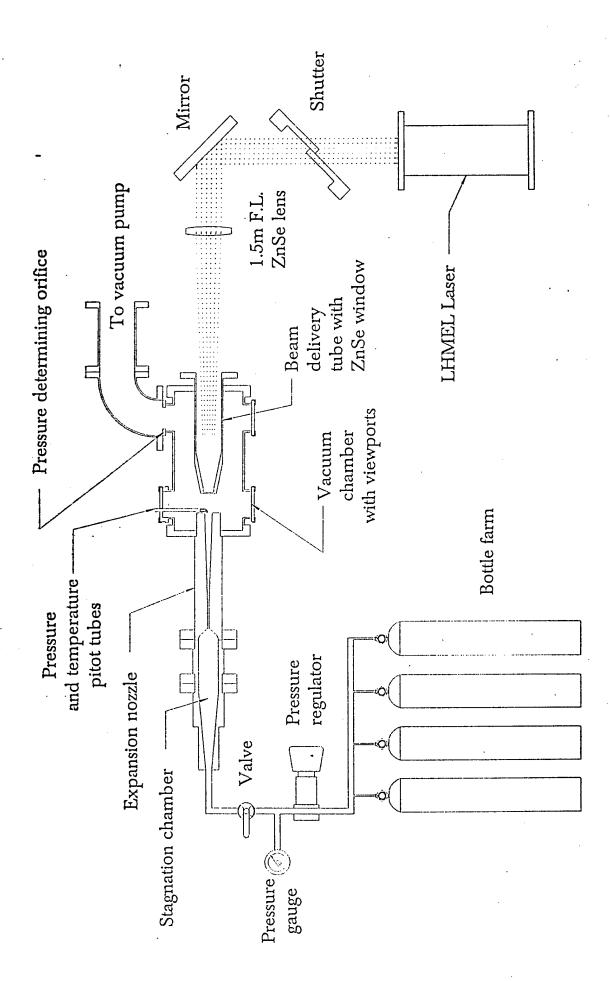
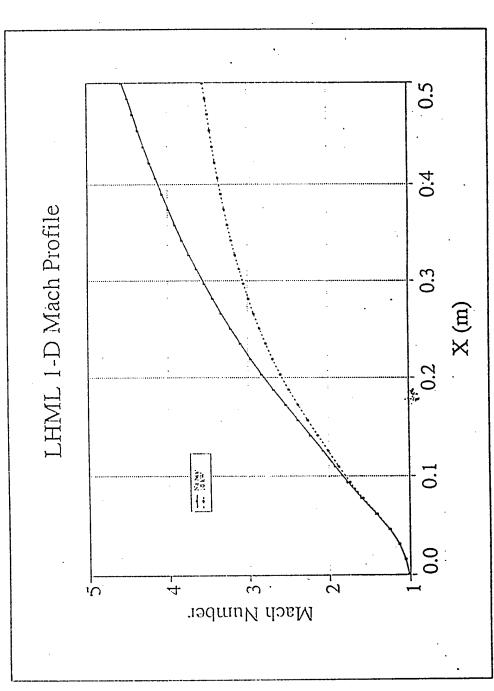


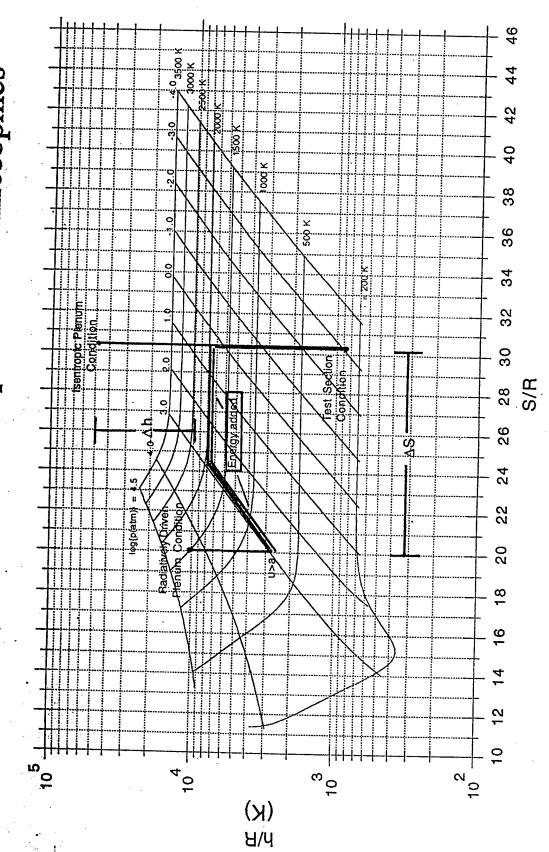
Figure 1. Diagram of 10 kw laser energy addition experiment

# Energy Addition

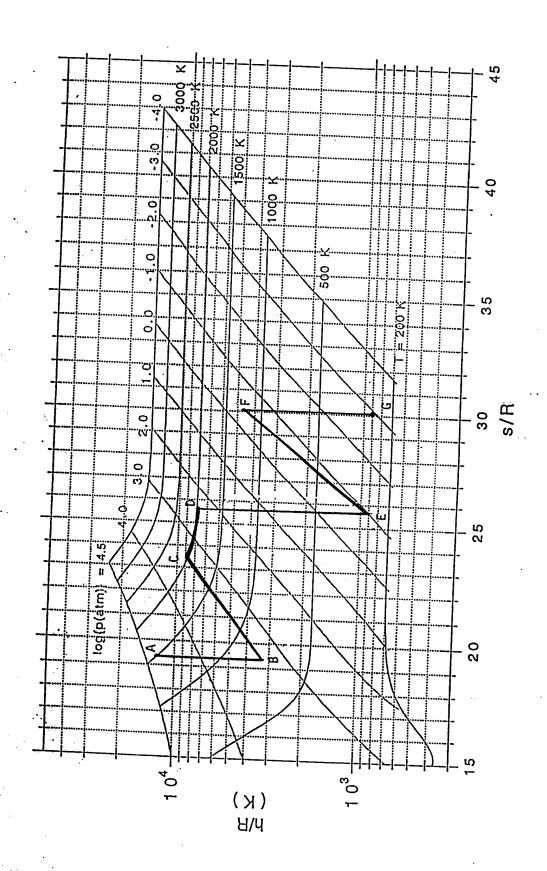


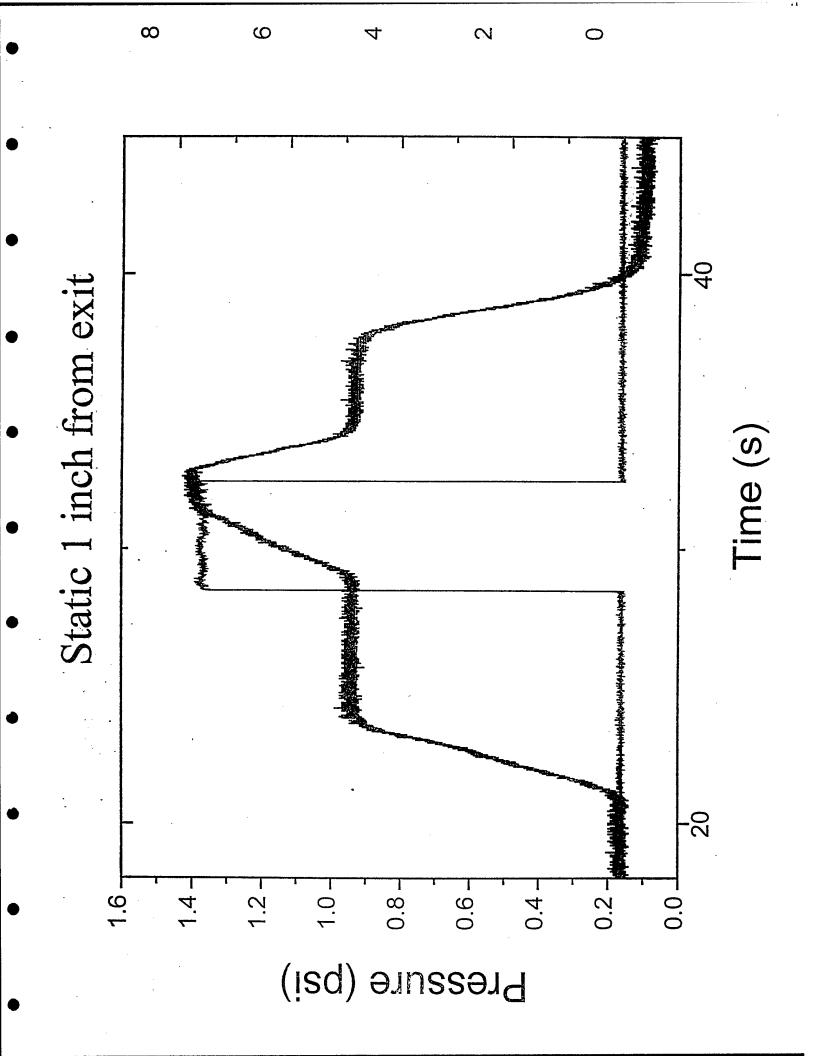


# Thermodynamic Comparison of Philosophies



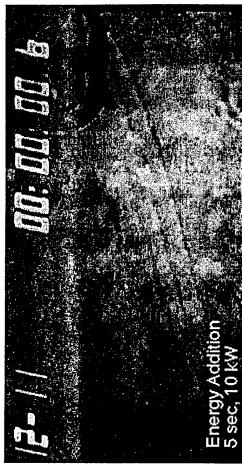
Energy equal to the energy deficit between the two plenum conditions is added along the highlighted path which is determined by the tunnel profile. An effective temperature,  $\Delta h/\Delta s$ , indicates the mean temperature at which the enthalpy must be coupled. Note that real gas effects are significant in the plenum region so that enthalpy is a function of pressure.





## Flow Around Probe



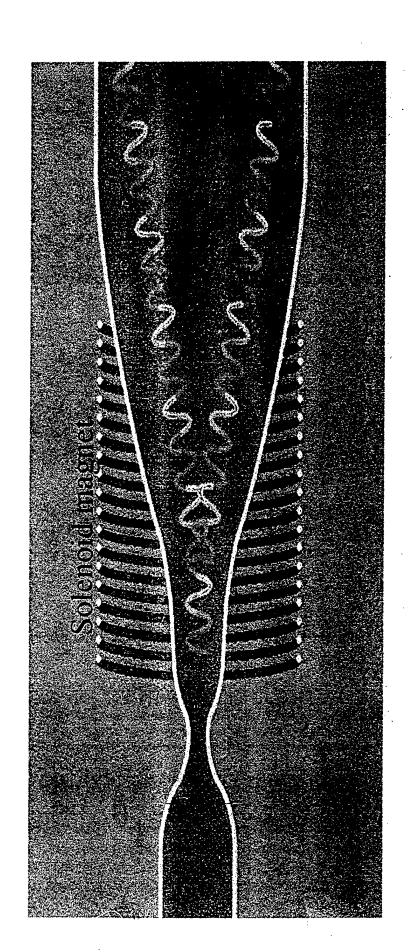


Laser Off M = 4.3

Laser On M = 3.9

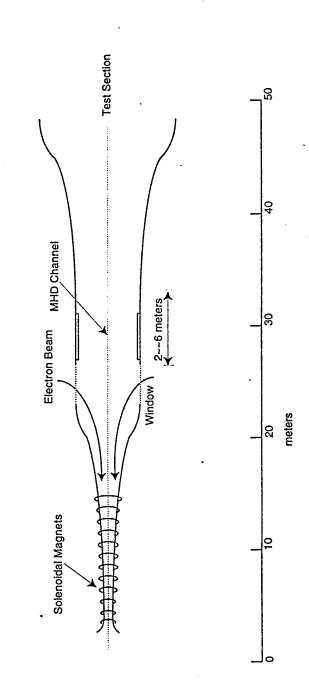
Results verified by Pitot Measurements

## Energy Addition by Electron Beams



RDHWT Review April 23 - 24, 1997

Hybrid Hypersonic Wind Tunnel with E-beam Heating and MHD Acceleration Mach 14, 3.0-m Exit Diameter



### Thermodynamic limit of RDHWT:

$$\Delta h = T_a \Delta s$$

 $T_a$  can't be extremely high (erosion, chemistry); minimum s is defined by incompressibility; maximum s is defined by test section requirements.

### THERMODYNAMIC ADVANTAGE OF MHD

Total enthalpy augmentation:

$$\Delta h_t = \frac{K}{K - 1} T \Delta s$$

where  $K \equiv E/(uB) = \text{(Energy added)/(Push work)}$ 

The best thermodynamically:

when  $K\rightarrow 1$ ,  $\Delta h_t$  can be large even for small  $T\cdot \Delta s$  (non-entropy-generating energy addition).

However, when  $K\rightarrow 1$ ,  $j=\sigma \cdot (E-uB)\rightarrow 0$ , and to add

$$\Delta h_t = \sigma K(K-1) u B^2 L/\rho ,$$

very large conductivity,  $\sigma$ , and/or length, L, would be required

### AJAX

### Proposed by Russians in 1990 (Vladimir Freistadt State Hypersonic Systems Scientific Research Enterprise St. Petersburg)

MHD converter in the inlet connected to MHD accelerator in the nozzle to by-pass free stream kinetic energy and reduce the entropy rise in the inlet.

- Reduces the flow to subsonic in the combustor
- MHD conditions almost the same as Mariah II
- Requires some method to sustain conductivity

Reduction in vehicle drag by cold plasma injection at the nose

Increase of combustion volume and efficiency within the engine by plasma injection or injection of materials ahead of the fuel injectors

Reforming of kerosene and water into hydrogen and CO for fuel.

Computational Hypersonics Initiative in Air Force Research Laboratory J. S. Shang
Air Vehicle Directorate
Air Force Research Laboratory
Wright-Patterson Air Force Base, Ohio 45433

### Objective

- Rekindle a multidisciplinary computational modeling and simulation research to support the USAF New World Vista Vision.
- Develop an enabling critical simulation technology for aerospace vehicle in hypersonic flight regime.
- Research the potential of electromagnetics/shock interaction as a new flowfield control mechanism.

# Scientific "Findings" in Plasma/Shock Interaction

- Appearance of a shock precursor and increase standoff distance of bow shock wave in weakly ionized gas.
- Shock propagation velocity increases and shock front disperses in plasma medium.
- Intermingled reflected compression and rarefaction waves propagation in inhomogeneous plasma media.
- Aerodynamic drag and heat transfer to solid surface are modified by weakly ionized gas.
- Magnetic field suppresses laminar-turbulent transition bypass.

## Macroscopic Conservation Equations

$$\frac{\partial \rho \alpha_{i}}{\partial t} + \nabla \cdot (\rho \alpha_{i} \bar{u} + \rho \alpha_{i} \bar{u}_{i}) = \dot{r}_{i}$$

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \bar{u}) = 0$$

$$\frac{\partial \rho \bar{u}}{\partial t} + \nabla \cdot (\rho \bar{u} \bar{u} - \bar{\tau}) = \rho \sum_{i} \bar{f}_{i}$$

$$\frac{\partial \rho \bar{u}}{\partial t} + \nabla \cdot (\rho e \bar{u} + \bar{u} \cdot \bar{\tau} - k \nabla T + \rho \sum_{i} \alpha_{i} h_{i} \bar{u}_{i} + \dot{q}_{r}) + \sum_{i} \dot{r}_{i} \Delta h_{i}^{o}$$

$$= \rho \sum_{i} \alpha_{i} \bar{f}_{i} \cdot (\bar{u} + \bar{u}_{i})$$

In numerical simulations of hypersonic flows, this system of conservative equations is usually written in strong conservation form.

$$\frac{\partial U}{\partial t} + \frac{\partial F}{\partial x} + \frac{\partial G}{\partial y} + \frac{\partial H}{\partial Z} = 0$$

### Arrhenius equation

In order to apply the law of mass action, the rate of reactions is assumed to be rate constant is given as  $K_{c,j} = K_{f,j}/K_{b,j} = \Pi(X_i)^{\nu_{i,j}}/\Pi(X_i)^{\nu_{i,j}}$  Only when the gas mixture is in chemical equilibrium, the forward andreverse reactions independent of whether or not the system is in equilibrium. This commonly accepted assumption is consistent with the local equilibrium approach. The are in dynamic balance, and the net rate of change in compostion vanishes.

$$\left(\frac{dX_{i}}{dt}\right)_{j} = \left(\nu_{i,j}^{"} - \nu_{i,j}^{"}\right) K_{f,j} \left[\Pi\left(X_{i}\right)^{\nu_{i,j}} - \frac{1}{K_{c,j}} \Pi\left(X_{i}\right)^{\nu_{i,j}}\right]$$

The so-called rate constant has been experimentally recognized as

$$K_{c,j} = C \exp\left(-\frac{\epsilon_a}{KT}\right)$$

ered to as the Arrhenius activation energy. This equation has been modified This is the well-known Arrhenius equation, and the constant  $\epsilon_a$  is often refto better fit to measurements as

$$K_{c,r} = CT^{\eta} \exp\left(-\frac{\epsilon_a}{KT}\right)$$

## Internal Degree of Excitation of Gas Medium

The partition function of a microscopic particle is fundamentally important in relating atomic/molecular structure, which influence the energy level, and thermodynamic behavior.

$$Z = \sum_{i} g_{i} \exp\left\{-\frac{\epsilon_{i}}{kT}\right\}$$

Usually, the coupling of internal degrees of freedom of gas medium is neglected, this assumption leads to the factorization property of partition functions

$$Z = Z_{trs.}Z_{rot.}Z_{vib.}Z_{el}$$

The energy of different internal degree of excitations is additive, the total internal energy is then found by summing the translational, rotational, vibrational, and electronic modes.

$$E_i = E_t + E_r + E_v + E_e$$

Partition Functions of Internal Degree of Freedom

Translational DOF 
$$Z_{trs} = \left(\frac{2\pi m kT}{h^2}\right)^{\frac{3}{2}}V$$
  
Rotational DOF  $Z_{rot} = \frac{T}{\sigma \theta_r}$   
Vibrational DOF  $Z_{vib} = \frac{1}{1 - \exp\left\{\frac{\theta_r}{T}\right\}}$   
Electronic DOF  $Z_{el} = g_o + \sum_i g_i \exp\left(-\frac{\theta_{e,i}}{T}\right)$ 

# Shortcomings in Computational Hypersonics

- Inadequate description of transport property.
- Unreliable non-equilibrium kinetic models for vibration-vibration and vibration-translation energy transfer.
- Marginal numerical accuracy and low computational efficiency.
- Sparse or non-existent verification data base.

### Mobility of Charged Particles

### Langevin's Formula

$$D = \frac{3}{8} \sqrt{\frac{\pi}{2}} \frac{1}{nS_D} \left( \frac{m+M}{mM} kT \right)^{\frac{1}{2}}$$
$$\frac{u}{E} = \frac{3}{8} \sqrt{\frac{\pi}{2}} \frac{q}{nS_D} \left( \frac{m+M}{mM} \frac{1}{kT} \right)^{\frac{1}{2}}$$

Mobility of Heavy Ions

$$D = \frac{3}{8} \sqrt{\pi} L \left( \frac{m+M}{mM} kT \right)^{\frac{1}{2}}$$

$$\frac{u}{E} = \frac{3}{8} \sqrt{\pi} q L \left( \frac{m+M}{mM} \frac{1}{kT} \right)^{\frac{1}{2}}$$

$$L = \frac{1}{\sqrt{2}nS_d}$$

Mobility of Free Electrons

$$\frac{u_e}{E} = \frac{2}{3} \sqrt{\frac{2}{\pi} \frac{eL_e}{(mkT)^{\frac{1}{2}}}}$$
$$L_e = 4\sqrt{2}L$$

## Understanding and Control of Ionized High-Speed Flows

**AFOSR Workshop** 

Plasma Aerodynamics Studies

V. Krivstov, A. Konchakov, A. Tseskis and V. Velikodnyi N. Malmuth, V. Soloviev, H. Hornung, V. Bytchkov

February 26, 1998



## Other Team Members

- W. Beaulieu, Boeing Aircraft and Missile Systems
- P. Bellan, Caltech
- A. Fedorov, Moscow Institute of Physics and Technology
- I. Goldberg, Rockwell Science Center
- A. Klimov, Moscow Technical Club
- K. Lee, Rockwell Science Center
- S. Leonov, Moscow Technical Club
- D. Ota, Rockwell Science Center
  - S. Palinswamy, Metacomp
- S. Ramakrishnan, Rockwell Science Center



## Plasma Aerodynamics Objectives/Approach

- Program Objectives
- Determine basic physical processes of plasma aerodynamic augmentation
- Develop analytical and computational models of these processes
- Provide links with experiments
- F-15 flight test
- Ground and on-board flight instrumentation
- Plasma generator technology
- Wind tunnel, ballistic range, discharge tube and other ground tests
- coupling with analytical model development, e.g. cross-validations
- design and in epretation of experiments



## Objectives/Approach (cont'd)

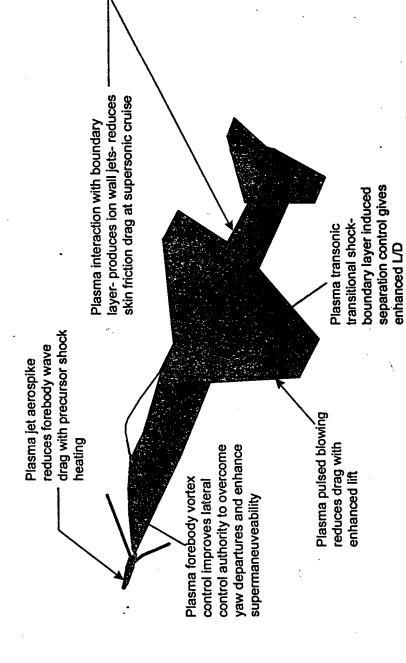
### Approach

- Study importance of key physical mechanisms in flow such as:
- plasma energy addition to flow such as Joule heating
- anomalous dispersion
- ion-acoustic waves
- non-equilibrium phenomena
- second viscosity and other transport parameter modification
- electromagnetic effects such as induced B fields and Lorentz forces
- Use solutions of unit problems such P1-P4 (for which limited experimental databases exist) to isolate these important mechanisms
- Interface with experiments
- Design new experiments
- Compare evolving theoretical models with previous datasets



## **Supercruise Fighter**

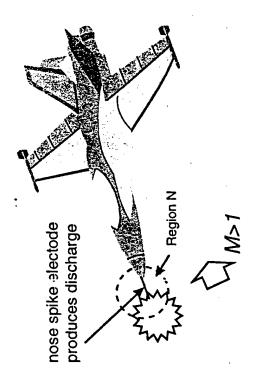
Plasma Aerodynamic Enhancements



# **Noseboom Plasma Flow Control**

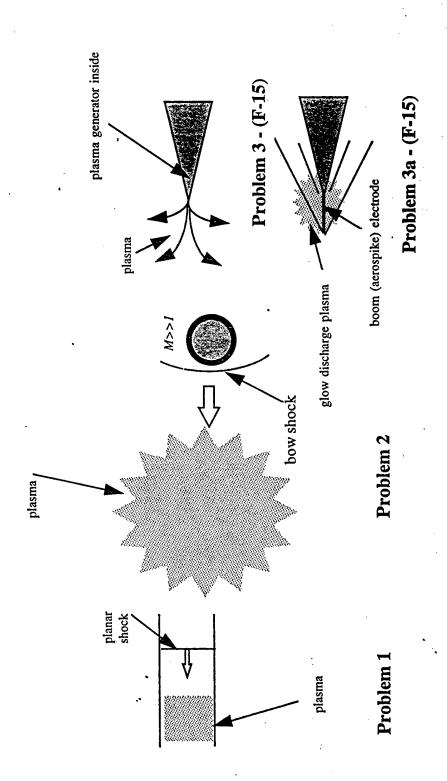
(Problem P4)

- Basic hypotheses:
- dissipative processes in plasma lead to
- Joule heating that reduces pressure drag
  - control of nose separation and nose shocks
- Problem is a useful departure point for treatment of:
- Problem 3: erosive plasma+ RF discharge on F-15
  - 1-D shock structure
- hypersonic applications
   P4 study useful since
   experimental dataset
   available to test models



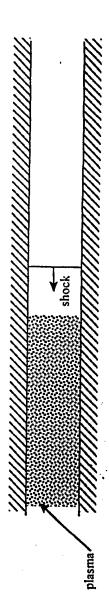
### (1)

### **Problems**



# Plasma Shock Structure

- Modify 1-D Navier Stokes equations to model
- electric field and other plasma terms
- second viscosity
- relaxation
- anomalous dispersion
- Examine scaling of shock thickness with strength from Russian experiments



1-D shock propagating into a plasma



# Perfect Gas Shock-Layer Problem

### Equations of Motion

Continuity

$$\frac{d}{dx}(\rho u) = 0$$

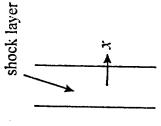
Momentum

$$\rho \, n \, \frac{dn}{dx} + \frac{dp}{dx} = \frac{d}{dx} \left( \mu'' \, \frac{dn}{dx} \right)$$

Energy

$$\rho \, u \frac{dh}{dx} - u \frac{dp}{dx} = \frac{d}{dx} \left( \frac{\mu''}{Pr''} \frac{dh}{dx} \right) + \mu'' \left( \frac{du}{dx} \right)$$

 $\mu'' \approx 2\mu + \lambda$ ,  $\mu = \text{shear viscosity}$ ,  $\lambda = \text{"second" viscosity}$ , Pr'' = Prandtl Number



### Boundary conditions

$$\frac{dn}{dx}, \frac{dh}{dx} \to 0, \text{ as } x \to \pm \infty$$

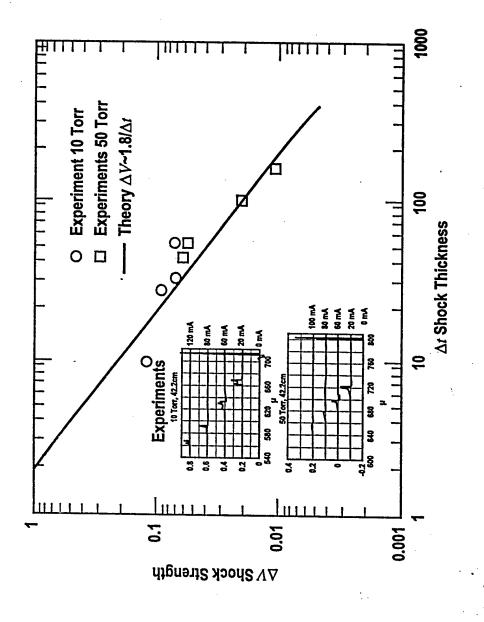
Solution for Shock Thickness

$$\delta = \frac{32\left(\gamma + (\gamma - 1)\left(\frac{1}{P_r''} - 1\right)\right)\nu'}{3(\gamma + 1)\left(\nu'_f - \nu'_i\right)}$$

 $\delta = \text{viscous shock layer thickness}$ 

 $V_f - V_t \equiv \text{shock strength}$ 

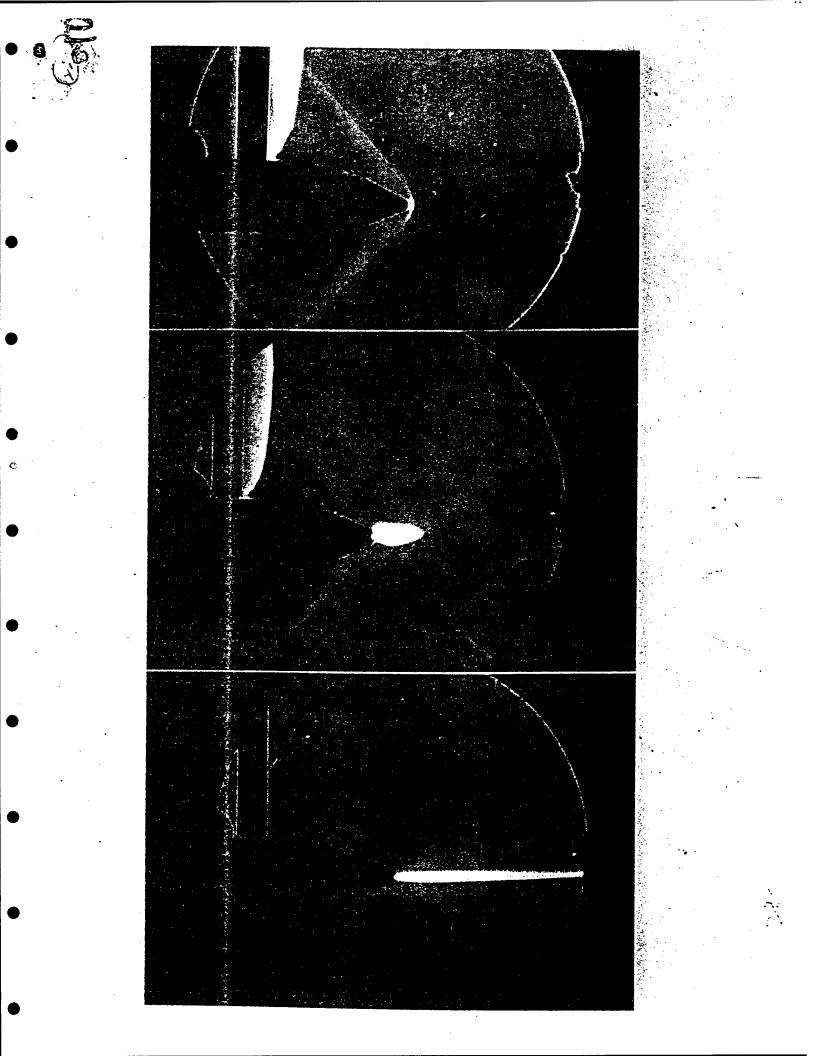
 $\gamma = \text{specific heat ratio}$ 







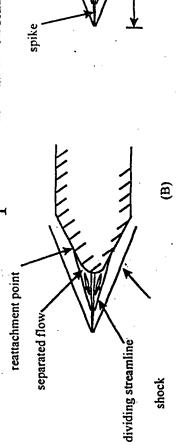
Science Center





# Drag Reduction Mechanisms

- Plasma jet aerospike extension
- aerospike reduces drag by making a shallow oblique shock out of blunt nose detached almost normal shock
- creates low pressure separation in front of blunt nose to give a net suction thrust increment
- Transverse shock due to plasma heating leading to rarefaction of separation region
- Interaction of separation and transition over the aerospike

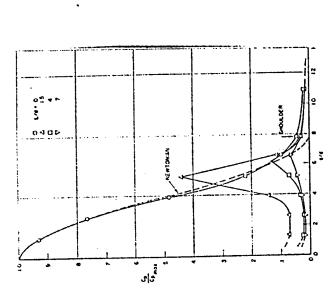


4/97

Flow Configurations



# Aerospike Effect on Pressures



Bogdanoff and Vas JAS 1939

- Spike produces peak in pressures near reattachment point
  - •Peak attenuates with increasing spike length reducing drag
- Needs to be traded against high heat transfer near peak
- •Plasma heating can affect reattachment and therefore pressure peak



Approximate formula based on Newtonian on blunt nose and cone part

$$C_p = 2\left(\sin^2 \varepsilon + \frac{1}{\gamma M_{e}^2}\right) \left(1 - \alpha^2\right) + \frac{P_{\text{plateau}}\alpha^2}{q} - \frac{2}{\gamma M_{e}^2} \left(1 - \left(\frac{r_{hare}}{r_d}\right)^2\right)$$

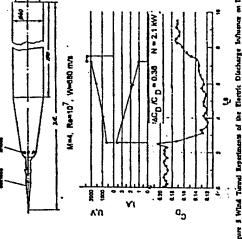
 $P_{\text{plateau}} \equiv \text{pressure in separation region}$ 

$$r_d \equiv \frac{d}{2}$$

$$\alpha \equiv \frac{r_j}{r_j}.$$

 $r_j = \text{radius at juction of spherical nose tip with cone portion}$ 

 $\varepsilon = \text{cone semiapex angle}$ 



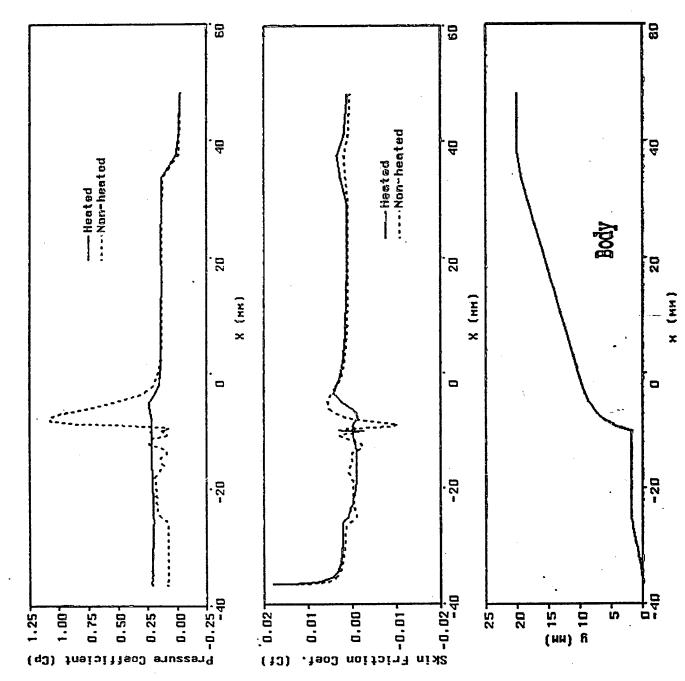
Pigure 5 Wind Turnel Experiments of the Electric Discharge Miner

		A.W. T. C.	
•			u o
vacuum due to plasma	.07	.12	current
norm al shock value			011
plateau pressure=1/2	.216	.19	current
separation zone			
Remarks/assumptions in	Estim ated	Experiment	
		•	

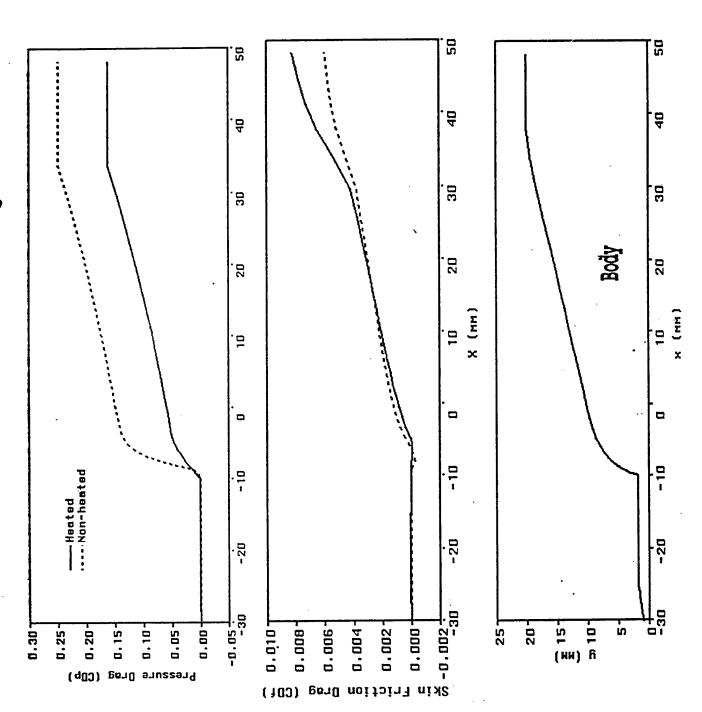
OFF FOR SSURE COLOR PANELS SSE FOR B. 200E SOUR; JUST FOR		
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C

Pressure and Skin Friction Distributions With Plasma Heating



Cumulative Pressure and Skin Friction Drag with Plasma Heating





	Rockwell Science	Russian Experiment
	Center Computation*	
C <sub>D</sub> (Plasma off)	0.254	0.220
C <sub>D</sub> (Plasma on)	on) 0.170	0.180
Δ C <sub>D</sub> / C <sub>D</sub>	0.33	0.18

<sup>\*</sup>Laminar Navier Stokes model with plasma power uniformly distributed over spike electrode surface

- Discrepancies above within experimental errors
- Heat source model may give dominant physics of spike electrode problem
- Computed relative drag changes agree with experimental order of magnitude



- Objectives
- Study competition of jet momentum drag with surface pressure

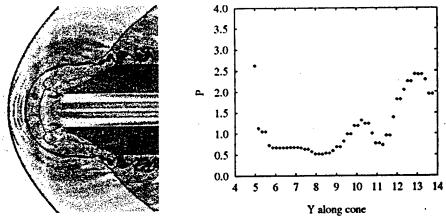
drag

- Study basic physical mechanisms
- Relate to plasma jet effects

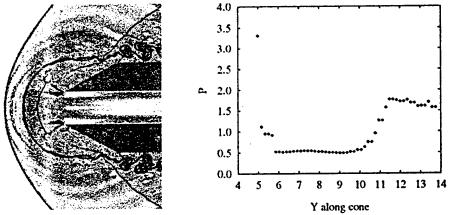




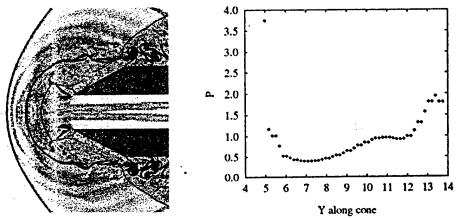




 $p_4/p_{\infty}=15.0,\,C_{D_c}=0.395,\,C_{D_t}=0.462,\,C_D=0.857$ 



 $p_4/p_{\infty}=18.0,\,C_{D_c}=0.342,\,C_{D_t}=0.553,\,C_D=0.895$ 



 $p_4/p_{\infty}=21.0,\,C_{D_c}=0.312,\,C_{D_t}=0.646,\,C_D=0.957$ 

Counterflow jet,  $M_{\infty}=2.0,\,T_4/T_{\infty}=10,\,\gamma=1.4.$ 

## Forebody drag of a cone-cylinder with counterflow jet in supersonic flow

Flow field features

- Small pressure ratios<12, (subsonic jets)</li>
- jet insufficiently powerful to counter freestream, contact surfact is an effective blunt body
- leads to saddle point singularity from which contact interface issues
- jet separation over body causing a low pressure region giving a thrust
- Large pressure ratios >12, (supersonic jets)
- Goes through normal shock prior to impingment with freestream
- Free shear layer stagnates on shoulder, leading to eddies, baroclinic vorticity, multiple secondary shocks and instabilities





## Forebody drag of a cone-cylinder with counterflow jet in supersonic flow

### Conclusions

- Two competing tendencies
- Jet momentum flux- increases drag
- Pressure thrust on forebody-decreases drag
- Drag can be lower thatn the forebody drag of an equivalent sharp cone or cone frustrum
- Minimum drag occurs when the jet to freestream pressure ratio is approximately 11







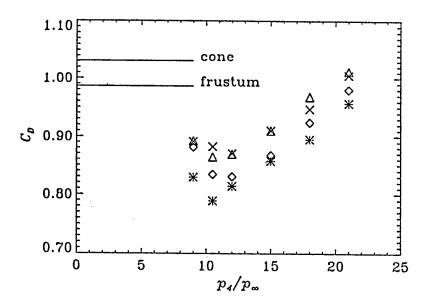


Figure 7: Forebody drag coefficient as a function of  $p_4/p_\infty$  for different values of  $T_4/T_\infty$  as follows: crosses:1, triangles:3, diamonds:6, asterisks:10. The forebody drag coefficients of the sharp cone and the cone frustum are shown as lines for reference.  $M_\infty = 2$ ,  $\gamma = 1.4$ 

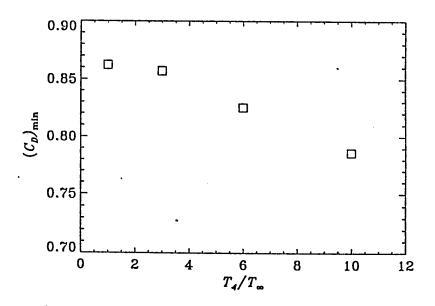


Figure 8: The minimum value of the forebody drag coefficient as a function of  $T_4/T_{\infty}$ .  $M_{\infty}=2, \gamma=1.4$ 

### Propagation of 1-D Shock Waves Through Weakly Ionized Plasmas

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### N.Malmuth Rockwell Science Center, CA, USA

### Main topics of the model

- Hugoniot relations on a shock wave (SW) in a weakly ionized plasma
- Estimations of the energy stored in different excited states for glow discharge plasma
- The existence of high situated metastable states in Ar and N<sub>2</sub>, which serve as
   a 'new ground state' for higher states excitation by electron impact
- Highly excited atomic and/or molecular states store sufficient energy to produce SW acceleration and attenuation
- Inclusion of highly excited atom energy release behind the SW front dramatically improves agreement of theory with experiment for 1-D shock penetrating into a plasma and hypersonic sphere entering a plasma

### Hugoniot relations on a shock wave (SW) in a weakly ionized plasma

A set of gas mass, momentum and energy conservation equations in SW coordinates

$$\begin{split} \frac{\partial \rho}{\partial t} + \frac{\partial (\rho u)}{\partial \xi} &= 0 \;, \\ \frac{\partial (\rho (u+D))}{\partial t} + \frac{\partial}{\partial \xi} (\rho u (u+D) + p) &= \frac{\partial}{\partial \xi} \left[ \frac{4}{3} \mu \frac{\partial u}{\partial \xi} \right] + f_{\xi} \;, \\ \frac{\partial}{\partial t} \left[ \rho \left( h + \frac{(u+D)^{2}}{2} \right) - p \right] + \frac{\partial}{\partial \xi} \left[ \rho u \left( h + \frac{(u+D)^{2}}{2} \right) \right] &= \frac{\partial}{\partial \xi} \left[ \frac{\lambda}{c_{p}} \frac{\partial h}{\partial \xi} \right] + \\ &\quad + \frac{4}{3} \mu \frac{\partial^{2}}{\partial \xi^{2}} \left( \frac{(u+D)^{2}}{2} \right) + f_{\xi} (u+D) + Q_{r} \end{split}$$

$$h = c_{p} T_{a} = \frac{\gamma}{\gamma - 1} \frac{p}{\rho} \;, \end{split}$$

 $\rho$ , p, h are density, pressure and enthalpy of the gas; v is its velocity;

 $\lambda$ ,  $\mu$  are thermal conductivity and dynamic viscosity coefficients;

 $c_p$ ,  $\gamma$  are specific heat at a constant pressure and the ratio of specific heats;

D is the SW velocity;

The  $f_{\xi}$  and  $Q_r$  terms describe the plasma influence on the gas.

### **Hugoniot relations**

$$\begin{split} & \rho_1 u_1 = \rho_0 D, \\ & \rho_1 u_1^2 + p_1 = \rho_0 D^2 (1 - \varepsilon_{u1}) + p_0, \\ & h_1 + \frac{u_1^2}{2} = h_0 (1 + \varepsilon_h) + \frac{D^2}{2} (1 - 2\varepsilon_{u2}), \end{split}$$

where

$$\varepsilon_{u1} = \frac{1}{\rho_0 D^2} \int_{-\infty}^{\infty} f_{\xi} d\xi , \quad \varepsilon_{u2} = -\frac{1}{\rho_0 D^3} \int_{-\infty}^{\infty} f_{\xi} u d\xi , \quad \varepsilon_h = \frac{1}{\rho_0 D h_0} \int_{-\infty}^{\infty} Q_r d\xi$$

• To produce a plasma effect on SW propagation it is necessary  $\varepsilon_{u1}$ ,  $\varepsilon_{u2}$ , or  $\varepsilon_h$  to be of the order of 1.

### The typical cold glow discharge plasma parameters in SW - discharge interaction experiments

gas pressure (gas density)	$p \approx 3 - 30 \text{ Torr } (N \approx 10^{17} - 10^{18} \text{ cm}^{-3})$
gas temperature	T ≈ 300 K
current density	$j \approx 1 - 100 \text{ mA/cm}^2$
electric field strength	E ≈ 100 V/cm
E/N value	$(2-10) \times 10^{-16} \text{ V} \times \text{cm}^2$
discharge specific power	$W \approx 0.1 - 10 \text{ W/cm}^3$
electron temperature	$T_e \approx 1 - 3 \text{ eV}$
electron density	$n_e \approx 10^{10} - 10^{12} \text{ cm}^{-3}$
metastable atom (or molecule) density	$N_{\rm m} \approx 10^{11} - 10^{13} \ {\rm cm}^{-3}$

### The energy stored in different excited states

• freestream gas enthalpy  $h_0=Nc_pT\sim 10^{16}~eV/cm^3$ 

• ionization 
$$n_i E_i \sim 10^{12} \text{ eV/cm}^3$$
,  $\epsilon_h = n_i E_i / N c_p T \sim 10^{-4}$ 

- metastable atoms (or molecules)  $N_m E_m \sim 10^{14} \text{ eV/cm}^3$ ,  $\epsilon_h = N_m E_m / N c_p T \sim 10^{-2}$
- specific discharge energy supply during the time of unit length SW pass  $\epsilon_h = W \times 1 \text{cm/D Nc}_p \text{T} \sim 10^{-2} 10^{-1}$
- the vibrational energy is shown to be unsuitable to explain the SW anomalious propagation effects because of large vibrational-translational relaxation time  $\tau_{VT}\sim 10^{-3}$ s

The scheme of Ar and N<sub>2</sub> electronic excited states

Ar(4s) and  $N_2(A^3\Sigma)$  are the metastable states

### The Ar metastable state quenching and building up

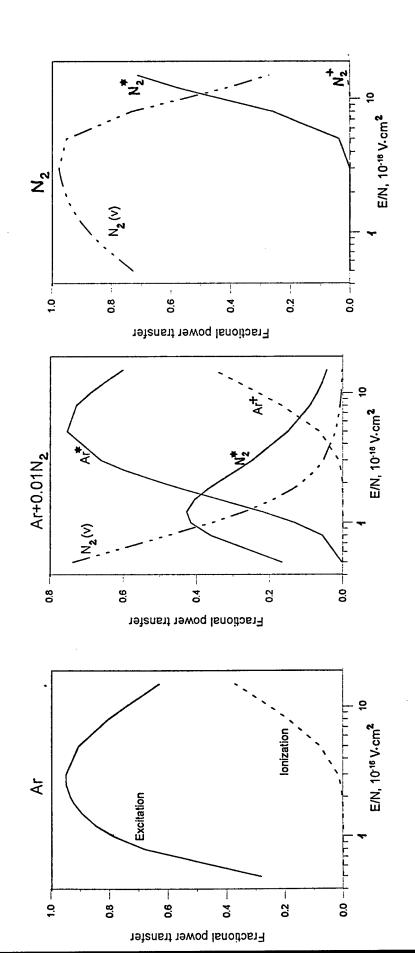
Process	Rate constant	Quenching time for p=10 Torr, n <sub>e</sub> =10 <sup>11</sup> cm <sup>-3</sup>
A (4 ) + 2 A = + A = + A =	$10^{-32} \text{ cm}^6/\text{s}$	and 1% N <sub>2</sub> diluent in Ar
$Ar(4s) + 2Ar \rightarrow Ar_2^* + Ar$	10 cm-/s	0.8 ms
$Ar(4s) + e \rightarrow Ar + e + 11.8ev$	$10^{-8} \text{ cm}^3/\text{s}$	1ms
$Ar(4s) + N_2 \rightarrow Ar + N_2(C, B,)$	$3.6 \times 10^{-11} \text{cm}^3/\text{s}$	0.01ms
$Ar(4s) + Ar(4s) \rightarrow Ar^+ + Ar + e$	$10^{-9} \text{ cm}^3/\text{s}$	$1 \text{ms} \times (10^{12}/\text{n}(4\text{s})[\text{cm}^{-3}])$
$Ar(4p) + Ar \rightarrow Ar(4s) + Ar$	$\sim 10^{-11}$ - $10^{-12}$ cm	$^{3}/s$ 0.3 - 3mcs
$Ar(4p) \rightarrow Ar(4s) + hv$	$3.2 \times 10^7 \text{ s}^{-1}$	0.03mcs

### The $N_2(A^3\Sigma)$ metastable state quenching and building up

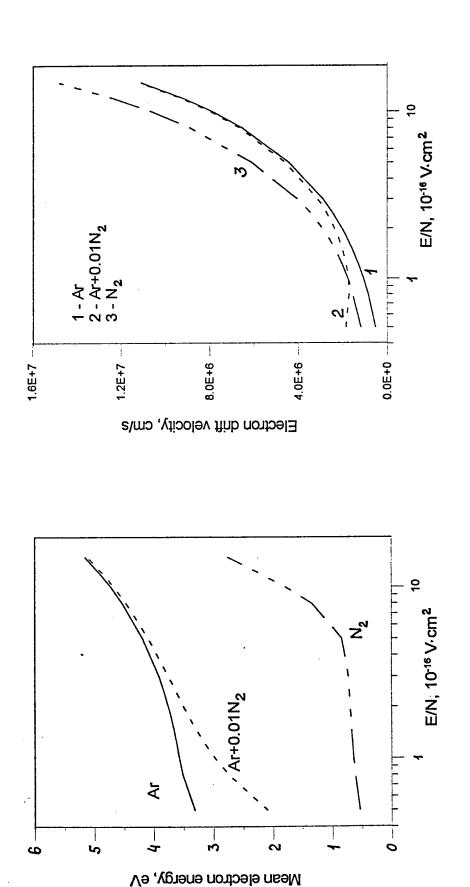
$N_2(A^3\Sigma) + Ar \rightarrow N_2(X) + Ar$	$<4\times10^{-14}$ cm <sup>3</sup> /s	> 0.1ms
$N_2(A^3\Sigma) + N_2(X) \to 2 N_2(X)$	$<4.5\times10^{-17}$ cm <sup>3</sup> /s	>100ms
$N_2(A^3\Sigma) + O_2 \rightarrow N_2(X) + O_2$	$3.6 \times 10^{-12} \text{cm}^3/\text{s}$ (for a	4mcs ir composition)
$N_2(A^3\Sigma) + N_2(X,v) \to N_2(B^3\Pi) + N_2(X)$	$\sim 10^{-10} \text{cm}^3/\text{s}$	
$N_2(A^3\Sigma) + N_2(A^3\Sigma) \rightarrow N_2(B,C,) + N_2(X)$	$10^{-9} \text{cm}^3/\text{s}$ $1 \text{ms} \times (10^{-9} \text{cm}^3/\text{s})$	$10^{12}/n(A)[cm^{-3}]$
$N_2(B^3\Pi) + N_2(X) \to N_2(A^3\Sigma) + N_2(X)$	$2 \times 10^{-11} \text{cm}^3/\text{s}$	0.15mcs
$N_2(B^3\Pi) \rightarrow N_2(A^3\Sigma) + h\nu$	$1.5 \times 10^5 \text{ s}^{-1}$	6.5mcs
$N_2(C^3\Pi) \rightarrow N_2(A,B) + h\nu$	$2.7 \times 10^7 \text{ s}^{-1}$	0.037mcs

## The discharge fractional power input into different excited states for Ar, N<sub>2</sub> and Ar-N<sub>2</sub> mixture

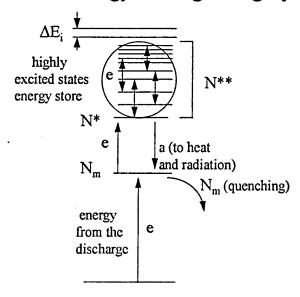
E-is electric field strength, N - is gas number density



The mean electron energy (electron temperature) and electron drift velocity versus  $\rm E/N$  value for Ar,  $\rm Ar+0.01N_2$ and N<sub>2</sub> discharges



The kinetic model of energy storing in highly excited states



The system of balance equations for excited states

$$\frac{\partial N_{m}}{\partial t} = \frac{W\eta}{E_{m}} - N_{m}(k_{p}N_{m} + \frac{1}{\tau_{q}}) - k_{e}n_{e}N_{m} + N^{*}(k_{q}N + A_{R}\theta)$$

$$\frac{\partial N^{*}}{\partial t} = k_{e}n_{e}N_{m} - N^{*}(k_{q}N + A_{R}\theta)$$

$$N^{**} = \sum_{n=n}^{n_{f}} N^{*} \frac{g_{n}}{g_{n}^{*}} \exp(-\frac{E_{n} - E_{n}^{*}}{T_{e}}), \quad \text{for } n > n^{*} \quad k_{e}n_{e} > k_{q}N \frac{\Delta E_{n,n+1}}{T_{e}},$$

$$\Delta E_{n,n+1} \approx \frac{2Ry}{n^{3}}, \quad n^{*} \approx \sqrt[3]{\frac{2Ry}{T_{e}} \frac{k_{q}N}{k_{e}N_{e}}} \approx 4 - 5, \quad E_{i} - E^{*} \approx 0.5 - 1 \text{eV}$$

$$Ry = 13.6 \text{eV} \text{ is the Rydberg constant}$$

W = jE - is the discharge specific power;

 $\eta$ ~1 - is the discharge fractional power input into excitation;

E<sub>m</sub>, E<sub>n</sub> - are the energies of the different states excitation from the ground state;

 $k_p$  - is the metastable atom Penning process rate constant;

 $\tau_q$  - is the metastable state quenching time in other processes;

ke - is the electron excitation rate constant from metastable to N\* states;

 $\mathbf{k}_{q}$  - is the gas quenching rate constant for  $N^{*}$  states;

A<sub>R</sub>- is the radiative decay rate for N<sup>\*</sup> states;

 $\theta$  - is the probability of radiation trapping;

ΔE<sub>i</sub> - is the decrease of ionization potential due to excited atom electron - ion interaction;

For the tube radius R

$$\theta = \frac{1}{3\sqrt{\pi\sigma_{abs}N_{m}R}}$$

For Ar(4p)  $\rightarrow$  Ar(4s) transitions  $\theta \approx 3 \times 10^{-2} (10^{12}/N_m)^{0.5}$  followed by

$$A_R\theta << k_qN$$

The steady state values of  $N_m$  and  $N^*$ :

$$N_m \approx \sqrt{\frac{W\eta}{k_p E_m}} \approx 2.5 \times 10^{13} \sqrt{W[W/cm^3]}, cm^{-3}$$

$$N^* \approx N_m \frac{k_e n_e}{k_q N} \approx 3.5 \times 10^{12} \frac{\sqrt{W[W/cm^3]}}{p[Torr]}, cm^{-3}$$

The equilibrium highly excited hydrogen-like states population

$$n_f \approx \sqrt{\frac{Ry}{\Delta E_i}} \approx \sqrt{\frac{Ry}{e^2 N_i^{\frac{1}{3}}}}$$
 - the upper limit of principle quantum number for hydrogen-like states;

 $n_f \approx 100 \text{ for N}_i \approx 10^{11} \text{cm}^{-3}$ 

$$N^{**} \approx N^* \frac{2n_f^3}{3g^*} \exp(-\frac{E_i - E^*}{T_e}) \sim 10^4 N^*$$

g\* ~30 is the degeneracy of N\* state

The energy stored in highly excited states

$$\varepsilon^{**} \approx (E^* - E_m) \frac{n_f^3}{g^*} \frac{k_e N_e}{k_q N} \sqrt{\frac{W\eta}{E_m k_p}} \exp(-\frac{E_i - E^*}{T_e})$$

$$\varepsilon^{**} \approx 10^{17} \frac{\sqrt{W[W/cm^3]}}{p[Torr]}, \frac{eV}{cm^3}$$

$$\frac{\varepsilon^{**}}{c_{p}NT} \approx 1$$

The energy released to heat behind the shock wave

$$\Delta \varepsilon \approx \varepsilon * * (1 - \frac{N_0 N_{e1}}{N_1 N_{e0}})$$

0 and 1 indexes correspond to the gas and plasma parameters before and behind the shock

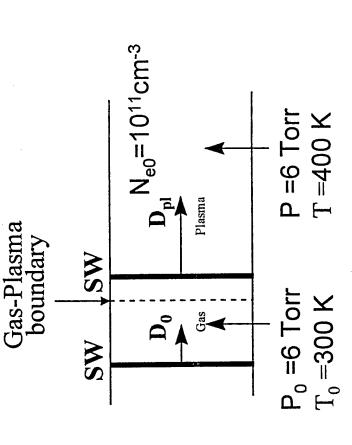
The relaxation length behind the SW front

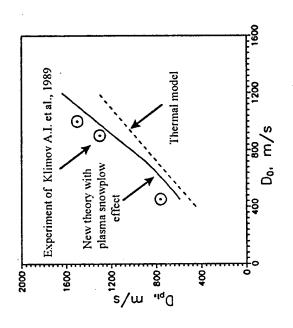
$$\xi_r \approx D \frac{N_0}{N_1} \frac{1}{k_p N_m} \approx 4 \times 10^{-5} \frac{N_0}{N_1 \sqrt{W[W/cm^3]}} D[cm/s], cm$$

## Improves Agreement of Theory with Experiment Inclusion of Plasma Effects Dramatically for 1-D Shock Penetrating Into a Plasma

Physical System
1.3<M<3.5, M= D<sub>0</sub>/a<sub>0</sub>,
a<sub>0</sub>=sound velocity

Dependence of shock speed in plasma D<sub>pl</sub> versus the initial shock speed D<sub>0</sub> in undisturbed gas.





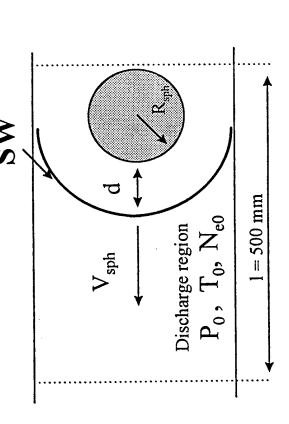
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## Improves Agreement of Theory with Experiment for Hypersonic Sphere Entering a Plasma Inclusion of Plasma Effects Dramatically

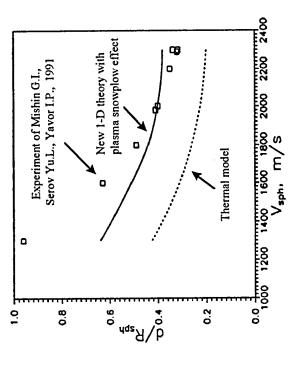
### Physical System

 $P_0=45 \text{ Torr, } T_0=1350 \text{ K, N}_{e0}=10^{11} \text{cm}^{-3},$ 

1.7<M<3.2,  $M=V_{\rm sph}/a_0$ ,  $R_{\rm sph}=20~\rm mm$ 



Dependence of relative shock standoff distance d/R<sub>sph</sub> from the sphere versus the speed of the sphere V<sub>sph</sub>.



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### Conclusions

- The mechanism of shock wave (SW) acceleration and attenuation due to interaction with a weakly ionized plasma really exists
- Preliminary calculations of 1-D SW speed in plasma are in a good agreement with experimental results when the highly excited states energy release behind the SW front is taken into account
- SW acceleration is accompanied by decrease of density and velocity jump with a small increase of static pressure jump through the SW front
- The foregoing results in a decrease of dynamic pressure jump through the SW front
- The creation of a discharge plasma IN FRONT OF the shock wave courses the SW attenuation and drag reduction for supersonic and hypersonic vehicles
- More detailed kinetic analysis is necessary to obtain more precise results

### Anomalous Behavior of Shocks Weakly Ionized Gases Theory & Modeling

Department of Mechanical Engineering The Ohio State University Columbus, Ohio 43210 Vish V. Subramaniam and Chemical Physics

Non-Equilibrium Thermodynamics Laboratories & Center for Advanced Plasma Engineering

- Anomalous effects seen in two different types of experiments:
- (1) Ballistic range



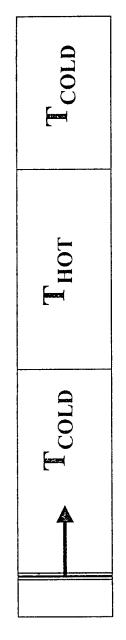
(2) Spark-generated shock launched into a glow discharge (WPAFB)

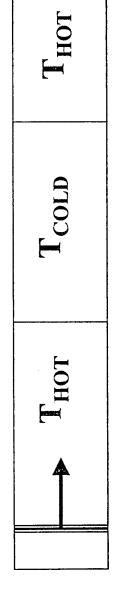


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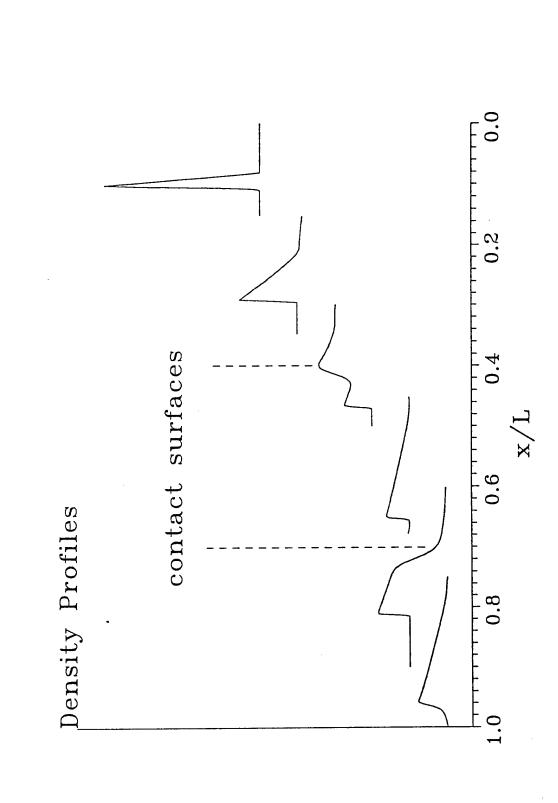


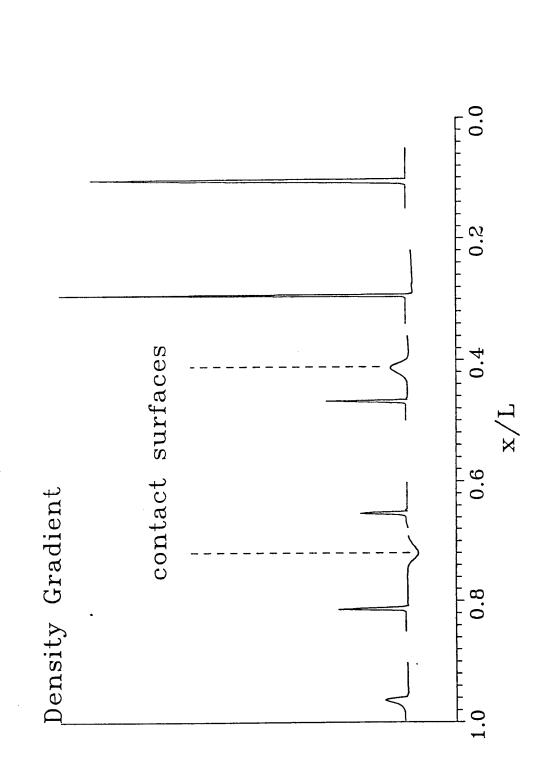
## Effects of purely axial thermal gradients

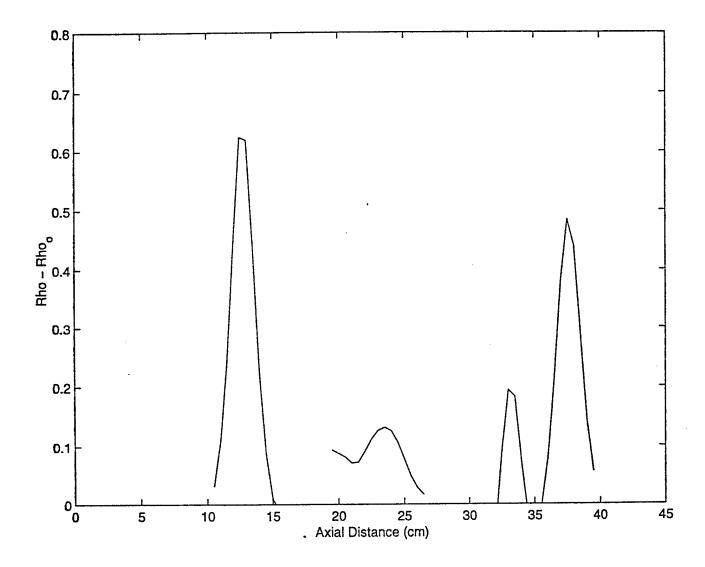


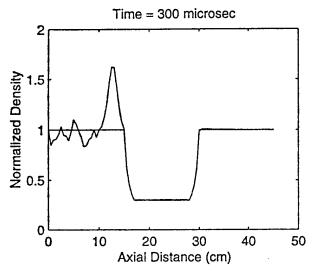


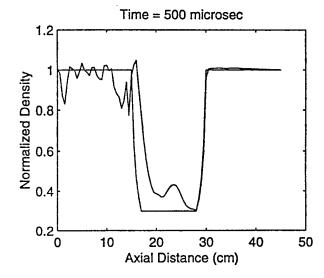
February 17, 1998

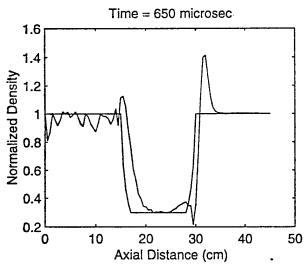


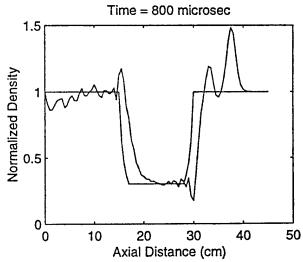


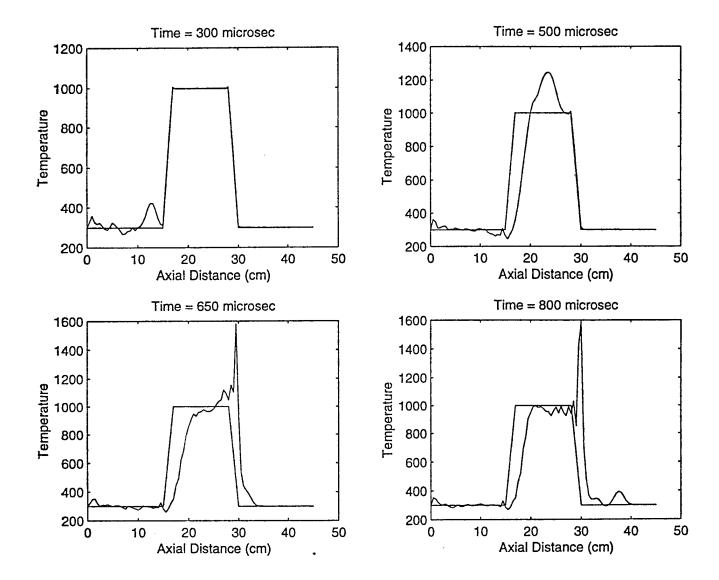


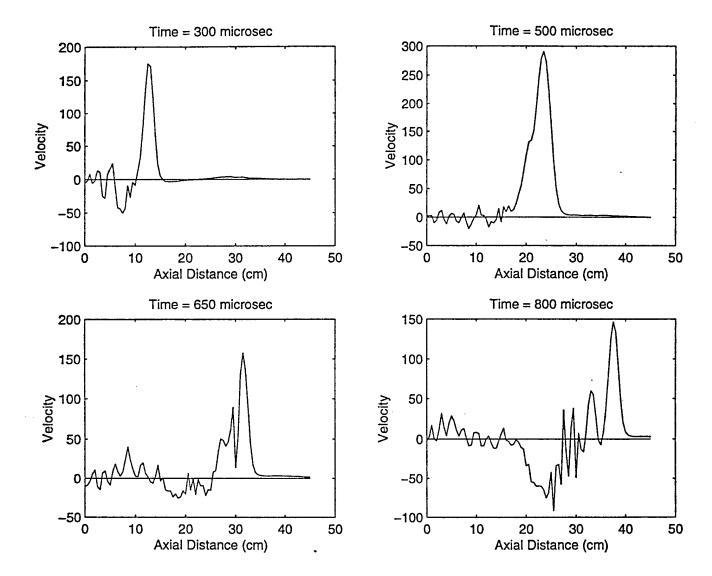


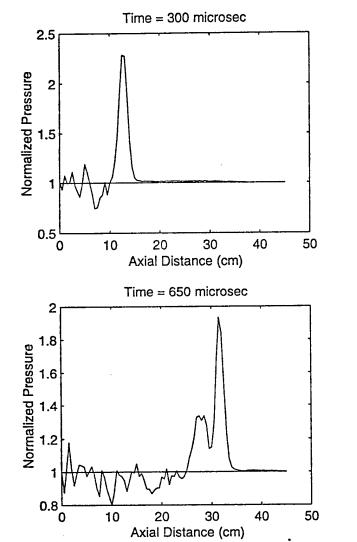


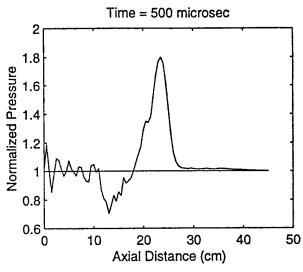


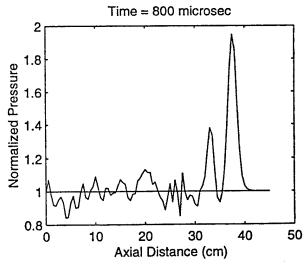


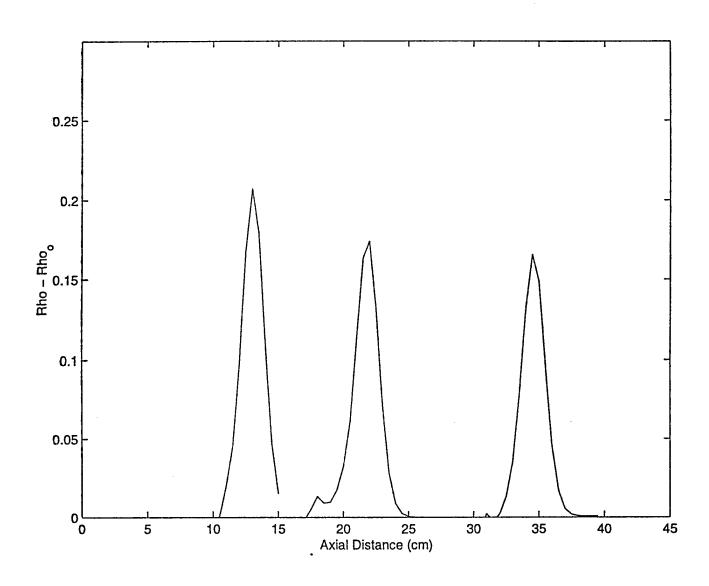












0.45

0.4

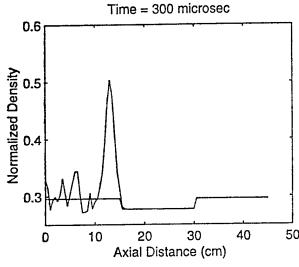
0.35

0.3

0.25

10

Normalized Density



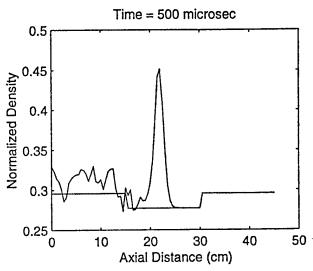
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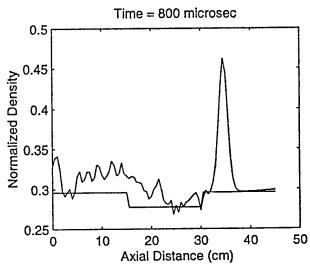
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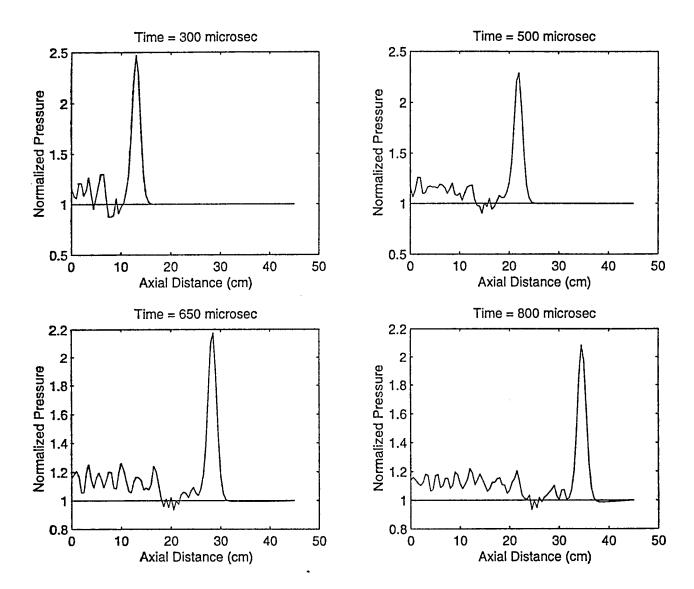
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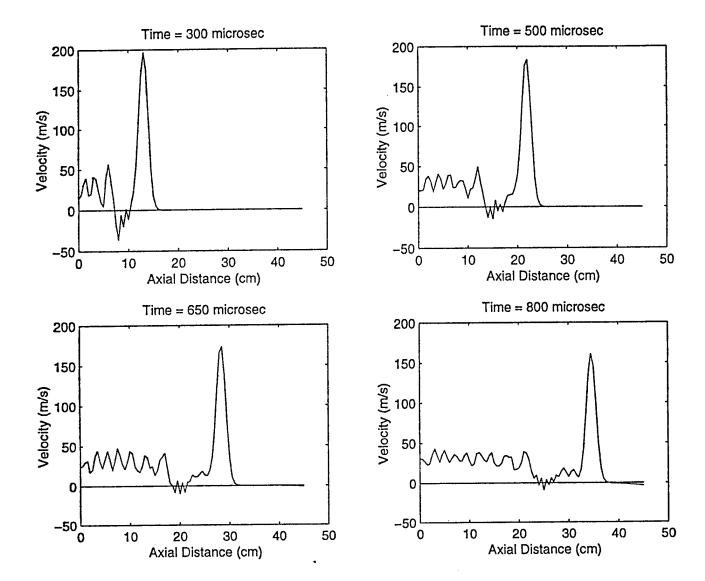


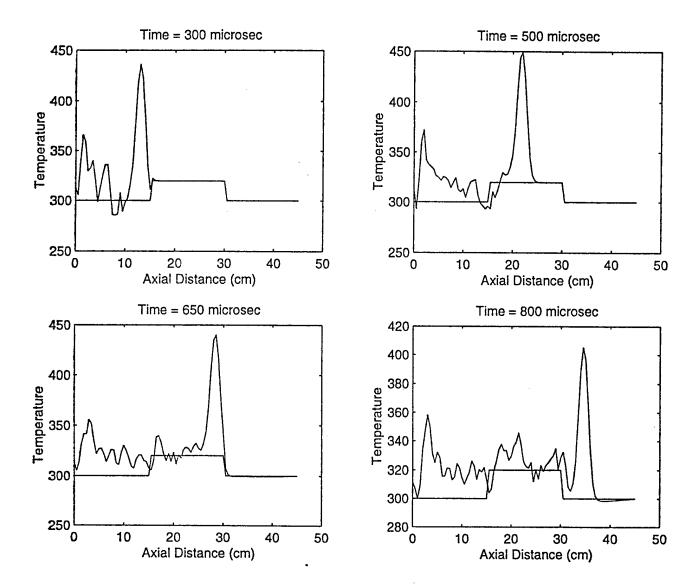
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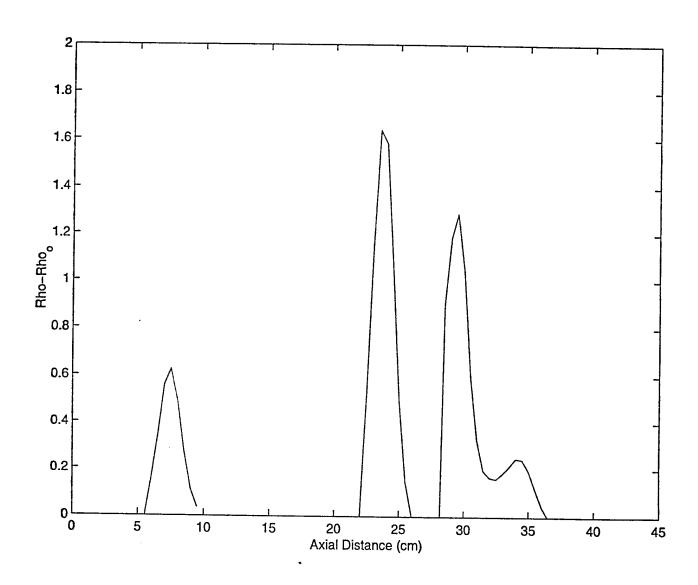


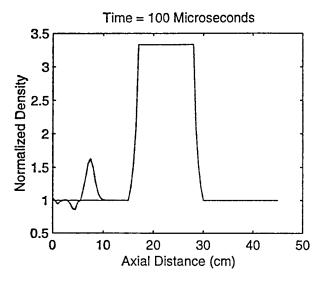


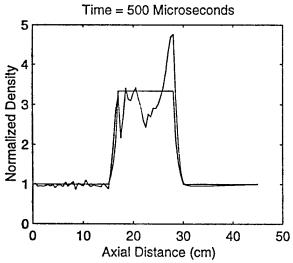


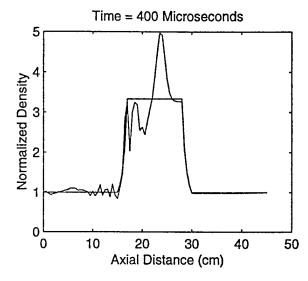


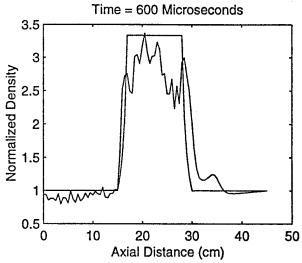


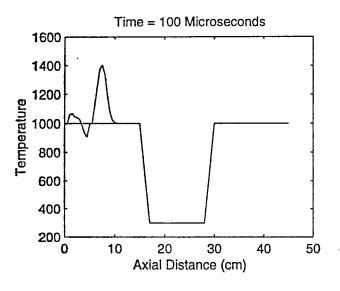


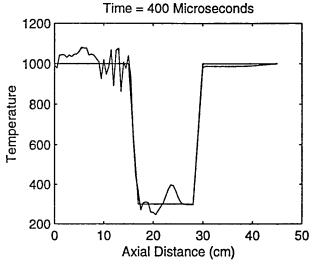


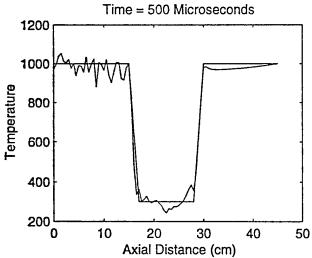


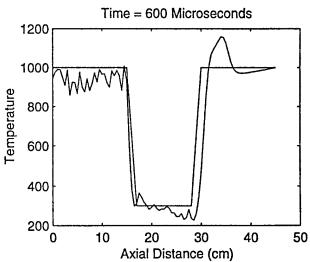


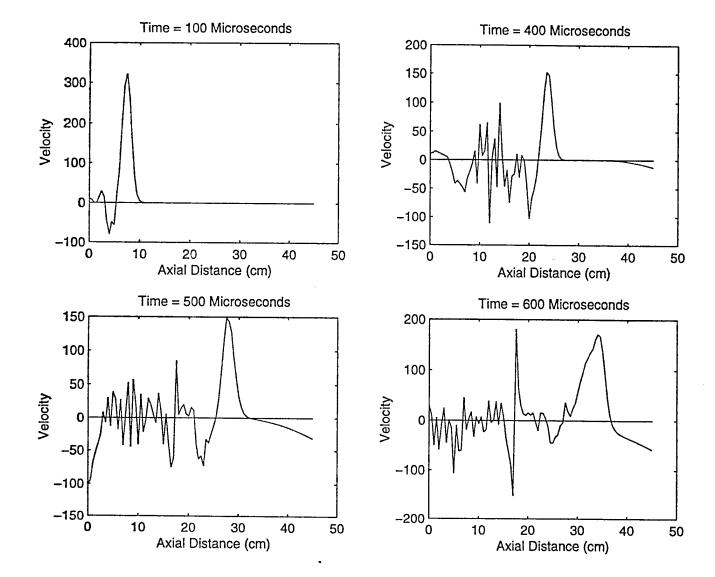


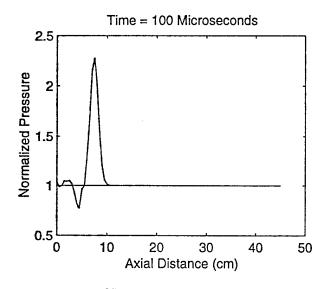


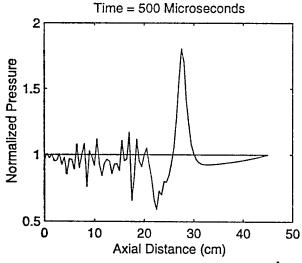


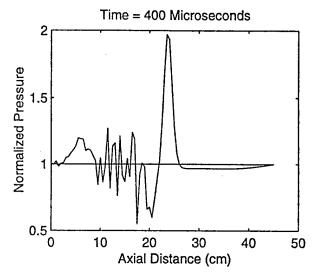


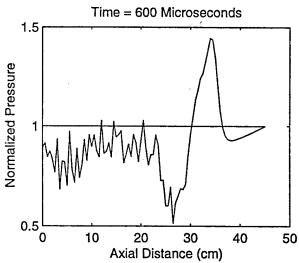




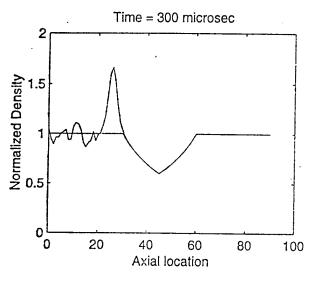


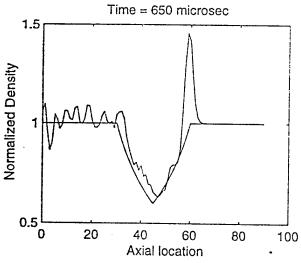


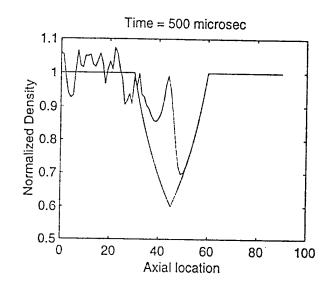


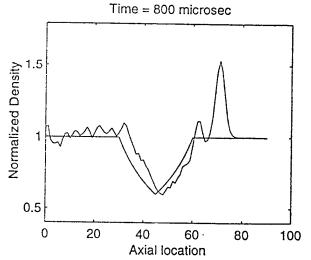


CASE III

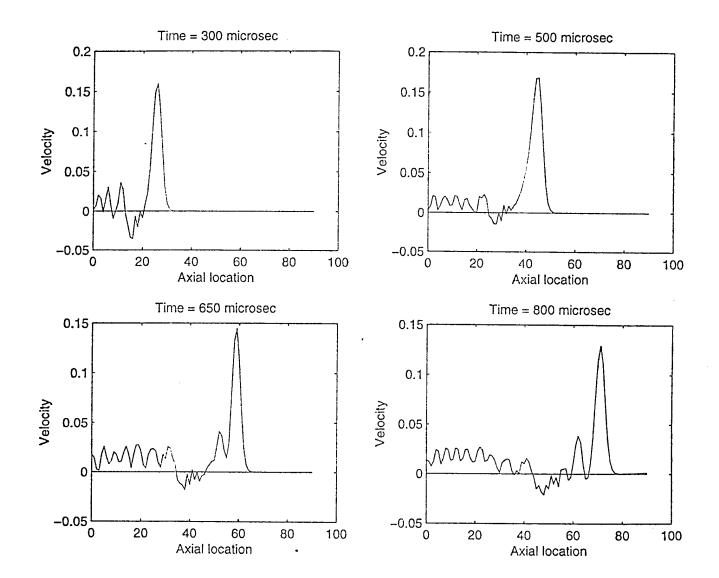






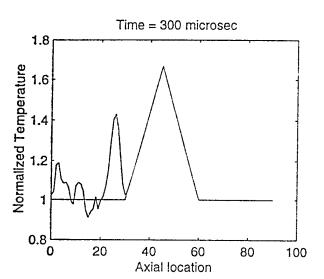


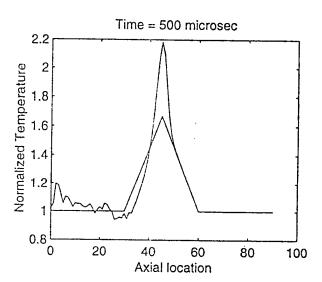
CASE TIT

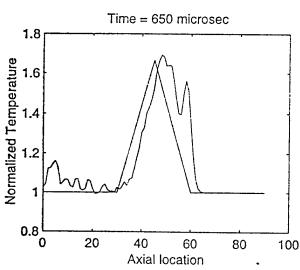


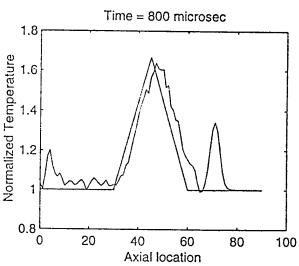
1) No radial lemp g.
2) Triangular
axial lemp gra
3) No plasma

CASE TT

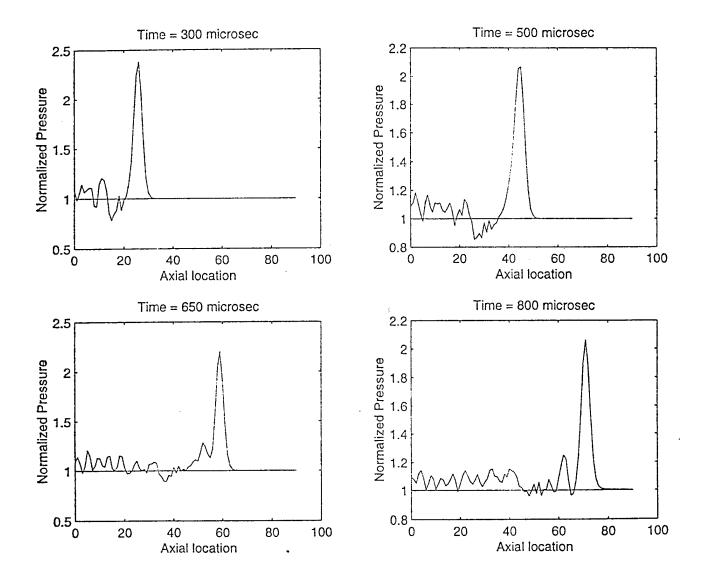


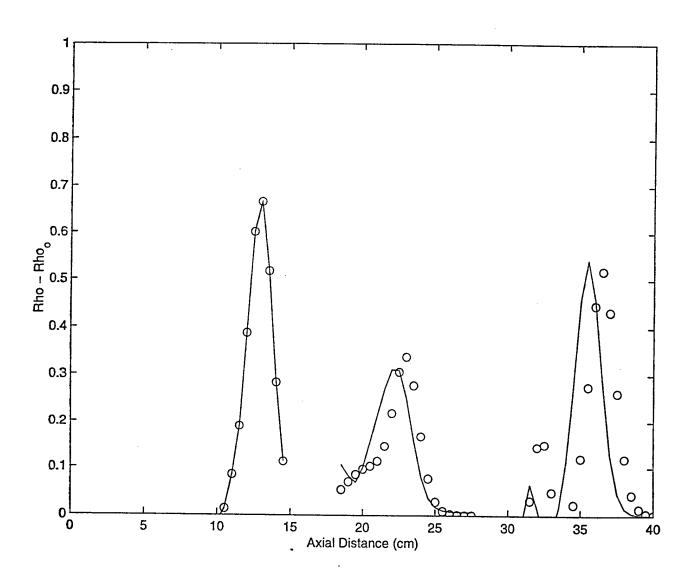


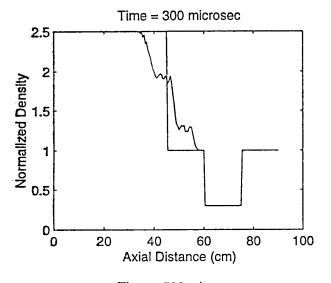


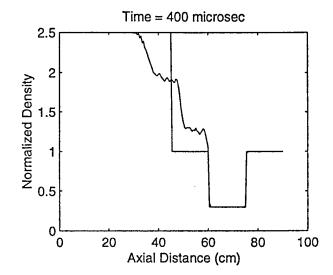


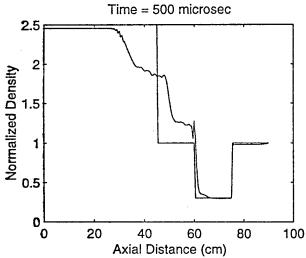
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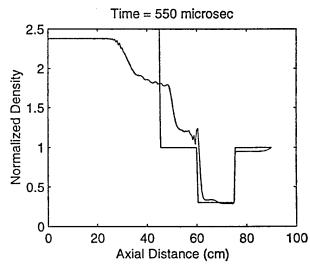


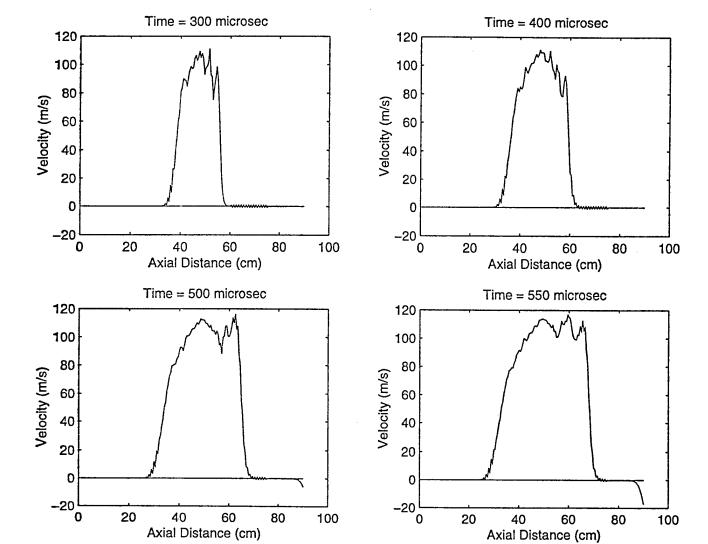


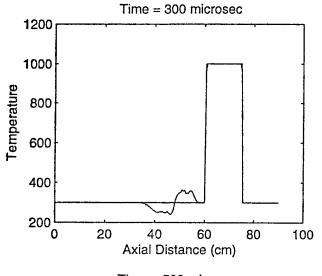


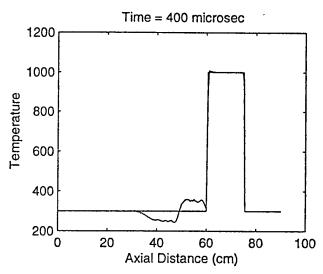


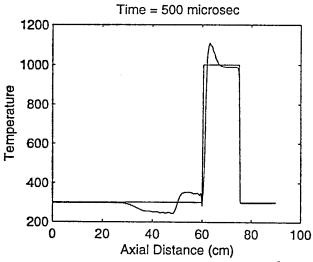


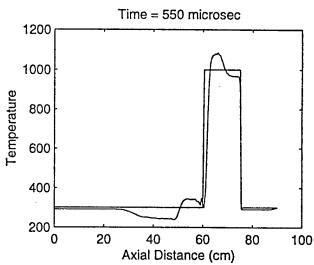


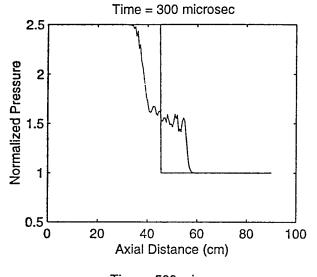


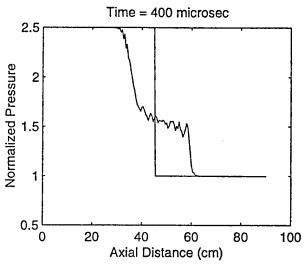


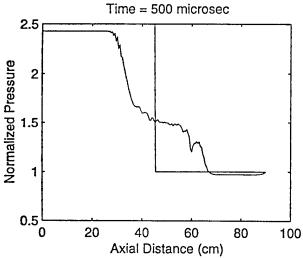


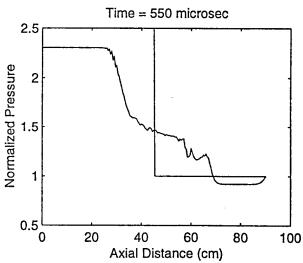


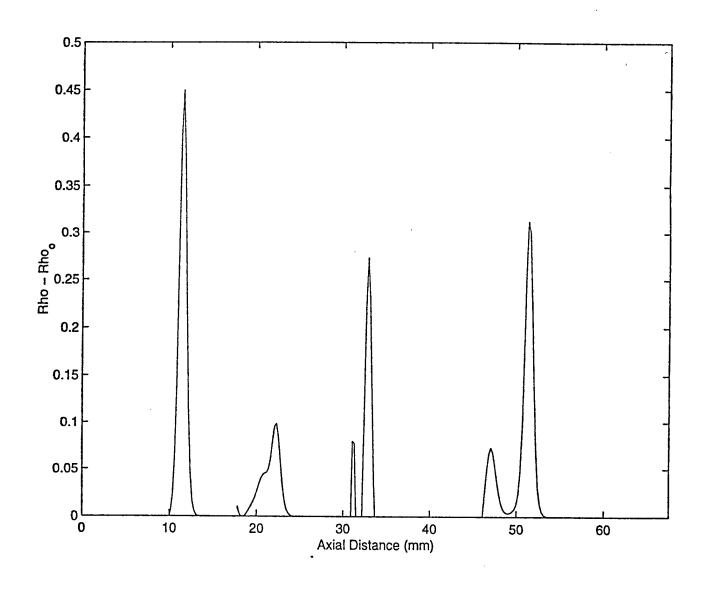


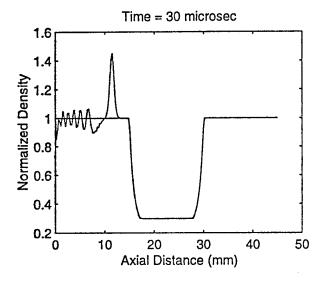


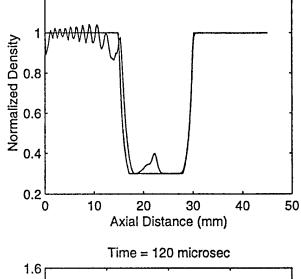






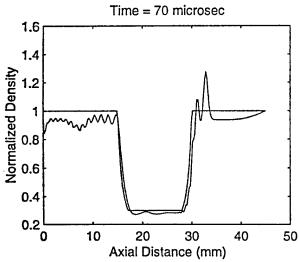


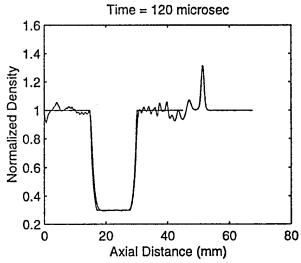


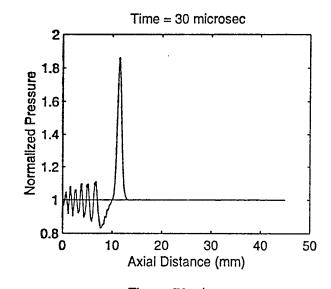


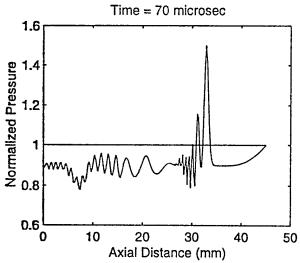
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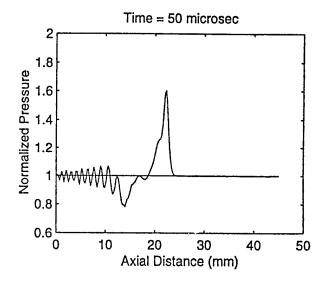
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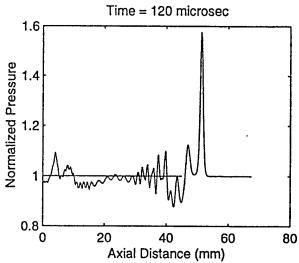


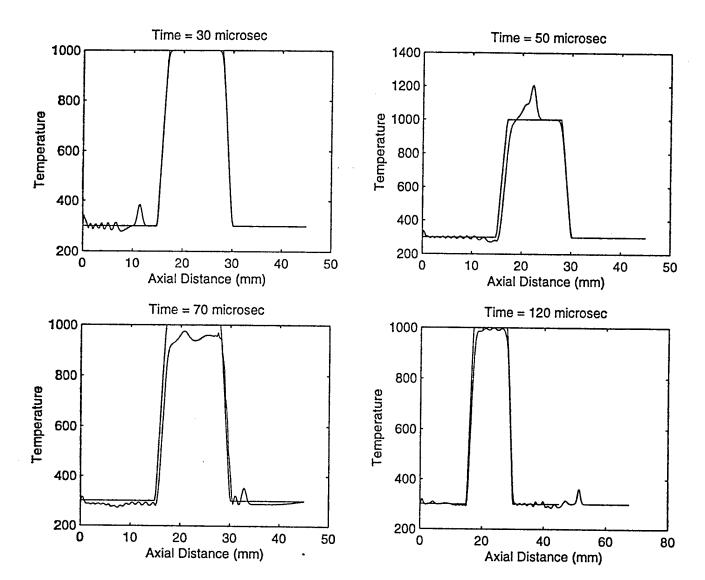


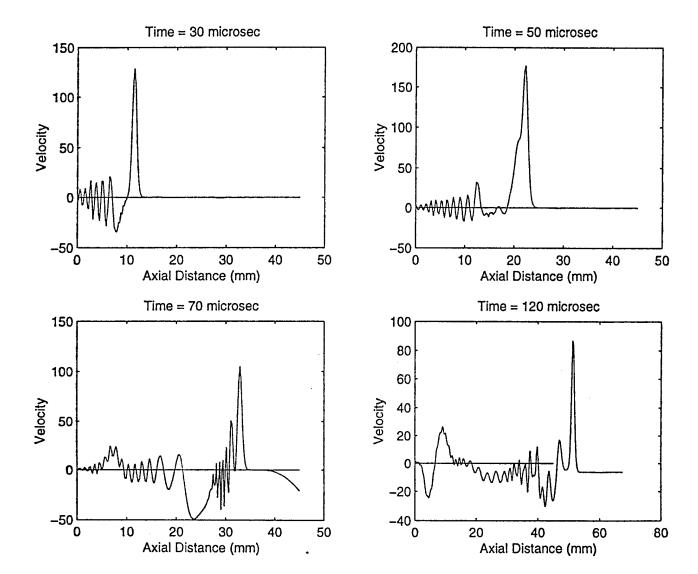


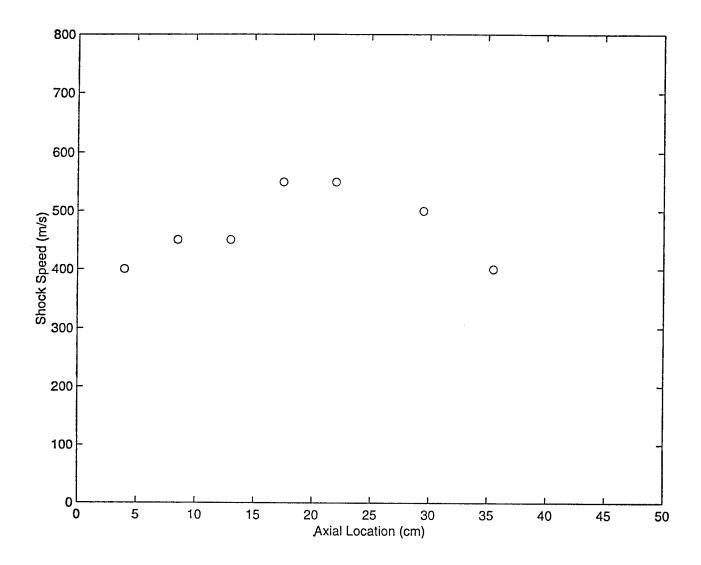


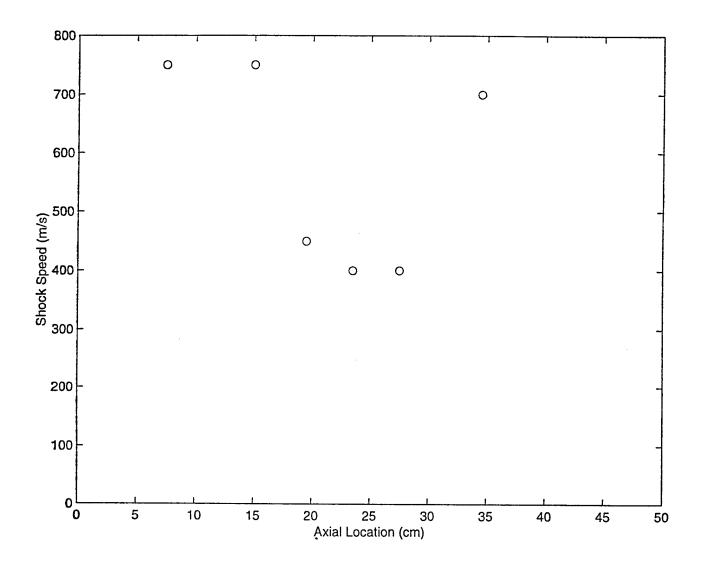














## Introduction

- · Anomalous behavior of shock waves in weakly ionized plasmas:
- shock wave accelerates
- stand-off distance increases
- shock splits into two or more structures
- shock strength (as measured by density differences) diminishes
- results occur in atomic and molecular gases
- shock nearly recovers its original strength well downstream of the discharge.

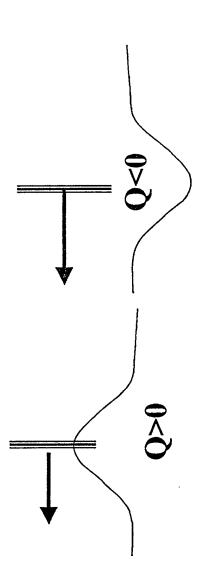


- Previous simulations (Bailey & Hilbun, Macheret & Martinelli) show radial thermal gradients can alter density profiles:
- in piston-driven shock tubes
- and when there is a curved boundary initially separating the hot and cold regions of a gas
- explain some experimental observations, but cannot explain others (such as shock Thermal effects have been invoked to recovery distance).



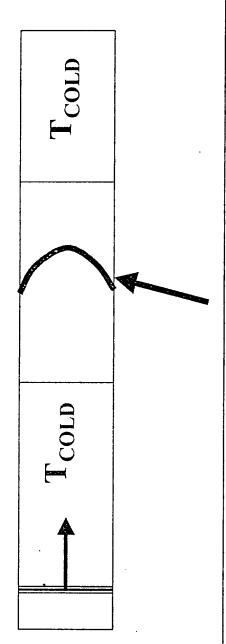
## Previous analysis (Adamovich et. al.) shows:

- (1) In order to change shock structure, an agent must have energy comparable to the incident kinetic energy density of the incident flow
- (2) Two globally adiabatic shocks, able to exchange reproduces themselves experimental observations: among





#### Effects of Radial Thermal Gradients (2-D axi-symmetric Navier-Stokes solution for Argon)



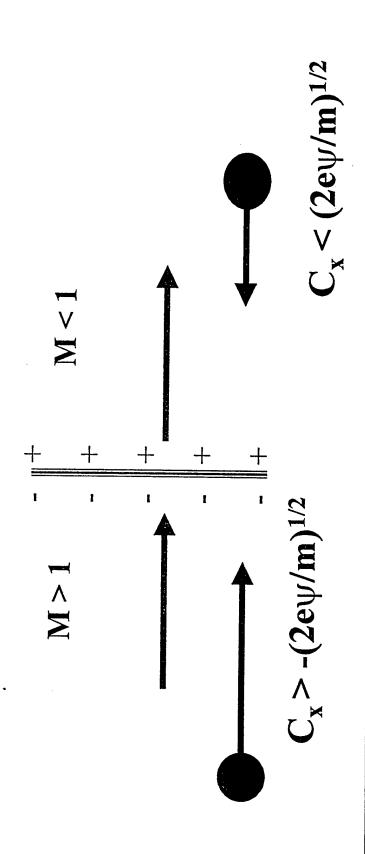
varying from T<sub>HOT</sub> at the centerline to Initial parabolic temperature profile T<sub>COLD</sub> at the wall.

# Summary of Thermal Effects

- Axial temperature gradients cause splitting of an impulsive load into two distinct waves, strong leader, and a weak follower.
- Radial gradients affect results quantitatively, but are not the cause of this splitting.
- Shock recovery is almost immediate, whereas they vary from 10 cm to 20 cm in the Ganguly-Bletzinger experiments.

: THERMAL EFFECTS CANNOT SOLELY EXPLAIN OBSERVED EXPERIMENTAL RESULTS.

a potential in the neutral gas, because Suppose that space charge layer induces neutrals are polarizable:



February 26, 1998

and Challe w. Mach. Mind To in Thomas Flux

CONTRIBUTION TO LEFTEME

FLUX

## Conseduences

Let the force experienced by the neutral particles be:

$$F_x = -e \left( \frac{\partial \psi}{\partial x} \right) 3 \sqrt{\frac{2e\psi}{m}} - C_x \left| 3(x - x_0) + 3 \sqrt{\frac{2e\psi}{m}} + C_x \right| 3(x_0 - x)$$

where 
$$\widetilde{\mathfrak{Z}}(z) = \begin{cases} 0, & z < 0 \\ 1, & z > 0 \end{cases}$$
 is the Heaviside step function,

and  $C_x$  is the x-component of the absolute particle velocity

## What would be the corresponding macroscopic equations to lowest order?

#### Continuity

$$\frac{\partial n}{\partial t} + \frac{\partial}{\partial x} (nu) = N = \begin{cases} \frac{ne}{m} \left( \frac{\partial \psi}{\partial x} \right) \sqrt{\frac{m}{2\pi kT}} & e^{-\left( \sqrt{\frac{e\psi}{kT}} - u\sqrt{\frac{m}{2kT}} \right)^2} \\ \frac{ne}{m} \left( \frac{\partial \psi}{\partial x} \right) \sqrt{\frac{m}{2\pi kT}} & e^{-\left( \sqrt{\frac{e\psi}{kT}} + u\sqrt{\frac{m}{2kT}} \right)^2} \\ \frac{ne}{m} \left( \frac{\partial \psi}{\partial x} \right) \sqrt{\frac{m}{2\pi kT}} & e^{-\left( \sqrt{\frac{e\psi}{kT}} + u\sqrt{\frac{m}{2kT}} \right)^2} \\ \vdots & x < x_o \end{cases}$$

### » x-momentum

$$\frac{\partial(nu)}{\partial t} + \frac{\partial}{\partial x} \left( nu^2 + \frac{nkT}{m} \right) = M = \begin{cases} \frac{en}{\partial x} \left( \frac{\partial \psi}{\partial x} \right) \sqrt{\frac{e\psi}{\pi kT}} e^{-\left(\sqrt{\frac{e\psi}{kT}} - u\sqrt{\frac{m}{2kT}}\right)^2} \\ -\frac{1}{2} \left[ 1 - erf \left( u\sqrt{\frac{m}{kT}} - \sqrt{\frac{e\psi}{kT}} \right) \right] \right] & ; x > x_o \\ \frac{en}{m} \left( \frac{\partial \psi}{\partial x} \right) \left( \frac{e\psi}{\pi kT} e^{-\left(\sqrt{\frac{e\psi}{kT}} + u\sqrt{\frac{m}{2kT}}\right)^2} \right) \\ -\frac{1}{2} \left[ 1 - erf \left( -u\sqrt{\frac{m}{2kT}} - \sqrt{\frac{e\psi}{kT}} \right) \right] \right] & ; x < x_o \end{cases}$$

#### Energy

$$\frac{\partial}{\partial t} \left( \frac{3}{2} nkT + \frac{1}{2} mnu^2 \right) + \frac{\partial}{\partial x} \left( \frac{5}{2} nukT + \frac{1}{2} mnu^3 \right) = S$$

$$- ne \left( \frac{\partial \psi}{\partial x} \right) \left[ \frac{2kT}{m\pi} \right]^{1/2} + \left( \frac{e\psi}{kT} \right) \left( \frac{kT}{2\pi m} \right)^{1/2} \right] - \left( \sqrt{\frac{e\psi}{kT}} - u \sqrt{\frac{m}{kT}} \right)^2$$

$$- \frac{neu}{2} \left( \frac{\partial \psi}{\partial x} \right) \left[ 1 - erf \left( u \sqrt{\frac{m}{kT}} - \sqrt{\frac{e\psi}{kT}} \right) \right] \qquad ; \quad x > x_o$$

$$- ne \left( \frac{\partial \psi}{\partial x} \right) \left[ \frac{2kT}{m\pi} \right]^{1/2} + \left( \frac{e\psi}{kT} \right) \left( \frac{kT}{2\pi m} \right)^{1/2} \right] = - \left( \sqrt{\frac{e\psi}{kT}} + u \sqrt{\frac{m}{kT}} \right)^2$$

$$- \frac{neu}{2} \left( \frac{\partial \psi}{\partial x} \right) \left[ 1 - erf \left( -u \sqrt{\frac{m}{kT}} - \sqrt{\frac{e\psi}{kT}} \right) \right] \qquad ; \quad x < x_o$$

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# Source term in momentum equation

$$M_{1} \approx -\frac{en_{1}}{m} \left( \frac{\partial \psi}{\partial x} \right) \Big|_{1} e^{-\frac{\gamma}{2} M_{1}^{2}}$$

$$I_{2} \approx -\frac{en_{2}}{m} \left( \frac{\partial \Psi}{\partial x} \right) \bigg|_{2} e^{-\frac{\gamma}{2} M^{\frac{2}{2}}}$$

$$\Rightarrow \left| \frac{M_2}{M_1} \right| \approx \frac{n_2}{n_1} \frac{(\partial \psi / \partial x)|_2}{(\partial \psi / \partial x)|_1} e^{\frac{\gamma}{2} (M_1^2 - M_2^2)}$$

### is upstream Net Force

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## Source terms in continuity equation

$$N_1 \approx \frac{en_1}{m} \left( \frac{\partial \psi}{\partial x} \right) \Big|_1 \sqrt{\frac{m}{2\pi kT_1}} e^{-\frac{\gamma}{2} M_1^2}$$

$$I_2 \approx -\frac{en_2}{m} \left( \frac{\partial \psi}{\partial x} \right) \Big|_2 \sqrt{\frac{m}{2\pi k T_2}} e^{-\frac{L}{2} M \frac{2}{2}}$$

$$\frac{N_2}{N_1} \approx -\frac{n_2}{n_1} \frac{(\partial \psi / \partial x)|_2}{(\partial \psi / \partial x)|_1} \sqrt{\frac{T_1}{T_2}} e^{\frac{\gamma}{2}} (M_1^2 - M_2^2)$$

$$\Rightarrow N_2 > N_1$$

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## Source term in energy equation

$$S_1 \approx e n_1 \left( \frac{\partial \psi}{\partial x} \right) \bigg|_1 \left( \frac{\gamma k T_1}{m \pi} \right)^{1/2} \left[ \left( \frac{\overline{2}}{\sqrt{\gamma}} - M_1 \right) \right] e^{-\frac{\gamma}{2} M_1^2}$$

$$S_2 \approx -en_2 \left( \frac{\partial \psi}{\partial x} \right) \left| \left( \frac{\gamma k T_2}{m \pi} \right)^{1/2} \left[ \left( \frac{2}{\sqrt{\gamma}} + M_2 \right) \right| e^{-\frac{\gamma}{2} M_2^2}$$

$$\frac{S_2}{S_1} \approx \frac{n_2}{n_1} \frac{(\partial \psi / \partial x)|_2}{(\partial \psi / \partial x)|_1} \sqrt{\frac{T_2}{T_1}} \left[ \sqrt{\frac{2}{\gamma} + M_2} \right] e^{\frac{\gamma}{2} (M_1^2 - M_2^2)}$$

in sign when  $\mathbf{M}_1 = \sqrt{\frac{2}{\gamma}}$ Note change

THREE CASES

(A)

(8)

(e)

Aut

- Distribution function will be non-M-B in the neighborhood of the shock
- ⇒ steep thermal, and density gradients will induce additional mass, momentum, and energy transfer from downstream region to upstream region.
- Questionable as to whether a steady state energy can exist when sources are present in and momentum, continuity, equations.

# Case(B): Potential well ahead of shock

- $(2/\gamma)^{1/2}$  while S $\rightarrow$ 0 for x>0 (downstream of S>0, provided M<sub>1</sub> in the region is less than • Just upstream of the shock, for x<sub>o</sub><x<0, the shock) since  $\partial \psi / \partial x \rightarrow 0$  there
- ⇒ SPLITTING?
- For  $M_1 > (2/\gamma)^{1/2}$ , S<0 in the same region  $\Rightarrow$  STABLE
- Further, M<0 for  $x>x_0 \Rightarrow a$  body force ⇒ LARGER STAND-OFF DISTANCE driving shock upstream is present

### Summary

- pulse in the presence of a streamwise temperature gradient But, split structure Classical gas dynamics predicts splitting of a appears different from that observed experiments.
- which induced dipole effects cause the presence of local adverse thermal gradients at the shock There may be special circumstances under front, by affecting the distribution function.

### Flow Control via MHD and EMHD

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Providence, RI 02912

http://www.cfm.brown.edu/CRUNCH

AFOSR Workshop on
Understanding and Control of Ionized High-Speed Flows

February 26–27, 1998 Princeton, NJ

### **High-Speed Flow Features**

:- - Multi-Rate Physics - Multiple BLs

- Strong shock wave effects/interactions
  - thin layers, small detachment distance, etropy layer
- Strong viscous effects/interactions

$$- \ \delta \sim \frac{M^2}{\sqrt{Re}}$$

- increased drag, heating at leading edge
- Transitional flow
  - $Re_c \sim 10^8$  vs.  $10^5$  (subsonic)
  - $C_f$  and  $C_H$  are  $3 \times$  laminar
  - $Re_c^{\theta} \sim 100 M_e$
- Nonequilibrium
  - thermal, chemical
  - introduction of length scale
  - multi-rate physics
- Ionization

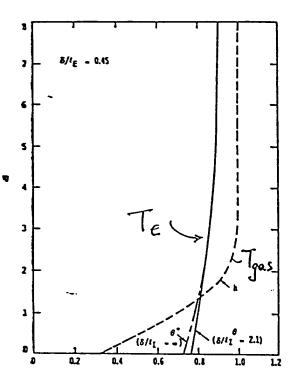
- 4000 K to 6000 K: 
$$NO \rightarrow NO^+ + e^-$$
 (mild)

- > 9000 K: 
$$N \to N^+ + e^-$$
  
 $O \to O^+ + e^-$ 

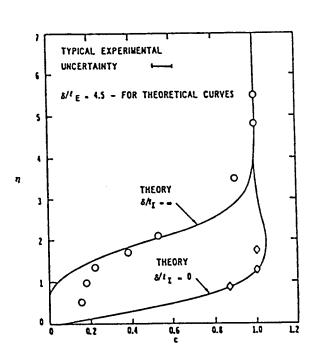
- Above 20kM + 10 km/s
- External B, E, frequencies
- Multiple boundary layers
  - hydrodynamics, thermal, species
  - electric conductivity, etropy layers

### Non-Equilibrium Plasma Boundary Layer

- Effects on  $T_e$ ,  $\sigma$
- atmospheric-pressure potassium-seeded argon plasma



Normalized Temperature



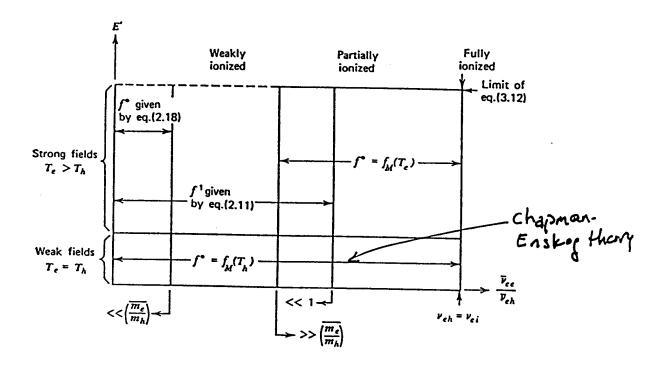
Normalized Conductivity

Ref: Brown & Mitchner (1971)

"... Even in plasma which is strongly collision dominated, significant nonequilibrium may be present in the boundary layer adjacent to a cooled solid surface..."

Note: Joule heating due to E could further increase conductivity.

### **Electrical Conductivity**



### Electric Field vs. Ionization

• In constant E, B fields tensor conductivity

Weakly-ionized 
$$\begin{cases} \sigma_{\parallel} = \mathcal{F}(n_e, m_e, \nu_{eH}, f^0) \\ \sigma_{\perp} = \mathcal{F}(n_e, m_e, \nu_{eH}, f^0, \omega_e) \\ \sigma_{H} = \mathcal{F}(n_e, m_e, \nu_{eH}, f^0, \omega_e) \end{cases}$$

$$- \text{If } B = 0 \Rightarrow \sigma_{\perp} = \sigma_{\parallel} = \sigma$$

$$- \text{If } E \sim e^{-i\omega t} \Rightarrow \text{dependence of } \sigma \text{ on } \omega \quad \text{i.e. pulsing with } f^0 = \mathcal{F}(E_{11}^0, E_{\perp}, \nu_{RH}, T_H, m_e, m_H)$$
Note:  $f^0 = \mathcal{F}(E_{11}^0, E_{\perp}, \nu_{RH}, T_H, m_e, m_H)$ 

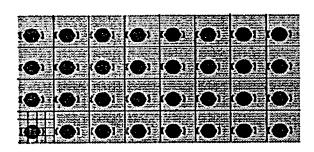
### **Lorentz Force: Numerical Modeling**

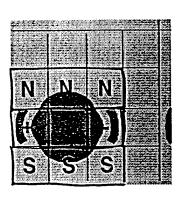
ullet Governing Equations for  $ec{B}$  and  $ec{E}$ 

Boundary Conditions - The Motz problem

Example 1: Electromagnetic Tiles

Dirichlet:  $\vec{F}_{\perp} \sim \frac{1}{3} \vec{F}_{\parallel}$ ; Neumann:  $\vec{F}_{\perp} \sim \vec{F}_{\parallel}$ 





Example 2: Alternate stripes of electrodes/magnets  $F_{\mu} \sim e^{-\frac{\pi}{a}\lambda y}$ ? penetration

Dirichlet Neumann D-N Mixed  $\lambda$  4 2 8 8

### **Lorentz Force**

• MHD Assumptions  $(t_c > \omega_p^{-1})$ 

- Convection current neglected:  $\frac{\rho_c U}{\tau} \ll 1$ 

- Force due to net charge neglected:  $\frac{\rho_c E'}{|I \times R|} \ll 1$ 

Then:

$$|| \vec{F}_L = \vec{J} \times \vec{B}; \ E_0 = \text{ external}$$

$$|| \vec{J} = \sigma(\vec{E} + \vec{u} \times \vec{B}) + \sigma \vec{E}_0$$
 simple Ohm's law

MHD-Control

**EMHD-Control** 

$$ullet$$
 Apply  $ec{B}$ 

$$ullet$$
 Apply  $ec{B}$  and  $ec{E}$   $ullet$   $E=-
abla\Phi$   $ullet$   $J\sim\sigma E_0$ 

$$\bullet E = -\nabla \Phi$$

• 
$$J \sim \sigma E_0$$

$$\bullet \ \nabla^2 \Phi = \nabla \cdot (\vec{u} \times \vec{B})$$

• 
$$\nabla^2 \Phi = \nabla \cdot (\vec{u} \times \vec{B})$$
 •  $I_{\text{applied}} = \frac{\sigma E_0 B L}{\rho U^2}$ 

$$\bullet \ I_{\text{induced}} = \frac{\sigma B^2 L}{\rho U}$$

where  $R_{em} = \mu \sigma U L \ll 1$  in lab scale

(neglect induced fields)

• But Ohm's law for partially ionized gas:

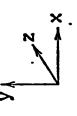
$$\underline{\vec{J}} + \beta_e \vec{J} \times \vec{b} + s\vec{b} \times (\vec{J} \times \vec{b}) = \underline{\sigma(\vec{E} + \vec{u} \times \vec{B})} + \frac{\sigma}{en_e} \nabla p_e$$
"Generalized Ohm's Law"

ion-slip

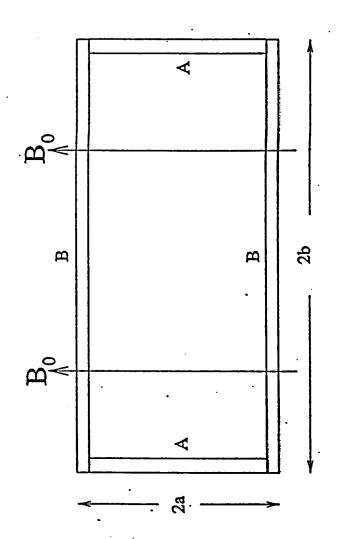
### Discontinuous Galerkin Method - $\mathcal{N}\varepsilon\kappa\mathcal{T}\alpha r$

- dynamical Direct Numerical Simulation (dDNS)
- MHD, Compressible & Incompressible flows
  - Full 3D Configurations Arbitrary Geometric Complexity
- Unstructured/Hybrids Grids
- High-Order/Spectral Accuracy
  - Conservative Formulation
  - h-refinement for shocks/discontinuities
  - ALE Algorithm for Moving Rotating Subdomains
  - METIS/MPI-based Parallelization

· MACH2/3 prototype-but high-order...

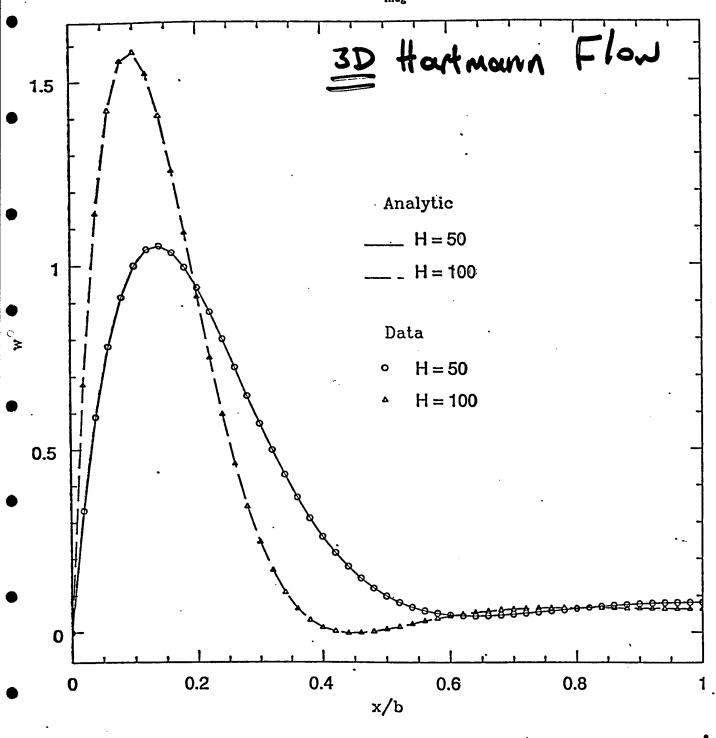


Hartmann-Hunt Flow: 3D



AA: Perfect Insulators BB: Perfect Conductors

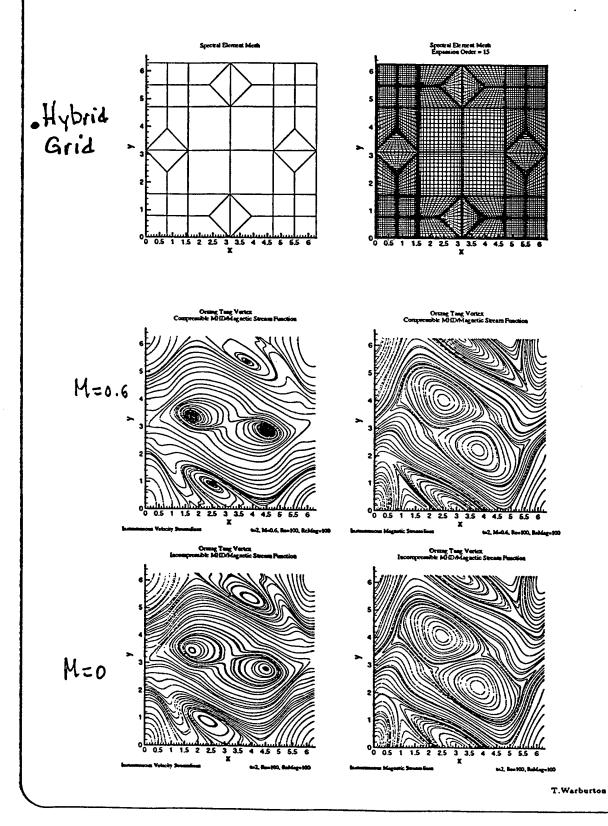
Flow is into the page



\* Spectral/hp on Unstructured Grids.

(AFOSIL)

### Orszag-Tang MHD-Vortex



### H-P Adaptive Refinement: Viscous Supersonic Flows

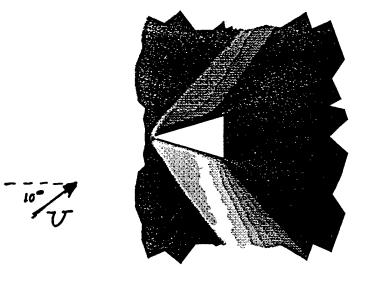


Figure 1: Discontinuous Galerkin Simulation: Density contours

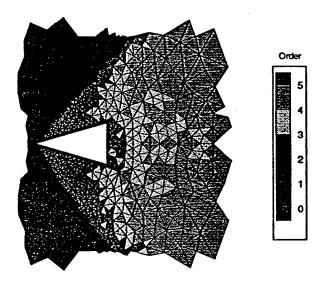
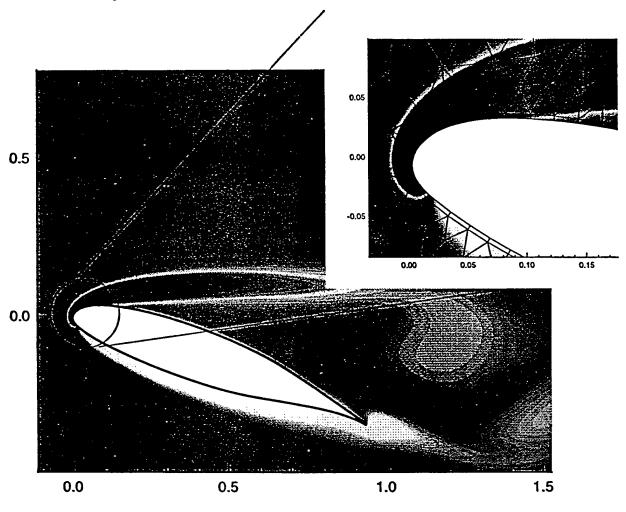


Figure 2: Unstructured grid and variable-order per element

### \* HYBRID APPROACH:

- · DNS near wall / structured
- · LES in Equilibrium regions

### Hybrid-Element Boundary Layer Resolution



PhD Thesis: T.Warburton

Plan: fed DNS with h-p refinement.

LES in equilibrium with h-p repirement

high Re #, Complex Geometry

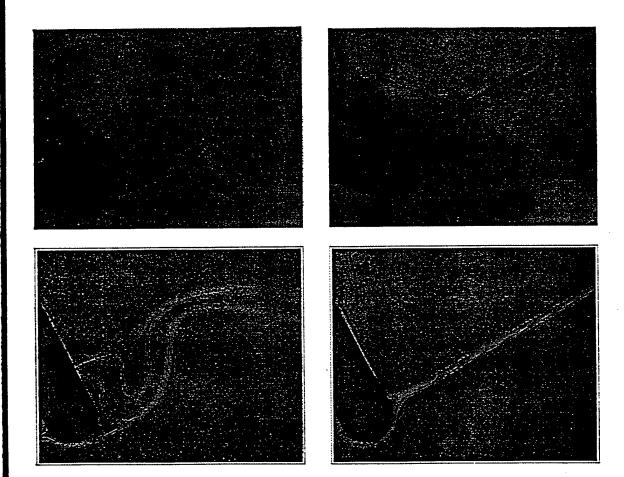
### MHD/EMHD-Simulations

- I. Laminar & Turbulent Wakes
  - a vortex street suppression
    - phase/frequency control
- II. Wall Turbulence
  - High  $\sigma$ , spanwise forcing/MHD
  - Low  $\sigma$ , steamwise forcing
  - $\bullet$  Low  $\sigma$ , "normal" forcing

Method: Parallel DNS - The  $\mathcal{N}\varepsilon\kappa\mathcal{T}\alpha r$  Code

**Experiments:** Conflicting results

### EMHD control of the flow around a circular cylinder

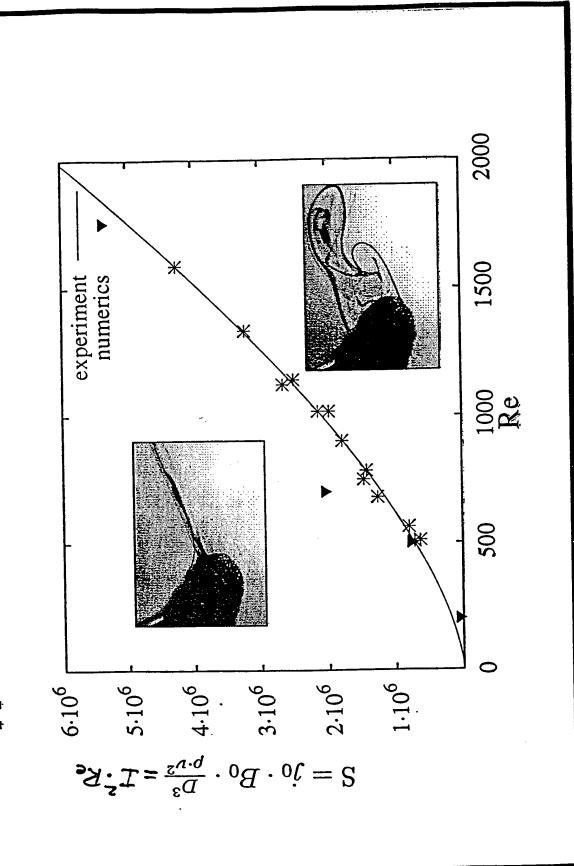


### Dimensionless numbers:

$$Re = \frac{v_{\infty} d}{v}$$
 - Reynolds number

$$N = \frac{j_0 B_0 d}{\rho v_{\infty}^2}$$
 - Interaction Parameter

## Suppression of the Kármán vortex street



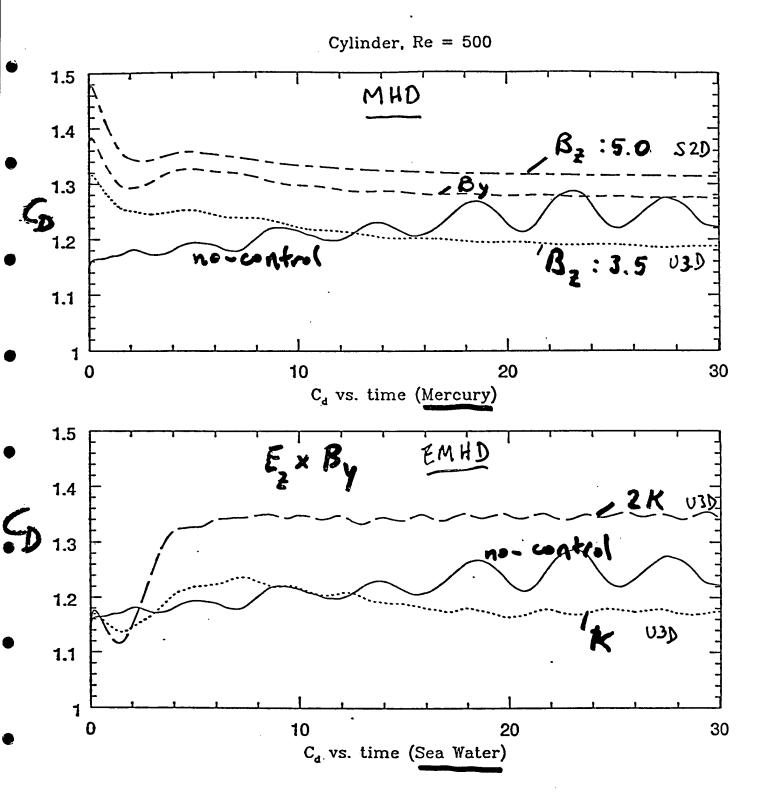
Air Force Workshop

Princeton NJ

Feb. 25, 1998

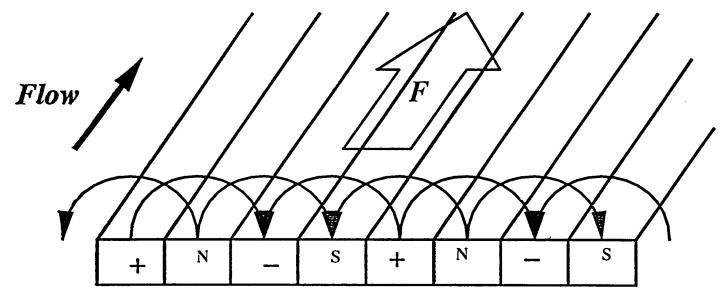
### TURBULENT WAKES

ATAA-95

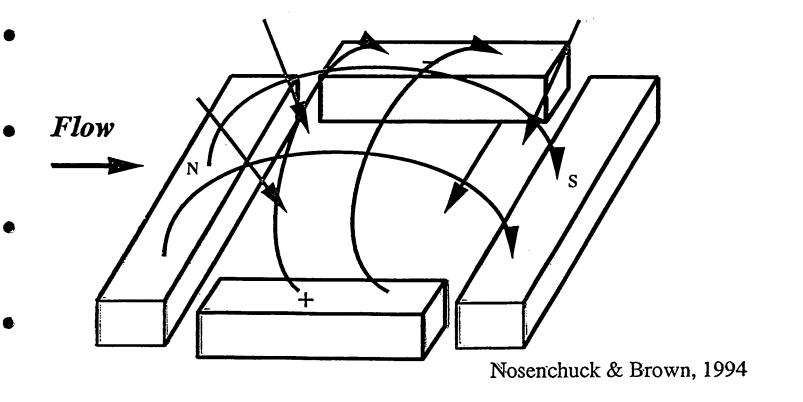


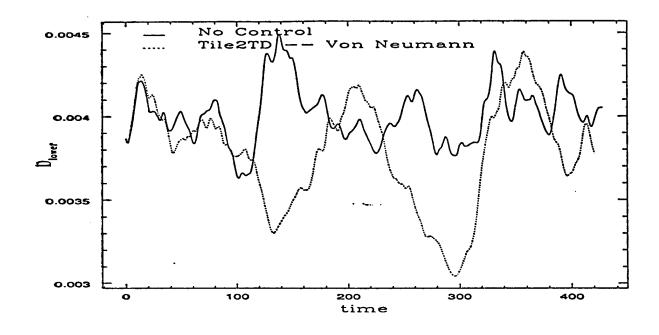
: Changes are non-Monotonic!

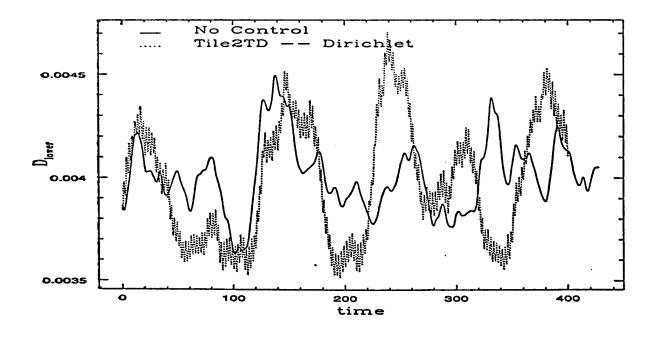
### Active Control: Lorentz Body Force



Henoch & Stace, 1995







### NEAR-WALL TURBULENCE and LAMB VECTOR

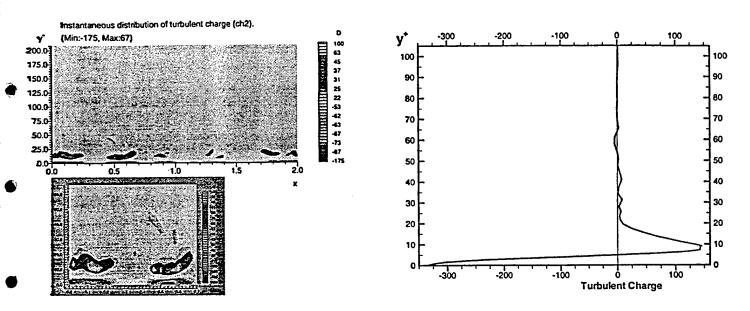


Figure 1: Dipole structure of the divergence of the Lamb vector: turbulent charge

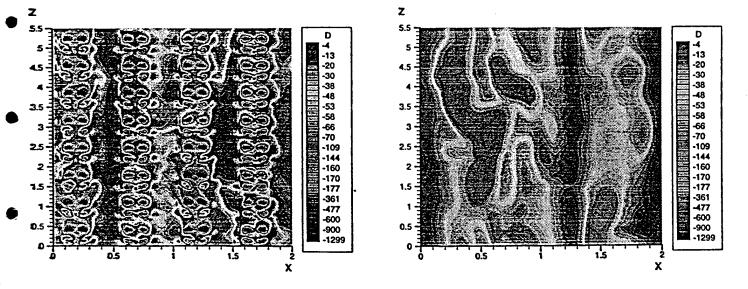


Figure 2: Footprint of the turbulent charge: LEFT - EMHD on; RIGHT: EMHD off

### **Summary**

- Explore MHD, EMHD and EHD
- Strong electrical conductivity non-uniformity
- Selection of physical model is application-dependent
  - degree of ionization
- Transitional Flow No ad hoc models
- Numerical Model ( $\mathcal{N}\varepsilon\kappa\mathcal{T}\alpha r$ ):
  - High order
  - Hybrid grids
- Benchmark Experiments

### 2D vortex dynamics associated with shock splitting

Kremeyer, Nazarenko, Newell (Arizona).

Is observed shock splitting due largely to plasma electromagnetics or due solely to gas heating which accompany the introduction of non-equilibrium plasmas into a gas slow?

Shock wave attenuation in argon plasmas

Ganguly, Bletzinger & Garscadden 21997

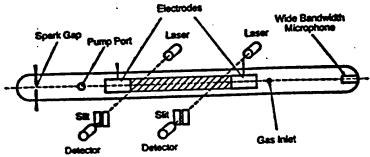


Fig. 1. Schematic of the experimental act-up.

- Sheek affervation d acceleration ID effects VT.
- · Shock splitting. ???

Ionisation unimportant, 2<<1?

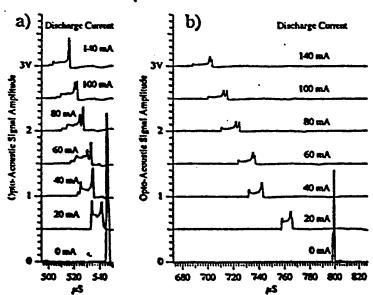
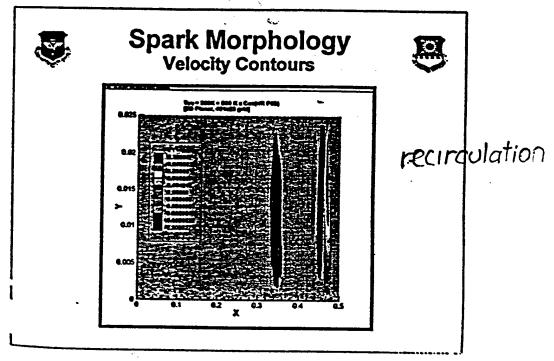
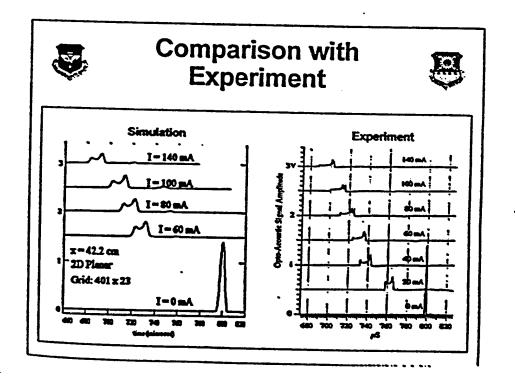


Fig. 2. Shock induced opto-acoustic signals in a 30 Torr argon discharge. (a) 30.2 cm from the spark source, (b) 42.2 cm from the spark source.

2D effects.

CFD of thermal effects, Bailey & Hilbun 1997.

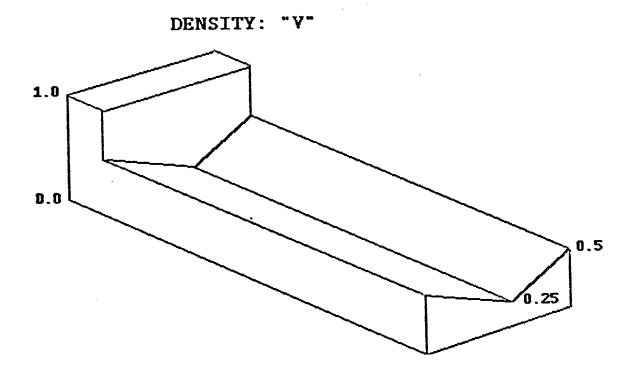




### 2D Shock Tube Simulation

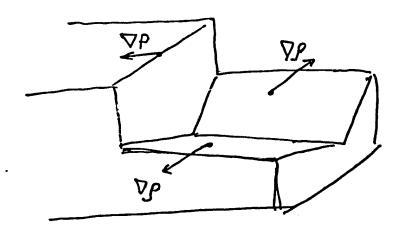
Left Boundary: p = 1.0; d = 1.0; u = v = 0
Right Boundary: p = 0.1; d = "V"; u = v = 0
(top and bottom B.C's are "reflecting slip")

Initially, these two states meet at a discont inuity.



### Baroclinic Vorticity Generation

$$\left[ \partial_{t} + (u \cdot \nabla) \right] \omega - (\omega \cdot \nabla) u = -\omega \nabla \cdot u - \nabla_{g}^{l} \times \nabla p$$
baroclinic
term



### Potential Vorticity Conservation

$$\left[\int_{0}^{\infty} \frac{\partial^{2} f}{\partial u} + (\vec{n} \cdot \vec{n}) + \hat{f} \vec{n}\right] = 0$$

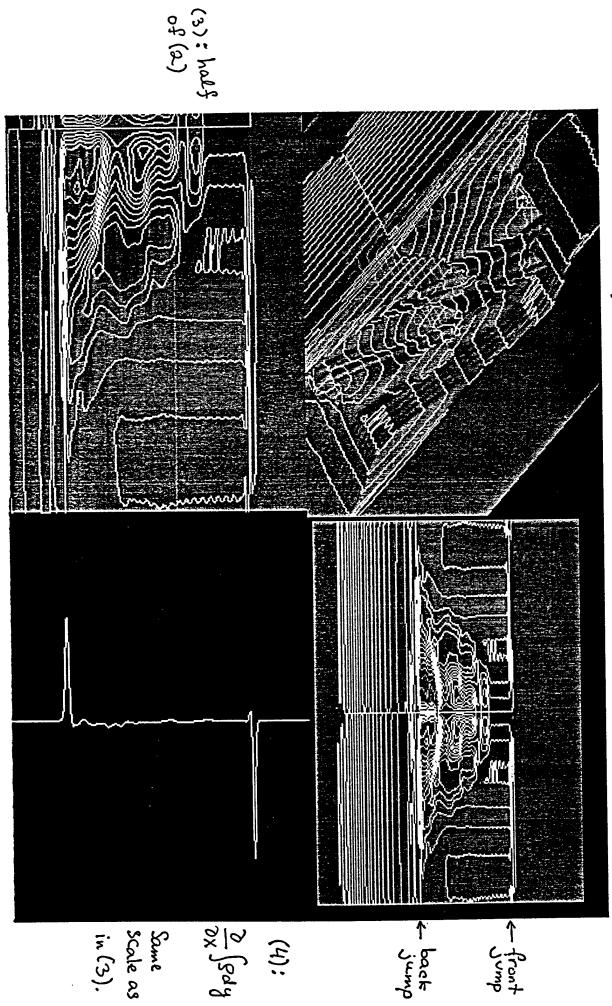
Potential vorticity  $\frac{\omega}{p}$  is conserved by each fluid element.

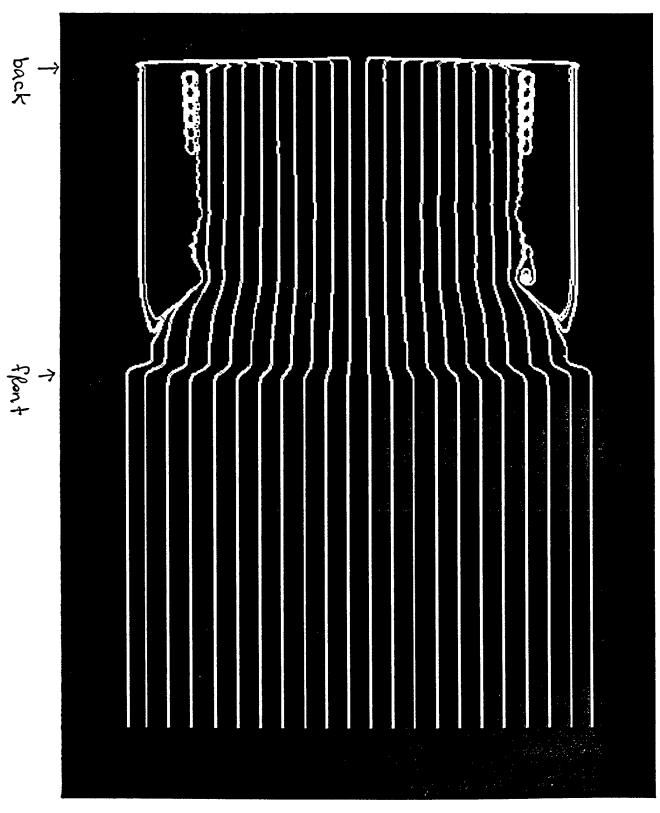
### SIMULATION METHOD:

(of the 2D Euler equations)

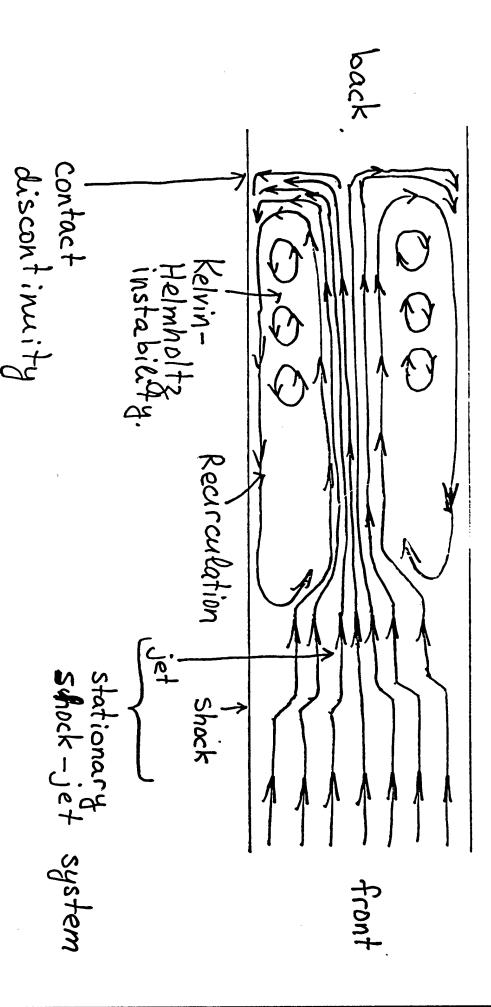
PHYSICAL ASPECT RATIO (x:y) = 100:1

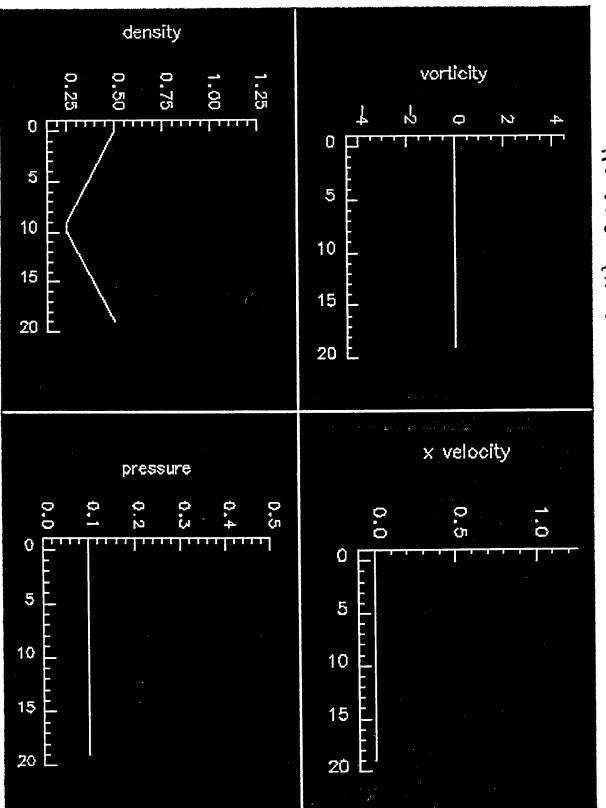
- # of gridpoints in x direction = 400
- # of gridpoints in y direction = 20
- # of ghostpoints = 3 (on each side)
- 1: Given the fluid parameters at each gridpoint, find the eigenvectors to Roe's matrices.
- 2: Use a 5th order weighted ENO scheme to find the flux eigenvectors at half gridpoints.
- 3: Use a 3rd order Runge Kutta routine to propagate the half gridpoint fluxes and find the new fluid parameters at the real gridpoints.
- 4: Repeat.



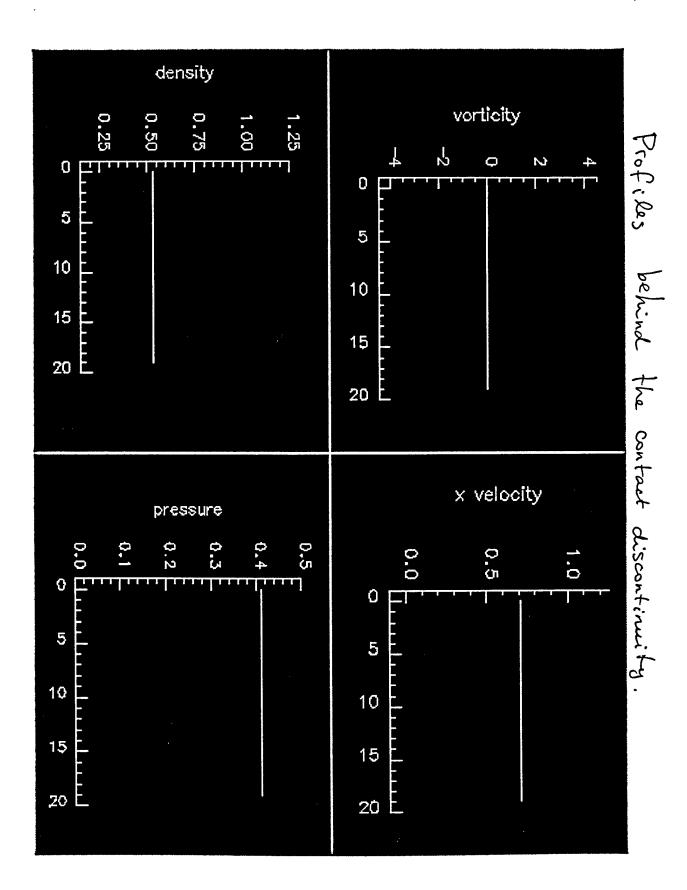


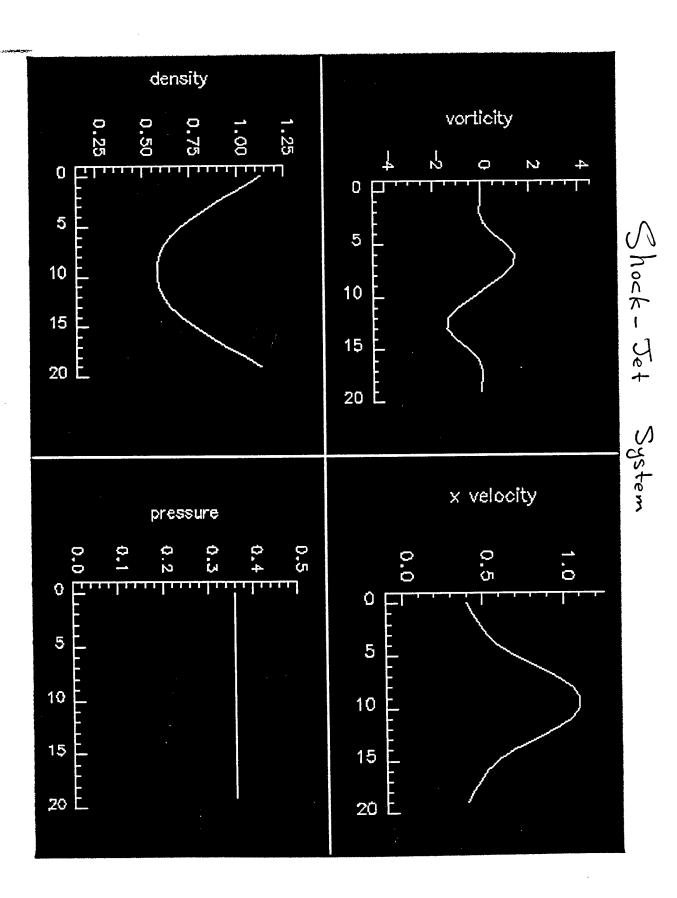
### Flow Structure

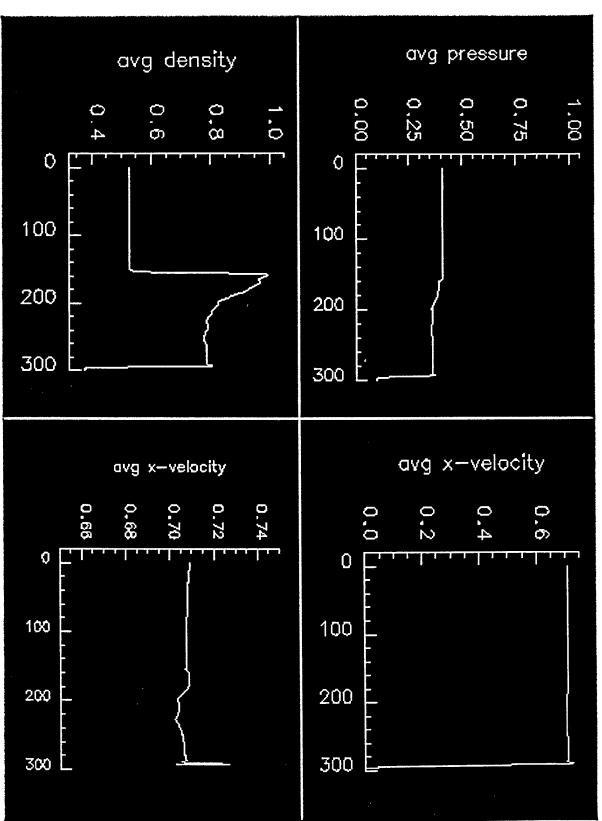


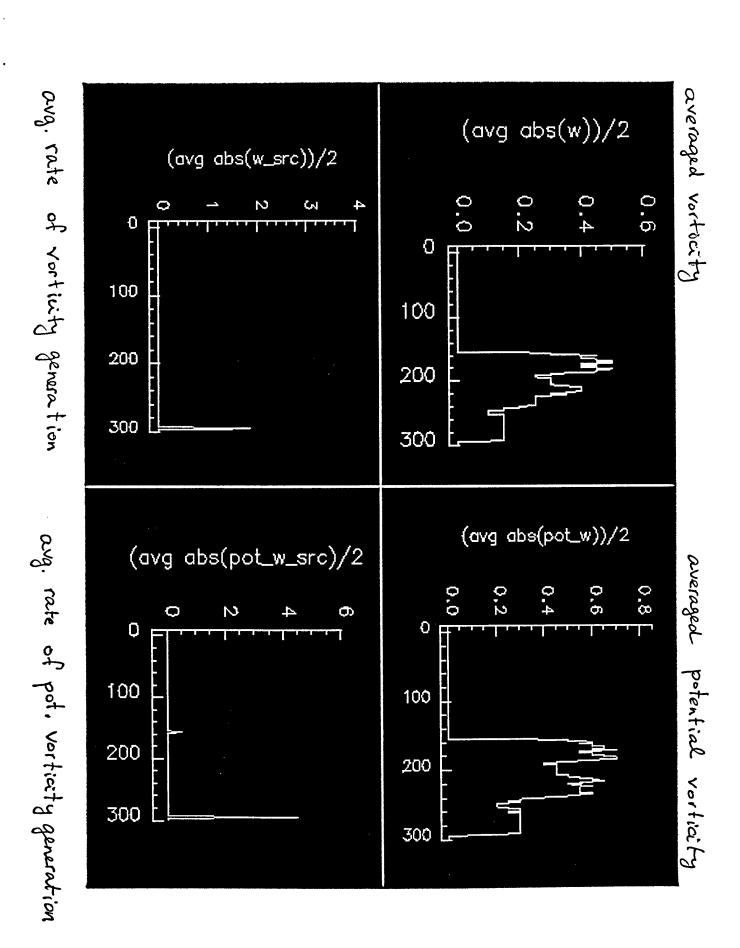


Profiles in front of the Shock









Research Support Instruments

# Further Investigation of Large Volume PIA (Persistent Ionizationin Air) Plasmas at Atmospheric Pressure

Mr. John F. Kline Dr. John E. Brandenburg Research Support Instruments Lanham, Maryland Presented at the Understanding and Control of

Ionized High-Speed Flows Workshop

Session IV: Plasma Generation and Maintenance

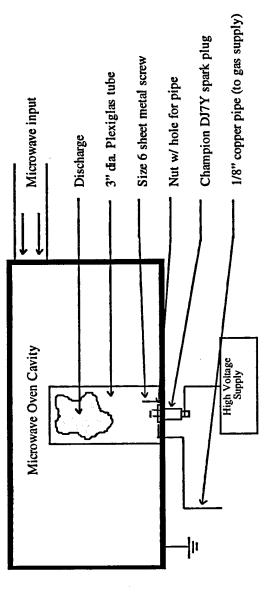
Princeton University

February 26, 1998

Research Support Instruments

# Materials and Methods 2.45 GHz (1)

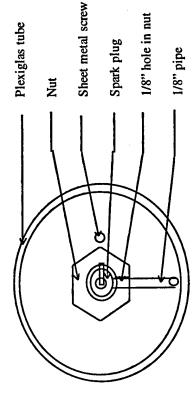
- Untuned cavity
- Field Enhancer
- Gas supply
- UV source
- Containment vessel



Research Support Instruments

# Materials and Methods 2.45 GHz (2)

- Top view of apparatus
- Gases stagnant air, nitrogen, argon, and helium
- Langmuir single probe
- Videocamera frame counting
- Microwave detector
- Photocell to measure light decay time



Research Support Instruments

# Materials and Methods 2.45 GHz (3)

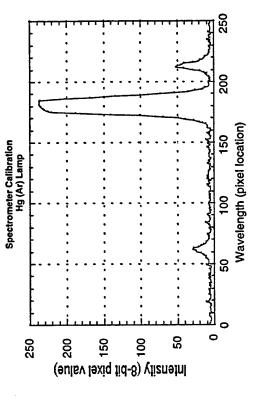
- Replacement of spark plug by laser induced breakdown
- » 1.06 μm, 0.3 1 J, 10 Hz Nd-Yag laser
- Field enchancement still necessary for microwave breakdown
- Elimination of field enchancer by using TM<sub>012</sub> resonant cavity
- Vortex ring generator to provide local E/P enchancement
- Loudspeaker with plastic cone using voltage pulses
- Shapes plasma into flat disc that follows vortex ring
- Emissions spectra measurements
- » 8-bit CCD viewing exit aperature of spectrometer
- Pixel values over a line give a time-resolved measurement over a broad 仌

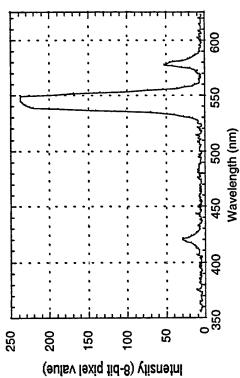
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Materials and Methods 2.45 GHz (4)



- Broad range of wavelengths
- Pixel depth vs. position yields intensity vs. wavelength
- Calibration using Hg (Ar) source

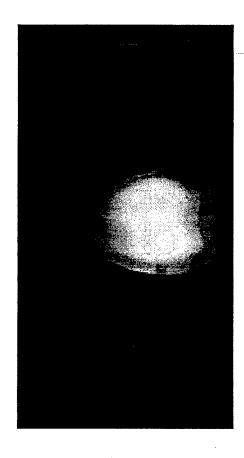




Research Support Instruments

# Results (1)

- Temperature 0.67 eV
- Density 10<sup>10</sup> cm<sup>-3</sup>
- Low neutral gas temperature
- Turbulent, with toroidal core
- Optimal flow rate 1.2 LPM
- Volume 280 cm<sup>3</sup> average
- Microwave shielding 1 order of magnitude increase with plasma (indicates 10<sup>11</sup> cm<sup>-3</sup>)

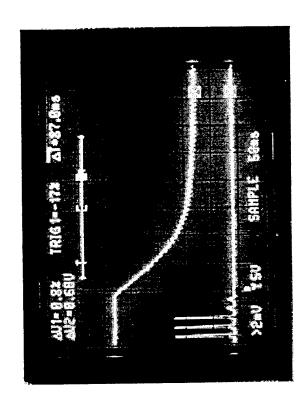


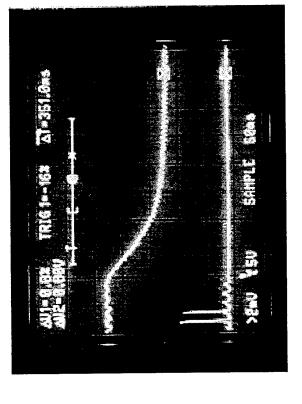


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# Results (2)

- Unpowered lifetime 200 ms average (3 e-folds at 60ms decay time)
- Upper channel shows photocell output
- Lower channel shows microwave detector output





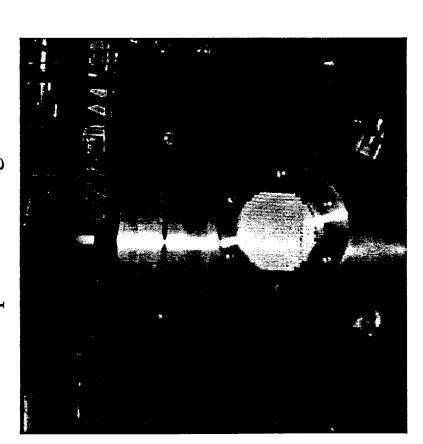
Air

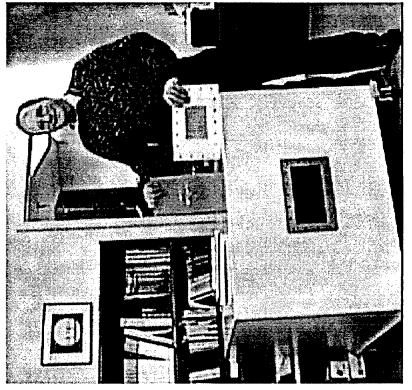
Argon

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# Results (3)

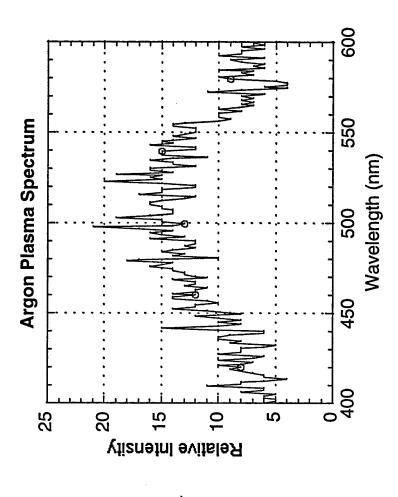
- Scaling of TM<sub>011</sub> resonant cavity to 0.915 GHz
- 45 kW operation using vortex-stabilized compressed air





# Results (4)

- Initial data on argon mixture
- Shows broad continuum (previously seen at Stanford)
- Can acquire time history data





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# Discussion

- Shared Electron Orbital (SEO) Hypothesis
- Decoupling of electrons from collisions with neutrals
- » Long collisional energy transfer times
- » Long recombination times
- Electrons shared between orbitals
- » Resemble conduction bands in liquid metals
- Vorticity suggests trapped magnetic fluxes and dynamo action (as in liquid metals) 仌

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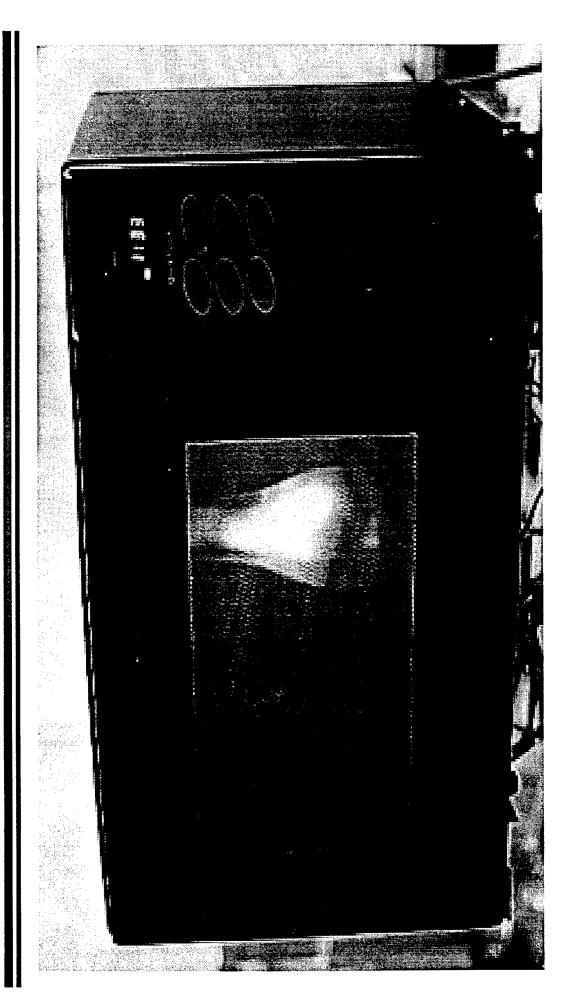
# Future Work

- Advanced diagnostics
- Continuing work on emissions spectra
- Triple probe with digital oscilloscope and function generator
- Investigate vorticity
- > Pulsed power vortex ring generator
- » Optically measure rotation



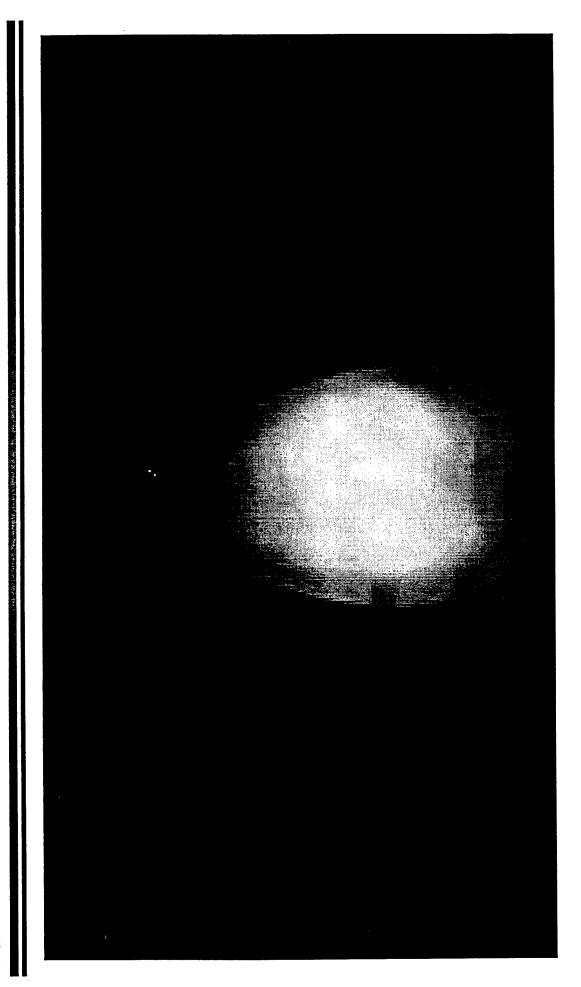
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Nitrogen Plasma - Low Flow



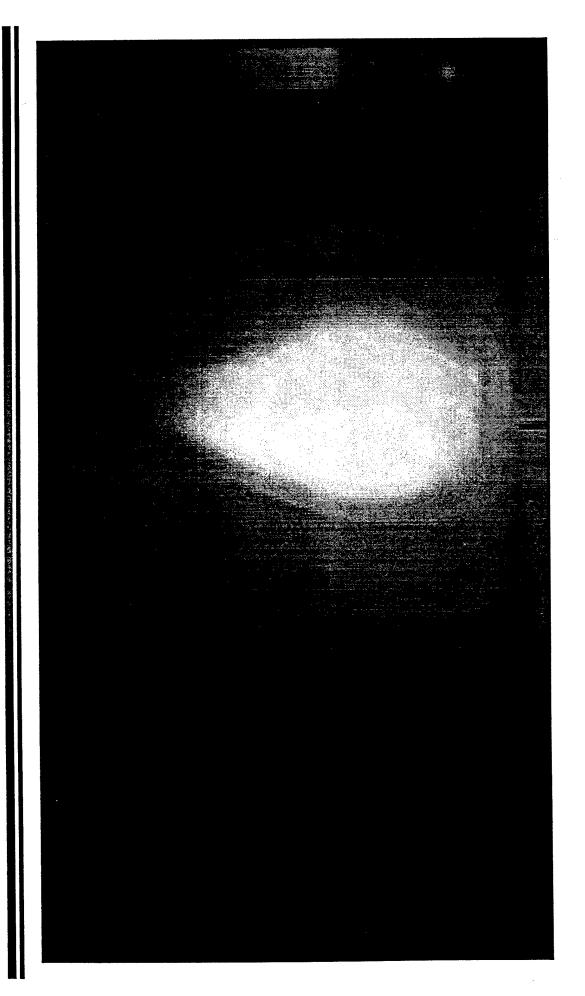
Research Support Instruments

Nitrogen Plasma - Stable



Research
Support
Instruments

Argon Plasma - Stable



## Plasma Torches and Their Demonstration

Spencer P. Kuo and Edward Koretzky

Department of Electrical Engineering

Polytechnic University

\*Work supported by the AFOSR

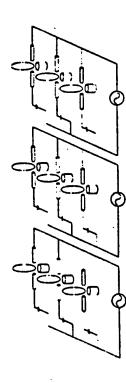


Figure 1.1: A schematic of the current arrangement for an array  $(3 \times 3)$  of plasma torches. Tungsten electrodes are used. Each electrode pair is facilitated with an air jet nozzle.

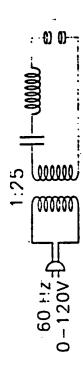
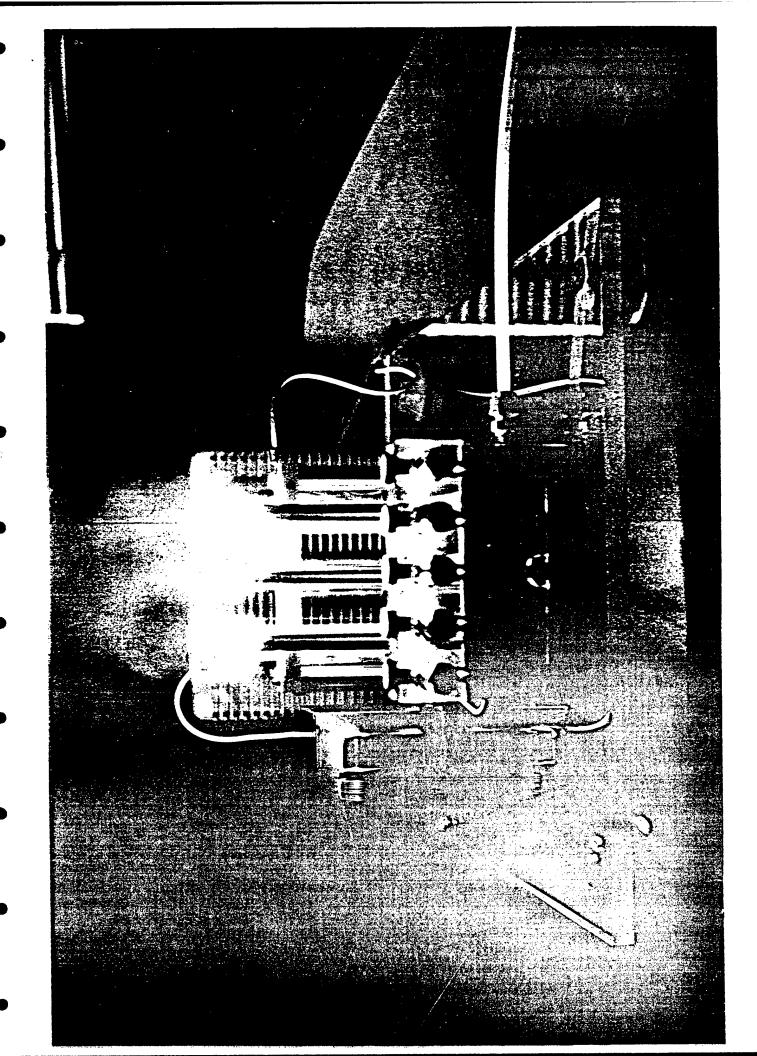
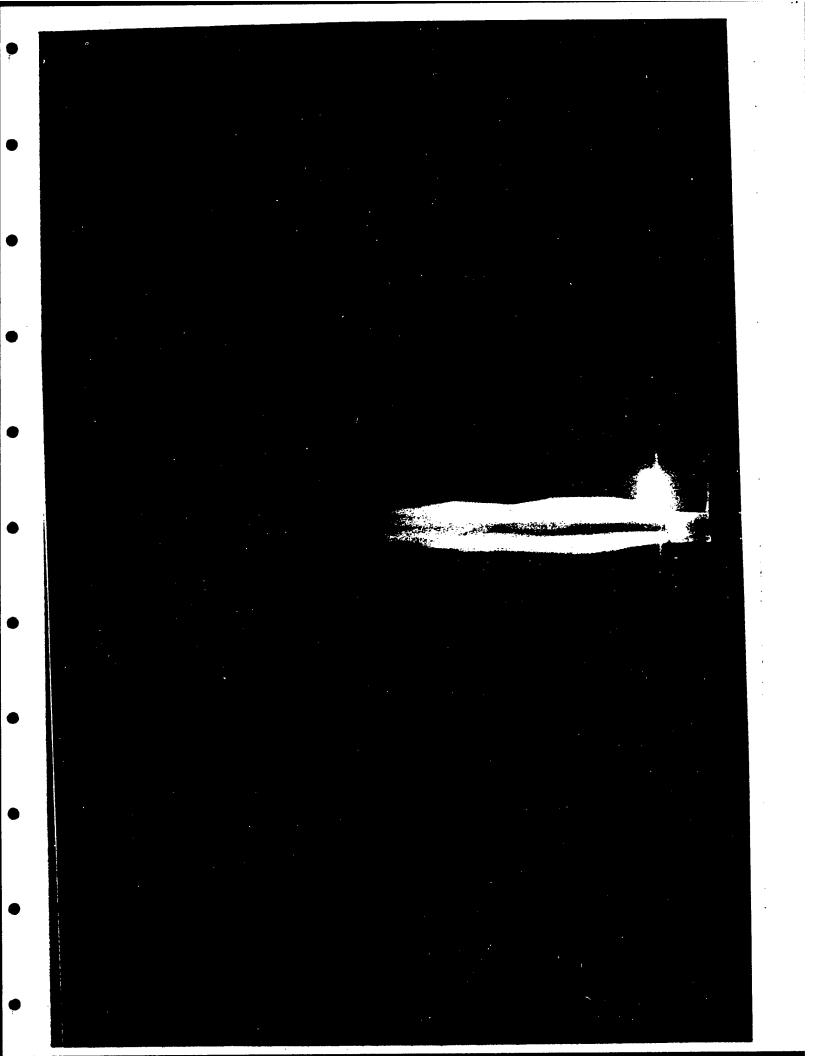
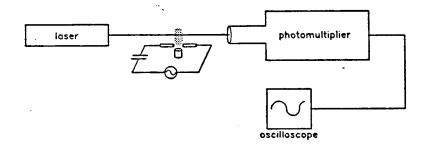
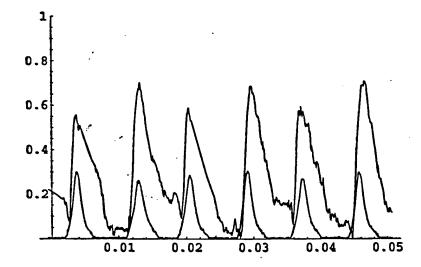


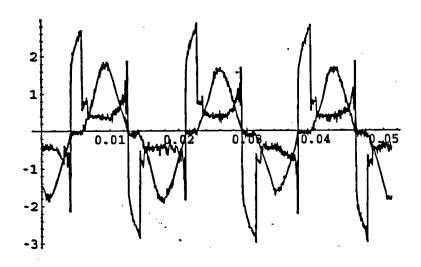
Figure 1.2: Circuit diagram of the plasma torch.

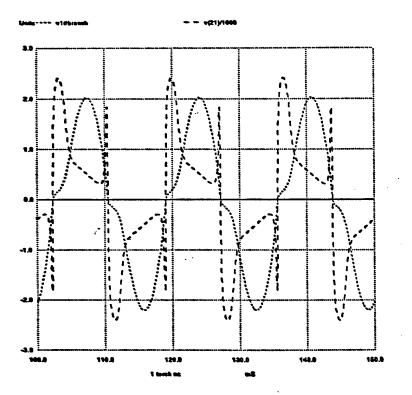


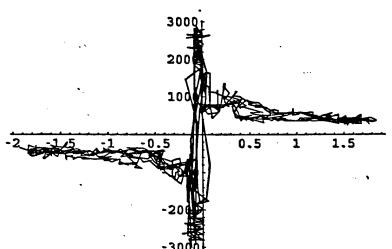


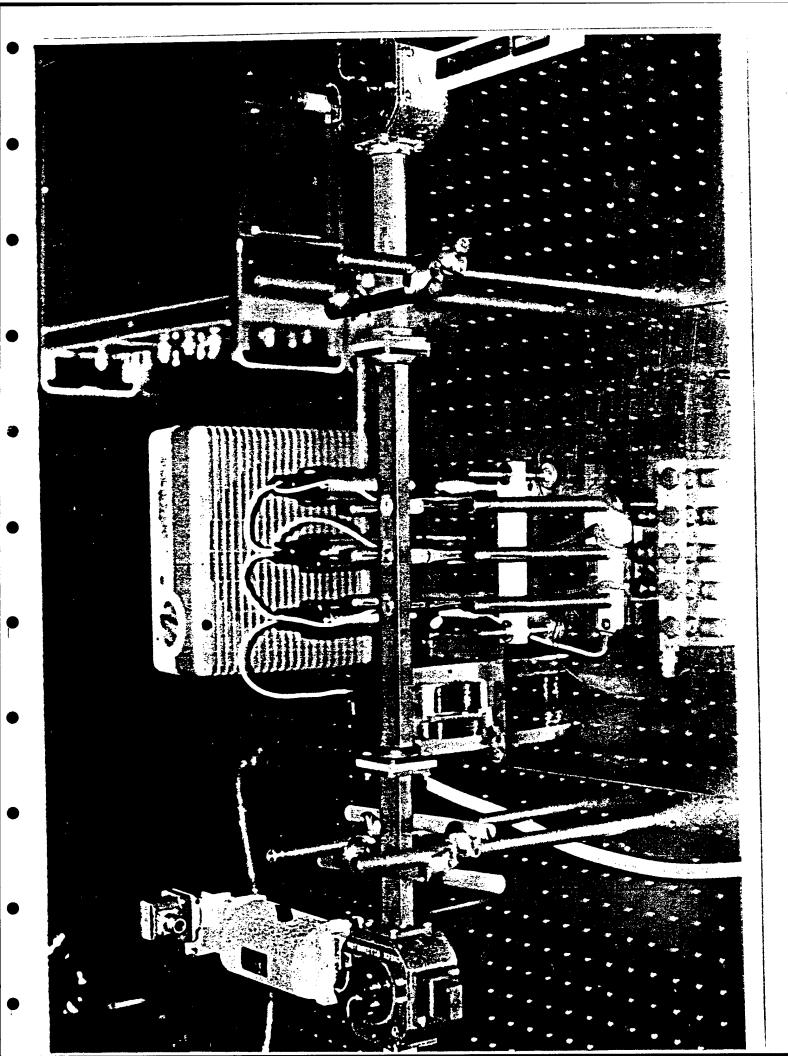


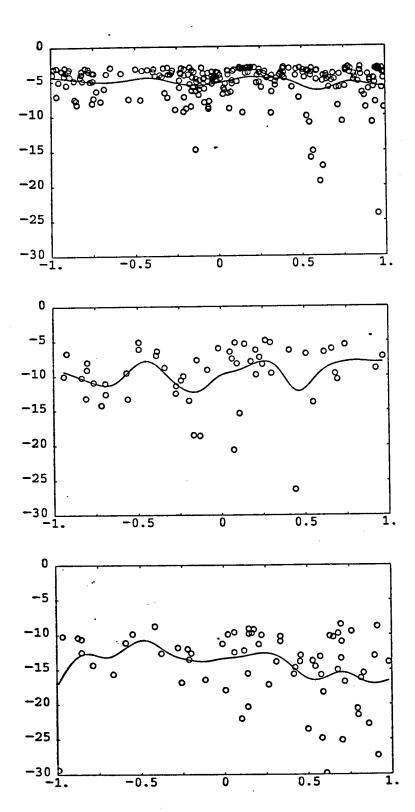


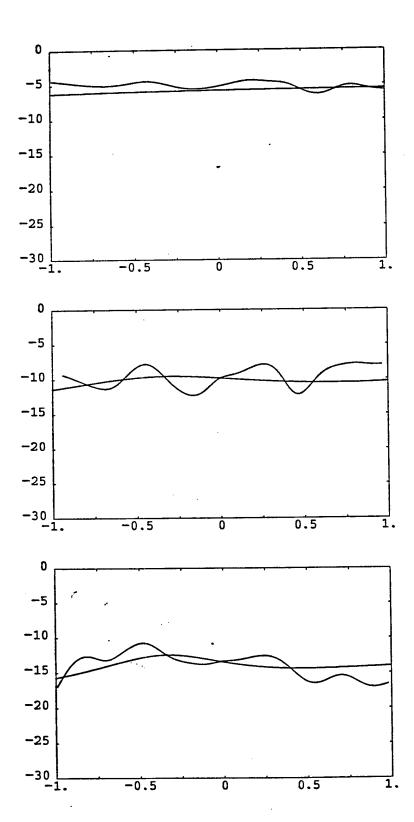












### Plasma Torch

Pressure:

1 ATM

Density:

 $1.5 \times 10^{13}$  (deduced from mea-

surements based on two inde-

pendent methods)

Temperature:

 $1200^{\circ}K$ 

Dimensions:

cylindrical shape having 1 cm

radius and  $7~\mathrm{cm}$  length

Volume:

 $20 \text{ cm}^3/\text{torch}$ 

Power Consumption:

600 W/torch

Peak Voltage and Current: 2.8 kV and 2 A

## Microwave Plasma Layers

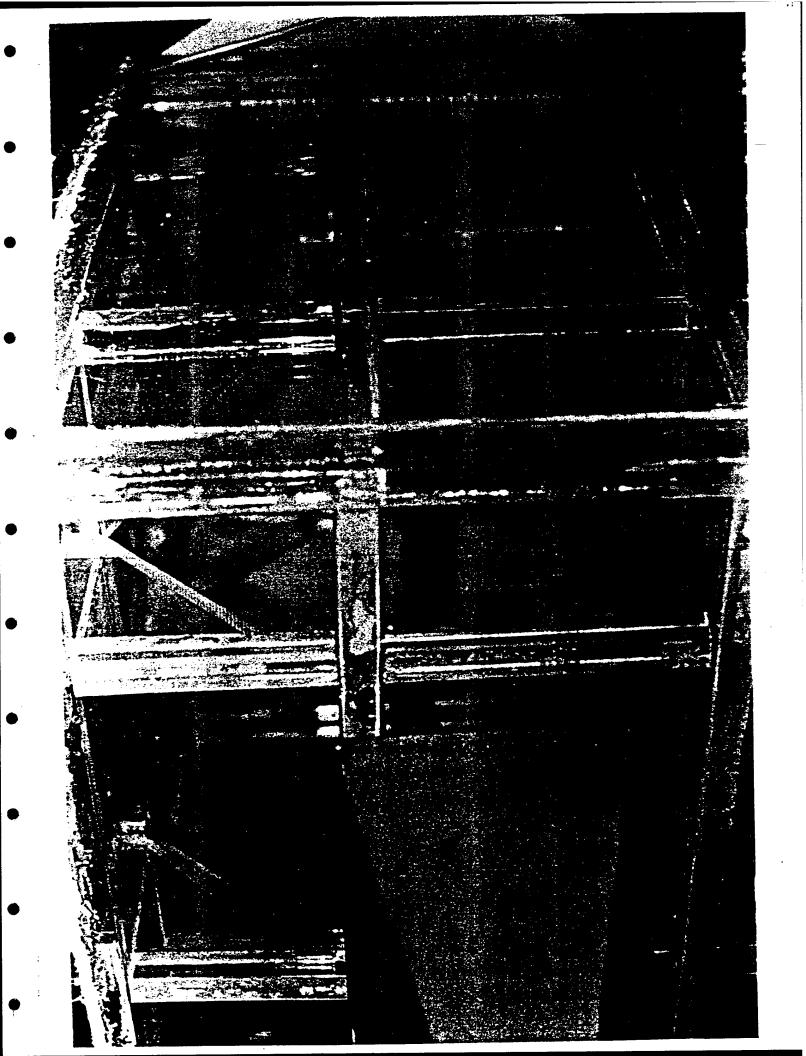
Pressure:

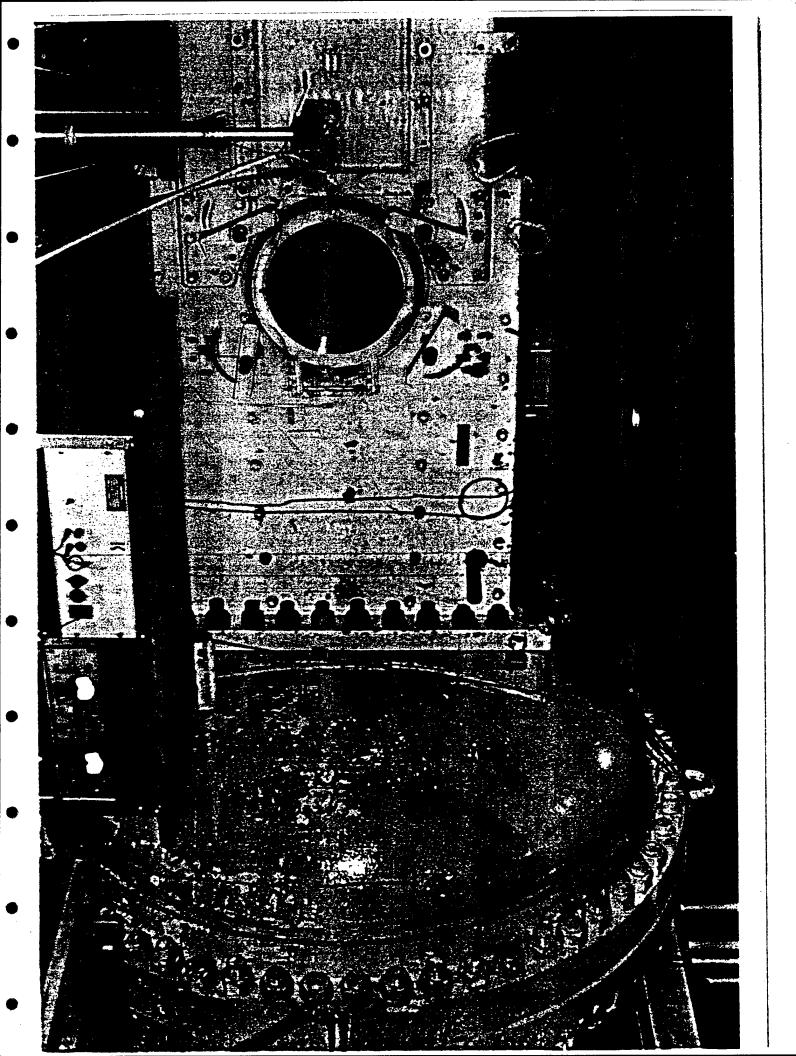
20 torr

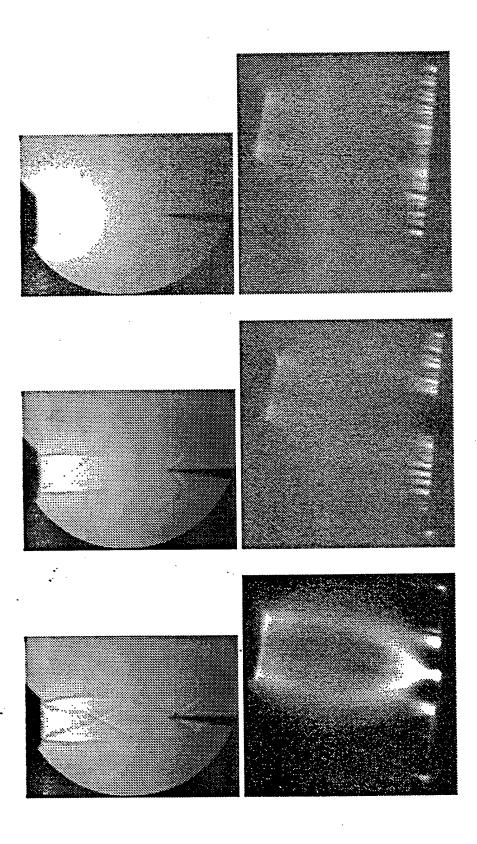
Density:

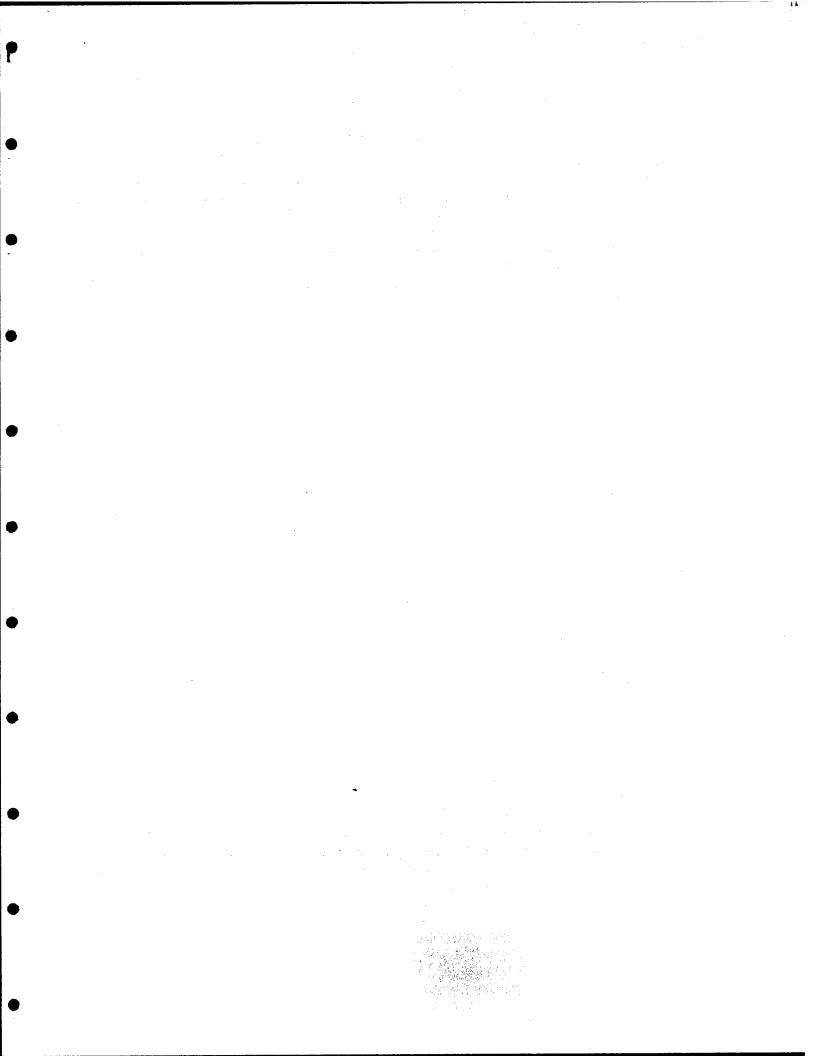
 $10^{11} \text{ cm}^{-3}$ 

Microwave Power: 1 MW peak, 1  $\mu$ s pulse, 40 rps









# Plasma Ramparts Using Metastable Molecules

**MURI Program** 

The Ohio State University Princeton University

"Optically Pumped Nonequilibrium Plasmas"

I. Adamovich, V. Subramaniam, W. Rich

Presented at

AFOSR Workshop
"Understanding and Control of
Ionized High-Speed Flows"

Princeton University Feb. 26-27, 1998

Work funded by the Director of Defense Research & Engineering (DDR&E) within the Air Plasma Ramparts MURI Program managed by AFOSR

Nonequilibrium Thermodynamics Laboratories

### The Ohio State University

### **Program Objectives:**

- Create large volume (O[m³]) free air plasma
- One atmosphere
- Free electron densities 10<sup>13</sup> cm<sup>3</sup> or greater
- Gas temperature less than 2,000 K
- Energy efficient method

### **Approaches:**

A. Thermal Plasmas (High Temperature Arcs, Reentry Plasmas)

### **Problems:**

- I) High Temperature
- B. NonThermal Plasmas (Glow Discharges, Optically Pumped Plasmas)

### **Problems:**

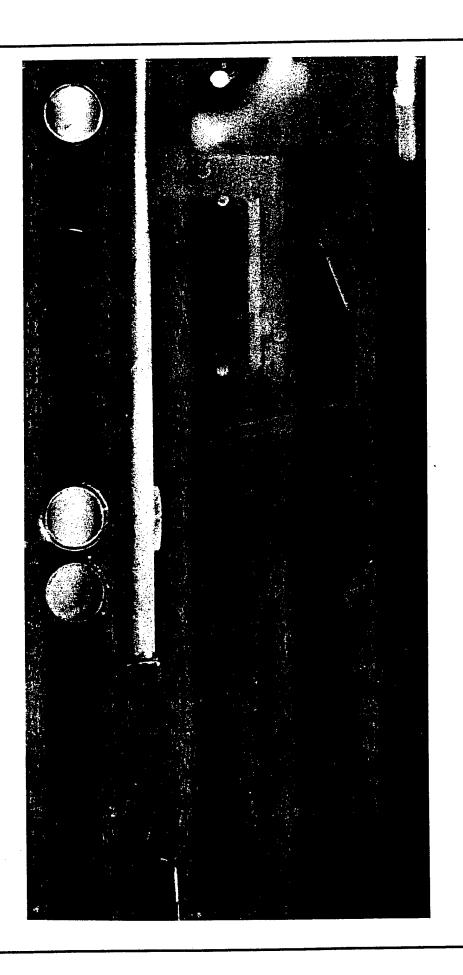
- I) Requires thermodynamic work (electrical work, laser work)
- II) Stability

OSU/Princeton Approach: Laser Pumped Metastable State Plasmas.

Nonequilibrium Thermodynamics Laboratories

### 92 W cw broad-band lasing conditions

Date: 10-	26-1992					
Gas	Partial Pressure (Torr)	mass flow rate (10 <sup>3</sup> g/min)				
He internal purge	4.15	18.9				
He	9.00	75.5				
N <sub>2</sub>	2.75	138				
co	1.60	6.61				
Air	.01	.89				
Total	17.5	239				
He:CO:N <sub>2</sub>	molar rati	o 751:92:157				
Discharge Conditions						
Current mADC		45				
Voltage kVDC		18				
Laser Power Broad Band W		92				
Physical Efficiency		30.3%				



### Advantages:

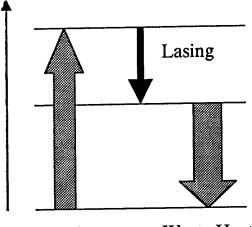
- Stable, large volume
- High pressure
- Low gas temperatures

### **Problems:**

- Electron density
- Efficiency
- Non-air species

### Three Level Laser

### Energy



Pumping

Waste Heat

Upper level energy: Eu

Lower level energy: EL

Ground level energy:  $E_0=0$ 

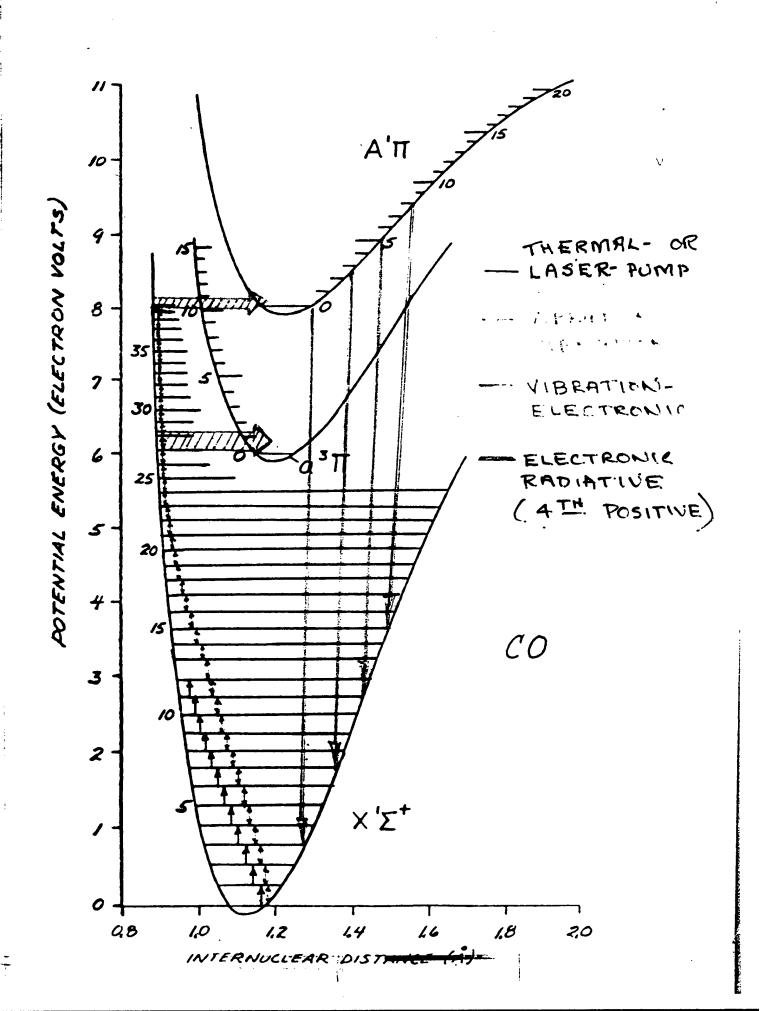
### Quantum Efficiency

$$\eta_{quantum} = \frac{E_U - E_L}{E_L}$$

 $\sim 40\%$  for CO<sub>2</sub>/N<sub>2</sub>

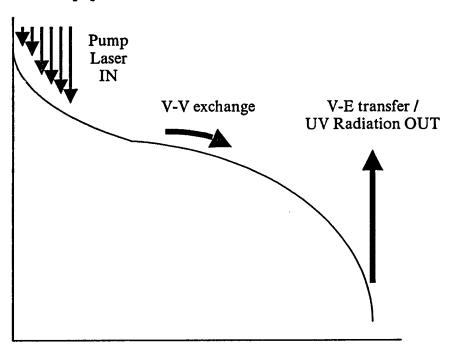
 $\sim 95\%$  for CO/N<sub>2</sub>

Scoville, 1954 showed equivalence with reversible engine efficiency

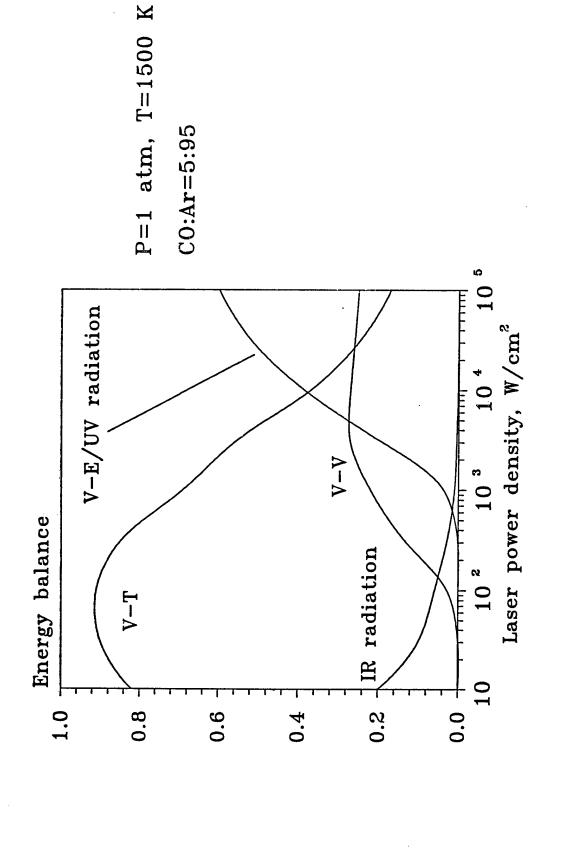


### IR/UV Radiation Conversion in Optically Pumped CO-Ar Plasma

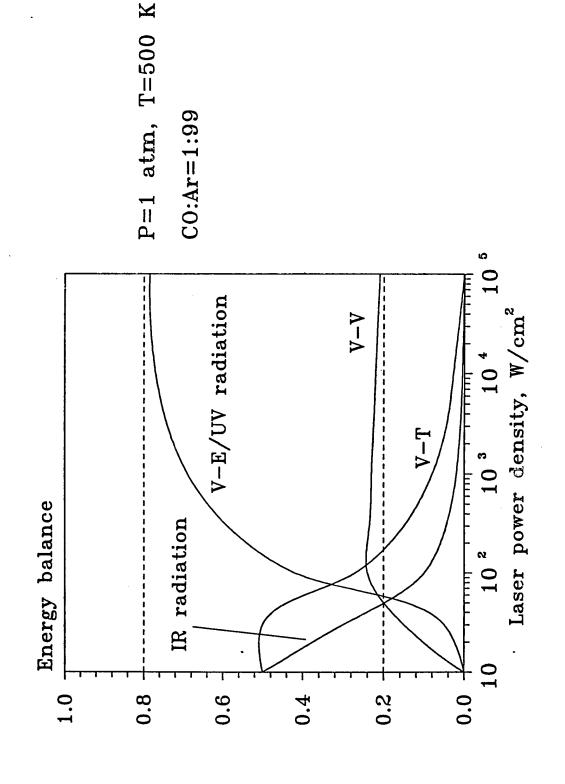
Relative population

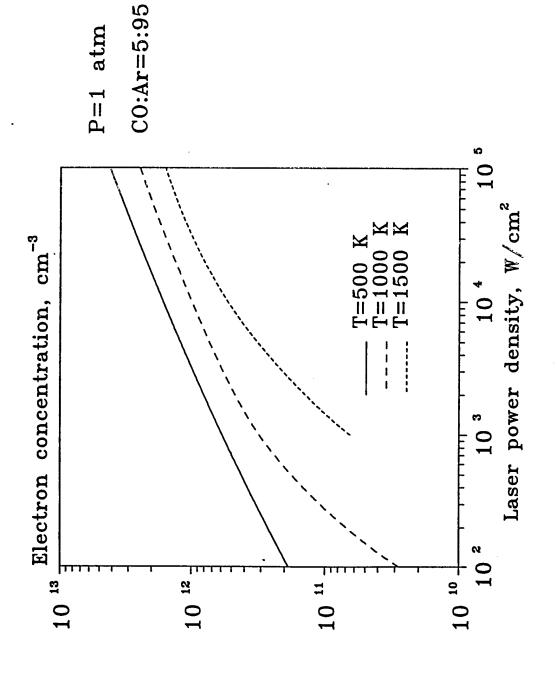


Vibrational Quantum Number



Nonequilibrium Thermodynamics Laboratories

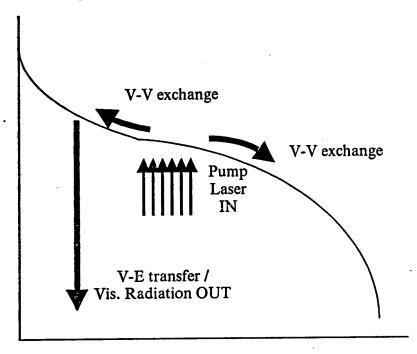




Nonequilibrium Thermodynamics Laboratories

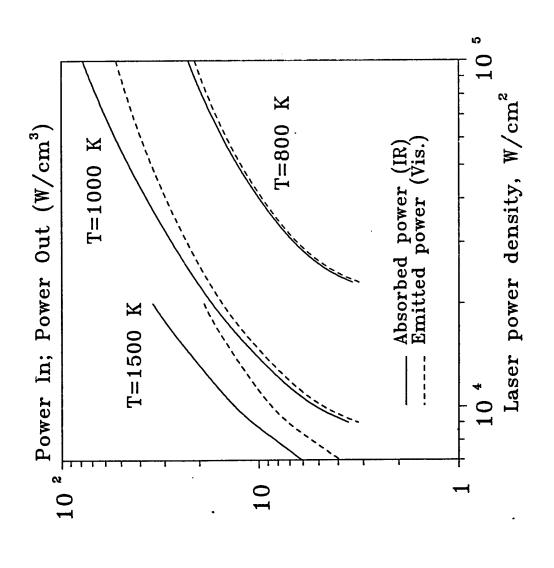
### IR/Visible Radiation Conversion in Optically Pumped CO-N2-Na Plasma

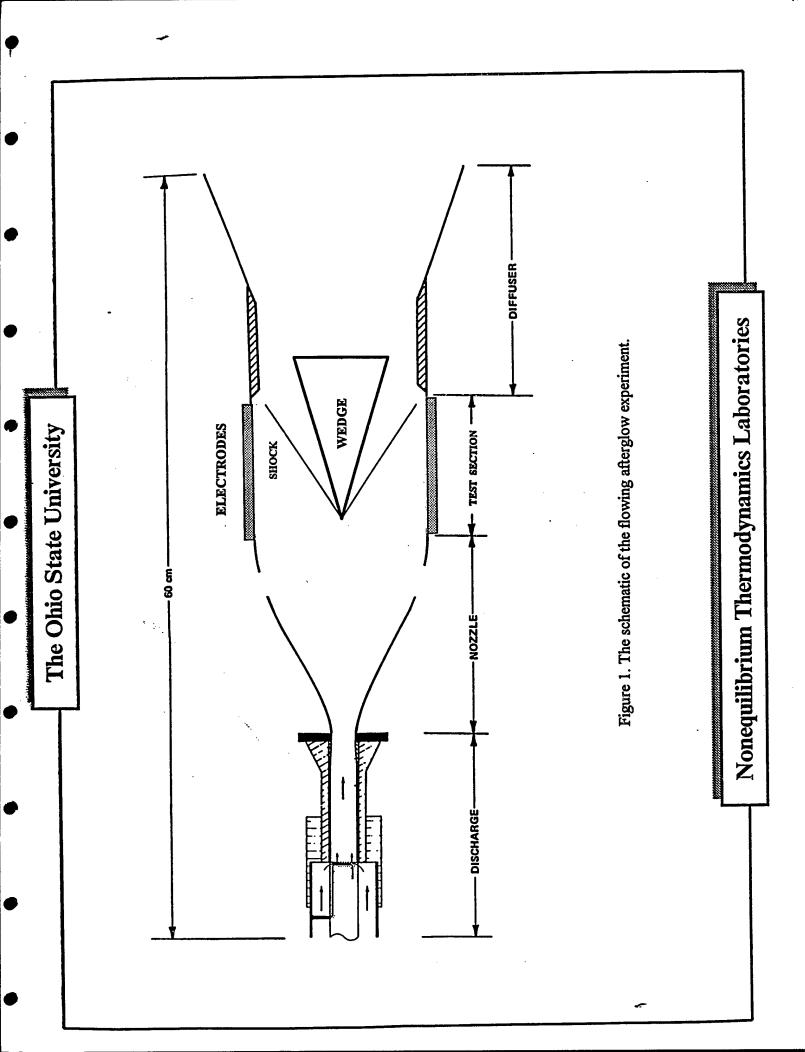
Relative population



Vibrational Quantum Number









### GRADIENT DISTORTION EXPERIMENT

• Transverse temperature gradient is created by absorption of CO laser radiation (1-2% CO is added to the flow to enable absorption and as a thermometric element).

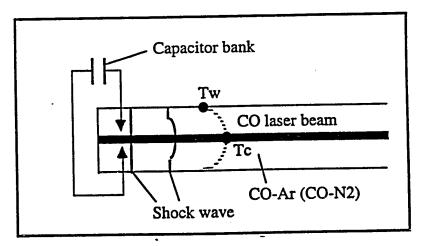
At P=100 Torr, dT/dr ~ 100 K/cm

Routinely used in CO and NO optical pumping kinetic experiments.

• Plane shock wave created by a capacitor bank discharge.

### Measurements of:

- flow density distribution
- Gas temperature and transverse temperature gradient before the shock arrival

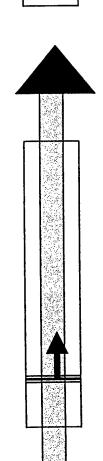


• Radial temperature profile is parabolic:

$$T(r) = T_C - (T_W - T_C)(r/R)^2$$

## Experimental verification

Repeat Ganguly-Bletzinger experiment with thermal effects alone - pure, non-intrusive gas heating induced in CO-seeded Argon, using optical pumping.



Axially directed CO laser beam

Transverse directed



Non-Equilibrium Thermodynamics Laboratories & Center for Advanced Plasma Engineering



# Experimental Validation

Body in wind-tunnel; Thompson discharge by photo-ionization Flow Flow Flow

February 17, 1998

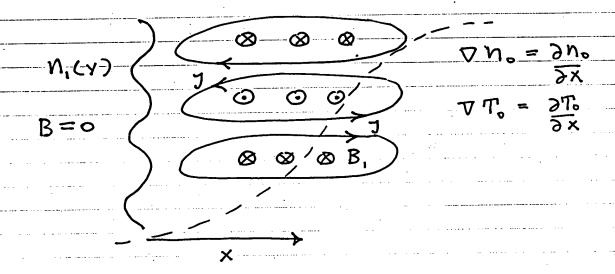
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## OHM'S LAW IN LIMIT OF HIGH DENSITY AND LOW CONDUCTIVITY Ωe→o, Rm→o CEXPECTATION THAT PLASMA IS TOO RESISTIVE INITIALLY TO PERMIT FLUX CONVECTION ) $\frac{\partial \vec{B}}{\partial t} = -\nabla \times (\gamma \vec{J}) - \left(\frac{k}{\epsilon}\right) \frac{\nabla n_e \times \nabla \vec{T}_e}{n_e}$

### QUALITATIVE BEHAVIOR



VNXVT TERM CAUSES GROWTH

OF MAGNETIC FIELD INTO AND OUT OF PLANE

AND ASSOCIATED IN-PLANE CURRENTS

TENDENCY TO TRANSFER AND CONCENTRATE

ENERGY FROM REGIONS OF GENERATION

TO REGIONS . OF DISSIPATION

$$P_d = -\vec{E} \cdot \vec{j}$$

(CURRENT DENSITY DIRECTION ALTERNATES

MAIN PRESSURE-GRADIENT INDUCED

ELECTRIC FIELD MAINTAINS DIRECTION)

### POSSIBLE NONLINEAR EFFECTS RESISTIVE HEATING MAY CHANGE PLASMA $7J^2 \rightarrow dT_e$ CHANGING PLASMA MAY CHANGE TRANSPORT 7 = 7 (ne, Te) $\mathcal{X} = \mathcal{X} (n_e, T_e)$ THESE CHANGES GREATLY COMPLICATE THE ARITHMETIC, BUT MAY BE CRITICAL FOR DESCRIBING EXPERIMENTAL BEHAVIOR FURTHER CONCENTRATION OF CURRENTS AND IONIZATION OPPORTUNITY FOR HEAT TRANSPORT AT SHOCK VIA HOT COLUMNS

 LINEARIZED ANALYSIS
 LOOK FOR ELEMENTS OF BEHAVIOR
 WITH SIMPLIFIED ARITHMETIC
 LET MAIN FLOW CARRY PRESSURE GRADIE
 $\frac{\partial P_0}{\partial x}$
 TRANSVERSE VARIATION OF DENSITY
 AND TEMPERATURE AT FIXED PRESSURE
 $\frac{\partial n_i}{\partial y}$ , $\frac{\partial T_i}{\partial y}$ with $\frac{\partial P_i}{\partial y} = 0$
 SOLVE FOR VARIATION OF (WEAK) MAGNETIC
 FIELD AS FUNCTION OF BOTH X AND Y
$\vec{B} = B\hat{k} = B_0 + \epsilon B_1(x,y)$
WITH BOEKEI

### LINEARIZED ANALYSIS (CONTINUED) $N(x,y) = N_0(x)(1 + \epsilon si \sim Ky)$ AT dP/dy=0, THEN 7 (x,y) = 7. (x) (1-Esinky) NHERE POLX) = No. R. To NOT STAGNATION フ=ク0+モグ, INTO FARADAY'S LAW YIELDS AT OCE): $\frac{\partial B_{i}}{\partial t} = \frac{1}{\sqrt{2}} \left\{ \gamma_{0} \left( \frac{\partial^{2} B_{i}}{\partial x^{2}} + \frac{\partial^{2} B_{i}}{\partial y^{2}} \right) + \frac{\partial B_{i}}{\partial x} \left[ \left( \frac{\partial \gamma_{0}}{\partial n_{0}} \right) \frac{\partial n_{0}}{\partial x} + \left( \frac{\partial \gamma_{0}}{\partial z} \right) \frac{\partial n_{0}}{\partial x} \right] \right\}$ + Kcosky 2Po STEADY STATE, $\frac{\partial B_i}{\partial t} = 0$ $\left(\frac{7}{3}\right)\left[\frac{3^{2}B_{1}}{3^{2}X^{2}} + \frac{3^{2}B_{1}}{3^{2}Y^{2}}\right] + \frac{3}{1}\frac{3}{3}\left[\left(\frac{3}{3}\frac{7}{n_{e}}\right)\frac{3}{3}\frac{1}{X} + \left(\frac{3}{3}\frac{7}{n_{e}}\right)\frac{3}{3}\frac{1}{X}\right]$ = - Kcos Ky 2 Po en. 7x

## LINEARIZED ANALYSIS (CONTINUED) $B,(x,y) = b(x) \cos Ky$ WHICH PROVIDES EQUATION ! $\left(\frac{70}{\text{d}}\right)\left[\frac{d^2b}{dx^2}-K^2b\right]+\frac{1}{\text{d}}\frac{db}{dx}\left[\left(\frac{370}{370}\right)\frac{3n_0}{3x}+\left(\frac{370}{370}\right)\frac{370}{3x}\right]$ $= -\frac{K}{e\eta_0} \frac{dP_0}{dx}$ EXPLORE SIMPLER CASE : LET 70 = CONSTA $\left(\frac{70}{m}\right)\left[\frac{d^2b}{dx^2} - K^2b\right] = -\frac{10}{e^{10}}\frac{d^{10}}{dx}$ $\frac{d^2b}{dx^2} - K^2b = -\frac{mk}{7.6} \frac{dP_0}{dx}$

### NORMALIZED EQUATIONS LET $P_0(x) = bc^2 p(\alpha)$ WHERE $\alpha = x/\chi$ $b(x) = b_c f(x)$ $= \frac{b_c^2}{2\mu k T_c \theta(\alpha)}$ $n_o(x) = P_o(x)$ k 7. (x) THEN PROVIDES! $\frac{d^2f}{d\alpha^2} - 4\pi^2f = -\left(\frac{2\pi nkT_e}{70ebc}\right)\frac{\theta(\alpha)}{\beta(\alpha)}\frac{d\beta}{d\alpha}$ FURTHER SIMPLIFIES $\frac{d^2f}{d\chi^2} - 4\pi^2f = -\frac{\Theta(\chi)}{\beta(\chi)} \frac{d\beta}{d\chi}$ By DEFINING be = 2Th h Tc

### SOLUTION OF NORMALIZED EQUATION HOMOGENEOUS PART! $\frac{d^2f_H}{d\alpha^2} = 4\pi^2f_H$ $f_{\mu} = c_{1}e^{2\pi\alpha} + c_{2}e^{-2\pi\alpha}$ PARTICULAR SOLUTION, WITH FURTHER SIMPLIFICATION 0=1, $\frac{d^2f_p}{d\alpha^2} - 4\pi^2f_p = -\frac{1}{5}\frac{d\beta}{d\alpha}$ TRY FORM OF fo (X) THAT PROVIDES USEFUL FORM FOR BCX): $f_{\rho}(x) = a sin(m\pi x)$ THIS GIVES (BY SUBSTITUTION AND INTEGRATION): $\alpha = 0$ , $\beta = \beta_1$ & = Ym , B = MAXIMUM THICKNESS OF PRESSURE RISE: B(K) ... 7 = 1/m ( WHICH GIVES M )

1/m

ITM $b_1 = 0$ AT $X = 0$ $\left( \frac{f(0) = 0}{\sqrt{2}} \right)$ AND $db_1 = 0$ ALSO $df = 0$ WE FULL SOLUTION IS! $B_1(x,y) = \frac{\sqrt{2}}{\sqrt{2}} \frac{2}{\sqrt{2}} \frac{\sqrt{2}}{\sqrt{2}} \frac{\sqrt{2}}{\sqrt{2}} \frac{\sqrt{2}}{\sqrt{2}} \frac{\sqrt{2}}{\sqrt{2}} $
AND $db_1 = 0$ ALSO $df = 0$ $dx$ WE FULL SOLUTION IS! $B_1(x,y) = \mu k T_0 \cos(\frac{2\pi y}{\lambda}) \frac{(\lambda/2) \ln k}{(\frac{\lambda}{2})^2 - 4}$
B, $(x,y) = \frac{nkT_0}{70e} \cos(\frac{2\pi y}{3}) \frac{(3/2)lnk}{[(\frac{3}{2})^2-4]}$
$B_{1}(x,y) = \frac{nkT_{0}}{7_{0}e} \cos\left(\frac{2\pi y}{3}\right) \frac{(3/2) \ln k}{\left[\left(\frac{3}{2}\right)^{2} - 4\right]}$
$\int sin\left(\frac{\pi \times}{2}\right) - \frac{\lambda}{22} sinh\left(\frac{2\pi \times}{\lambda}\right)$
WHERE A IS THE WAVELENGTH OF TRANSVERSE PERTURBATIONS OF PLAS
Z IS THE COMPRESSION THICKNESS
AND IS THE PRESSURE RATIO
THE SOLUTION IS RESTRICTED TO
0 ≤ x ≤ 2 // <sub>2</sub> > 2
(AND LINEARIZED ANALYSIS)
IT CAN MATCH TO XZZ WITH UNIFORM PRESSURE,

 CONCLUDING REMARKS
INTERACTION OF COMPNESSION WAVE WITH FIELD-FRE
NONHOMOGENEOUS PLASMA CAN GENERATE
CULRENT CONCENTRATIONS DUE TO VIXYT PROCE
MAGNITUDES OF CULLENT DENSITIES INCREASE
EXPONENTIALLY AS X/7 (FOR LINEARIZED
SOLUTION ) THROUGH THE THICKNESS OF
Compression
NONLINEAR EFFECTS IN PLASMA MAY RESULT
IN FURTHER CONCENTRAJON AND INCREASED
TRANSPORT
THE RESULT OF SUCH CONCENTRATION OF
ENEMAY AND # INCREASED TRANSPORT MAY
BE CHANGE IN FLOW STRUCTURE AND
RELATED AERODYNAMIC DRAG

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